# MODEL QUESTION PAPER

# MATHEMATICS – Paper II B (Coordinate Geometry and Calculus)

Max Marks: 75

#### Section - A

- I. Very Short Answer Questions 10x2=20 Marks Attempt all Questions. Each Question carries 2 marks.
- 1. If  $x^2 + y^2 4x + 6y + c = 0$  represents a circle with radius '6', find the value of 'c'.
- 2. Find the equation of the directix of the parabola  $2x^2 + 7y = 0$ .

3. Find the length of the latus rectum of the ellipse 
$$\xrightarrow{}$$
  $+$   $=$  1

- 4. Find the eccentricity of the hyperbola  $x^2 4y^2 = 4$
- 5. Find the distance between the two points in a plane whose polar coordinates are  $(2, \pi/6)$   $(3, \pi/4)$

6. If 
$$y = \frac{1}{2x + 5}$$

Time: 3 Hours

7. Find 
$$\int \sqrt{1 + \sin 2x} \, dx$$

8. Find 
$$\int \frac{e^{\sin - 1} x}{\sqrt{1 - x^2}} dx$$

9. Obtain 
$$\int_{1}^{4} x \sqrt{x^2 - 1} \, dx$$

10. State the Simpson's rule for Numerical Integration of a function f(x) over the interval [a,b] by dividing [a,b] into n sub-intervals.

#### Section - B

II. Short Answer Questions

$$5 \times 4 = 20 \text{ Marks}$$

Attempt any five questions. Each question carries 4 marks

11. If the line y = mx + c touches the ellipse  $\frac{x^2}{a^2} + \frac{y^2}{b^2}$ 

$$c^2 = a^2 m^2 + b^2$$
;  $(a > b)$ 

- 12. Find the equations of the tangents shown drawn from (-2,1) to the hyperbola  $2x^2 3y^2 = 6$ .
- 13. Transform the polar equation  $r \cos^2 \theta = a$  (a>0), origin as pole and the 2 +ve axis as initial line, into Cartesian form.
- 14. If  $y = \frac{\log x}{x}$  then show that

$$y_n = \frac{(-1)^n \angle n}{x^{n+1}} \left[ \log x - 1 - \frac{1}{2} - \frac{1}{3} \dots \frac{1}{n} \right]$$

15. Evaluate 
$$\int \frac{x^6 - 1}{1 + x^2} dx$$

16. Solve 
$$(x^2 + y^2) dx = 2 xy dy$$

17. Solve 
$$\frac{dy}{dx} = \frac{2x+y+3}{2y+x+1}$$

#### Section - C

 $5 \times 7 = 35 \text{ Marks}$ 

II. Long Answer Questions

Attempt any five questions. Each question carries 7 marks

- 18. Find the equation of the pair of tangents drawn from (3,2) to the circle  $x^2 + y^2 6x + 4y 2 = 0$
- 19. Find the equation of the circle passing through the points of intersection of the circles  $x^2 + y^2 8x 6y + 21 = 0$ ,  $x^2 + y^2 2x 15 = 0$  and the point (1,2).
- 20. Find the equation of the circle passing through the origin and coaxial with the circles  $x^2 + y^2 6x + 4y 8 = 0$  and  $x^2 + y^2 2x + y + 4 = 0$ .
- 21. Find the pole of the line x + y + 2 = 0 with respect to the parabola  $y^2 + 4x 2y 3 = 0$ .

22. Evaluate 
$$\int \frac{3 \sin x + \cos x + 7}{\sin x + \cos x + 1} dx$$

23. Evaluate 
$$\int \frac{x^{1/4}}{x^{1/2} + 1} dx$$

24. Find the area enclosed by the curves y = 3x and  $y = 6x - x^2$ .

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## QUESTION PAPER PATTERN

Subject : **Mathematics** Paper : Paper –II B

Class : II Year Intermediate

(Coordinate Geometry, Calculus)

Time : 3 Hours

Max. Marks : 75

# 1. Weightage of Ojbectives :

| Objectives      | Knowledge | Understanding | Application | Total |
|-----------------|-----------|---------------|-------------|-------|
| Actual<br>Marks | 41        | 28            | 28          | 97    |

## 2. Weightage to form of Questions:

| Form of questions | VSA       | SA                | LA       | Total    |
|-------------------|-----------|-------------------|----------|----------|
|                   | Sec A     | Sec B             | Sec C    |          |
| No. of questions  | 10 of 10  | 5 of 7            | 5 of 7   | 20 of 24 |
| Marks allotted    | 10 x 2=20 | 5 x 4=20          | 5 x 7=35 | 75 / 97  |
|                   | 10 x 2=20 | $7 \times 4 = 28$ | 7 x 7=49 |          |

| 3. Weightage to content units / sub-units : | Marks    |
|---|----------|
| <b>Coordinate Geometry</b>                  |          |
| 1. Circles                                  | 16       |
| 2. System of Circles                        | 07       |
| 3. Parabola                                 | 09       |
| 4. Ellipse                                  | 06       |
| 5. Hyperbola                                | 06       |
| 6. Polar Coordiantes                        | 06       |
| <u>Calculus</u>                             |          |
| 7. Successive differentiation               | 06       |
| 8. Integration                              | 15       |
| 9. Definite Integration                     | 09       |
| 10. Numerical Integration                   | 09       |
| 11. Differential equations                  | 08       |
|   | Γotal 97 |
|   |          |