SCRA Exam: 2015

DO NOT OPEN THIS TEST BOOKLET UNTIL YOU ARE TOLD TO DO SO

T.B.C. : B-UETC-O-PDV TEST BOOKLET MATHEMATICS Paper – III

Time Allowed : Two Hours

Maximum Marks : 200

INSTRUCTIONS

- 1. IMMEDIATELY AFTER THE COMMENCEMENT OF THE EXAMINATION, YOU SHOULD CHECK THAT THIS TEST BOOKLET **DOES NOT** HAVE ANY UNPRINTED OR TORN OR MISSING PAGES OR ITEMS, ETC. IF SO, GET IT REPLACED BY A COMPLETE TEST BOOKLET.
- 2. Please note that it is the candidate's responsibility to encode and fill in the Roll Number and Test Booklet Series Code A, B, C or D carefully and without any omission or discrepancy at the appropriate places in the OMR Answer Sheet. Any omission/discrepancy will render the Answer Sheet liable for rejection.
- You have to enter your Roll Number on the Test Booklet in the Box provided alongside.
 DO NOT write anything else on the Test Booklet.
- 4. This Test Booklet contains 100 items (questions). Each item comprises four responses (answers). You will select the response which you want to mark on the Answer Sheet. In case you feel that there is more than one correct response, mark the response which you consider the best. In any case, choose **ONLY ONE** response for each item.
- 5. You have to mark all your responses **ONLY** on the separate Answer Sheet provided. See directions in the Answer Sheet.
- 6. All items carry equal marks.
- 7. Before you proceed to mark in the Answer Sheet the response to various items in the Test Booklet, you have to fill in some particulars in the Answer Sheet as per instructions sent to you with your Admission Certificate.
- 8. After you have completed filling in all your responses on the Answer Sheet and the examination has concluded, you should hand over to the Invigilator *only the Answer Sheet*. You are permitted to take away with you the Test Booklet.
- 9. Sheets for rough work are appended in the Test Booklet at the end.

10. Penalty for wrong answers :

THERE WILL BE PENALTY FOR WRONG ANSWERS MARKED BY A CANDIDATE IN THE OBJECTIVE TYPE QUESTION PAPERS.

- (i) There are four alternatives for the answer to every question. For each question for which a wrong answer has been given by the candidate, **one-third** of the marks assigned to that question will be deducted as penalty.
- (ii) If a candidate gives more than one answer, it will be treated as a **wrong answer** even if one of the given answers happens to be correct and there will be same penalty as above to that question.
- (iii) If a question is left blank, i.e., no answer is given by the candidate, there will be **no penalty** for that question.

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B-UETC-O-PDV

1. ²² Let S be any set and P(S) be its power set. We	5. A group of order 4 is
define a relation R on P(S) by ARB to mean	(a) always cyclic
$A \subseteq B$ for all A, $B \in P(S)$. Consider the	(b) always non-abelian
following in respect of the relation R :	
1. R is a reflexive relation.	(c) abelian and may not be cyclic
2. R is an anti-symmetric relation.	(d) always non-cyclic
3. R is a symmetric relation.	6. If a and b are rational and $(b^2 + 1)$ is not a
4. R is a transitive relation.	perfect square, then the quadratic equation
Which of the above are correct ?	with rational coefficients whose one root is $a(1, \sqrt{1-2})$.
(a) 1, 3 and 4	$\frac{a}{2}\left(b+\sqrt{1+b^2}\right)$ is
(b) 3 and 4 only	(a) $x^2 - 2abx - a^2 = 0$
(c) 1, 2 and 4	(b) $4x^2 - 4abx - a^2 = 0$
(d) 1 and 2 only	(c) $x^2 - abx - a^2 = 0$
	(d) $x^2 - abx + a^2 = 0$
2. What is the real part of $(\sin x + i \cos x)^5$, where $i = \sqrt{-1}$?	$(u) \mathbf{x} - ab\mathbf{x} + a = 0$
where $v = \sqrt{-1}$:	7. If $2 z-1 = z-2 $ and $3(x^2 + y^2) = kx$,
(a) $-\cos 5x$	then what is k equal to ?
(b) $-\sin 5x$	(a) 2/3
(c) $\cos 5x$	(b) 4/3
(d) sin 5x	(c) 4
3. If 5^{99} is divided by 13, then the remainder is	(d) 1
(a) 1	8. Let a_1, a_2, a_3, \dots be a sequence of real
(b) 5	numbers such that $ \mathbf{a}_i = \mathbf{a}_{i-1} + 1 $ for $i \ge 2$
(c) 8	and $a_1 = 0$. If A denotes the arithmetic mean
(d) 11	of $a_1, a_2, a_3, \dots, a_n$ then which one of the
	following is correct ?
4. The number of consecutive odd integers whose sum can be expressed as $50^2 - 13^2$ is	(a) $2nA = a_{n+1}^2 - n$
(a) 33	(b) $2nA = a_n^2 - n$
(b) 35	H .
(c) 37	(c) $2nA = a_{n+1}^2 - n - 1$
(d) 39	(d) $2nA = a_n^2 - n - 1$

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(2 – A)

9. If A is a non-singular matrix of order 3, then what is adj(adj A) equal to ?	13. If $ z - 25i \le 15$ where $i = \sqrt{-1}$, then what is $ \max amp(z) - \min amp(z) $ equal to ?
(a) $ \mathbf{A} ^3 \mathbf{A}$	(a) $\cos^{-1}\left(\frac{3}{5}\right)$
(b) $ A ^2 A$	
(c) A A	(b) $\pi - 2\cos^{-1}\left(\frac{3}{5}\right)$
(d) A	(c) $\frac{\pi}{2} + \cos^{-1}\left(\frac{3}{5}\right)$
10. If A, B and C are the angles of an isosceles	
triangle, then what is	(d) $\sin^{-1}\left(\frac{3}{5}\right) - \cos^{-1}\left(\frac{3}{5}\right)$
1 2 1	(5) (5)
$1+\sin A$ $2+\sin A+\sin B$ $1+\sin C$	
$\sin A(1+\sin A) \sin A(1+\sin A)+\sin B(1+\sin B) \sin C(1+\sin C)$	14. If the quadratic equation
equal to ?	$x^2 - 4px + 4p(p-1) = 0,$
(a) 0	where p is real, has its real roots greater than
(b) 1	p, then p lies in the interval
(c) $\sin A \cdot \sin B \cdot \sin C$	(a) $(4, \infty)$
(d) None of the above	(b) $(-\infty, -4)$
	(c) (-4, 0)
11. Let A and B be two 3×3 matrices whose	(u) (-4, -1)
determinants are 2 and 4 respectively. What $\frac{1}{2}$	5
is $det(adj(A^{-1}B))$ equal to?	15. What is the sum of the first 10 terms of the
(a) A	series $\frac{2}{3} + \frac{5}{3^2} + \frac{8}{3^3} + \dots$?
(b) B	$3 3^2 3^3$
(c) 4 A	
(d) 4 B	(a) $1 + \frac{3}{4} \left(1 - \frac{1}{3^9} \right) - \frac{29}{2 \times 3^{10}}$
12. Let S be the set $S = \{2, 4, 6, 8,, 20\}$. Define	
12. Let S be the set S = $\{2, 4, 6, 8,, 20\}$. Define the operation $p_{O_n}q$ as remainder when pq is	
divided by n. Then the inverse of the element	
2 in (S, ⊙ ₂₂) is	
(a) 12	(c) $1 + \frac{3}{4} \left(1 - \frac{1}{3^9} \right) - \frac{25}{2 \times 3^{10}}$
(b) 8	$4(3^{\circ}) 2 \times 3^{\circ}$
(c) 6	3(1) 29
(d) 4	(d) $1 + \frac{3}{4} \left(1 - \frac{1}{3^9} \right) - \frac{29}{3^{10}}$
	Δ Λ \
B-UETC-O-PDV (3	3 – A)

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16. A square matrix of third order is said to be 20. If the complex numbers z_1 , z_2 , z_3 are in AP, skew-symmetric if they lie on (a)All elements of leading diagonal are (a) a circle zero (b) $a_{ii} = a_{ii}$ (b) a line All elements of leading diagonal are 1 (c) a parabola (c) (d) $\mathbf{a}_{ii} = -\mathbf{a}_{ii}$ (d) an ellipse where a_{ii} being element in the ith row and jth 21. Which one of the following binary operations * column. is associative on the set of real numbers? 17. The equations (a) $a * b = a^b$ kx + y + z = k - 1, x + ky + z = k + 1, $\mathbf{a} \ast \mathbf{b} = \mathbf{a} + \mathbf{b} - \mathbf{1}$ (b) x + y + kz = k - 1 has no solution if (a) k = 1 only (c) b ≠ 0 a * b = (b) $k \neq -2$ (d) a * b = a - b(c) k = -2 or 1(d) k = -2 only 22. All the fourth roots of unity are What is the value of 18. (a) 1, 1, -1, -1 $\left(\frac{i+\sqrt{3}}{-i+\sqrt{3}}\right)^{52722} + \left(\frac{i-\sqrt{3}}{i+\sqrt{3}}\right)^{52722}$ (b) i, i, -i, -i(c) 1, -1, i, -iwhere $i = \sqrt{-1}$? (d) -i, -i, -i, -iwhere $i = \sqrt{-1}$. (a) $\sqrt{2}$ $\sqrt{3}$ (b) Consider the following in respect of the 23. equation $(x + 2)^2 - 3 |x + 2| + 2 = 0$: (c) 2 The sum of all possible roots of the (d) 1. equation is -8. 19. The function 2. The product of all possible roots of the $\mathbf{f}(\mathbf{x}) = \mathbf{a}_0 + \mathbf{a}_1 \|\mathbf{x}\| + \mathbf{a}_2 \|\mathbf{x}\|^2 + \mathbf{a}_3 \|\mathbf{x}\|^3$ equation is 0. is differentiable at x = 0Which of the above statements is/are correct? only when $a_1 = 0$ (a) (a) 1 only only when $a_1 = a_3 = 0$ (b) (b) 2 only (c). only when $a_1 = a_2 = a_3 = 0$ (c) Both 1 and 2 (d) Neither 1 nor 2 (d) for any values of a_0 , a_1 , a_2 and a_3 (4-<u>A</u>). **B-UETC-O-PDV**

2 4.	Three straight lines l_1, l_2, l_3 are parallel and	27.	Consider the following statements :
	lie on the same plane. 5 points are taken on line l_1 , 6 points are taken on line l_2 and	· .	1. $\sin 75^\circ + \cos 105^\circ \neq \cos \theta$ for any θ , where $0 < \theta < 60^\circ$.
·, *	7 points are taken on line l_3 . What is the maximum number of triangles formed with vertices at these points?	•	2. $\sin \theta + \cos \theta < 1$ for all θ , where 90° < θ < 120°.
			Which of the above statements is/are correct?
• •	(a) 620 (b) 746	•	(a) 1 only
•	(c) 751		(b) 2 only
			(c) Both 1 and 2
	(d) 781		(d) Neither 1 nor 2
25.	Consider the following statements in respect		34 66
	of the expansion $\frac{(1+x)^{2n}}{x^n}$:	28.	Let T = { $\theta \in \mathbf{R}$: 30 is not of the form $k\pi$ for any
	x ⁿ		$\mathbf{k} \in \mathbf{Z} \} \cap [0, 2\pi].$
	1. Independent term does not exist in the	. 1	Consider the following statements :
•	expansion.		Statement-I :
.•	2. The coefficient of x is equal to coefficient of x^{-1} in the expansion.	4	There exists at least one $x \in \mathbb{R} \setminus (-1, 1)$ for which there exists no $t \in T$ such that
	Which of the above statements is/are correct ?	1	$\frac{1+2\cos 2t}{\sin 3t} = x.$
	(a) 1 only		Statement-II : For any $\theta \in T$, $\frac{1+2\cos 2\theta}{\sin 3\theta} = \csc \theta$.
	(b) 2 only		
	(c) Both 1 and 2		Which one of the following is correct in respect of the above statements ?
	(d) Neither 1 nor 2		(a) Both the statements are true and statement-II is the correct explanation of statement-I.
26.	If $A \in (0, 2\pi) - \{\pi\}$, how many solutions of A		(b) Both the statements are true but
	$\cot \frac{A}{2} - \tan \frac{A}{2} = 2 \text{ are possible }?$		statement-II is not the correct explanation of statement-I.
	(a) Only one(b) Two		(c) Statement-I is true, but statement-II is false.
	(c) Four		(d) Statement-I is false, but statement-II is
	(d) No solution is possible		true.
R-LI		– A)	· ·

29.

Consider the following statements :

Statement-I:

There exists no triangle ABC satisfying $\frac{\cos A}{a} = \frac{\cos B}{b} = \frac{\cos C}{c} = \frac{1}{2R}$, where R is the circum-radius of the triangle ABC.

Statement-II :

If ABC is an isosceles triangle satisfying

$$b^{2} = c^{2} + a^{2}$$
, then $\frac{a}{\cos A} = \frac{c}{\cos C} = b$.

Which one of the following is correct in respect of the above statements ?

- (a) Both the statements are true and statement-II is the correct explanation of statement-I.
- (b) Both the statements are true but statement-II is not the correct explanation of statement-I.
- (c) Statement-I is true, but statement-II is false.
- (d) Statement-I is false, but statement-II is true.
- **30.** Let ABC be a triangle with $\angle B = 60^{\circ}$. Statement-I:

If $a = b \sin C + c \sin B$, then $\angle C \neq 45^{\circ}$. Statement-II:

$$b^2 (1 - \sin 2C) = c^2 \left(\frac{2 - \sqrt{3}}{2}\right)$$

Which one of the following is correct in respect of the above statements ?

- (a) Both the statements are true and statement-II is the correct explanation of statement-I.
- (b) Both the statements are true but statement-II is not the correct explanation of statement-I.
- (c) Statement-I is true, but statement-II is false.
- (d) Statement-I is false, but statement-II is true.

31. It is given that $(\sin^{-1} x) \cos^{-1} \left(-\frac{\sqrt{3}}{2} \right) = \frac{5\pi^2}{36}$.

Which one of the following is *not* correct?

(a)
$$\sin^{-1} x - \cos^{-1} \left(\frac{1}{2}\right) \neq 0$$

(b)
$$\sin^{-1} x + \cos^{-1} \left(\frac{\sqrt{3}}{2}\right) = \frac{\pi}{3}$$

(c) $\sin^{-1} x = \frac{1}{5} \cos^{-1} \left(-\frac{\sqrt{3}}{2}\right)$

(d)
$$(\sin^{-1} x)^2 = \frac{1}{9} \left[\cos^{-1} \left(\frac{1}{2} \right) \right]^2$$

Consider the following statements :

- 1. If α , β are supplementary angles and $\cot(\alpha \beta) = 1$, then $\tan 2\alpha = \cot 2\alpha$.
- 2. If α , β are complementary angles and $\tan (\alpha \beta) = 1$, then sec $2\beta = \operatorname{cosec} 2\beta$.

Which of the above statements is/are correct?

(a) 1 only

32.

- (b) 2 only
- (c) Both 1 and 2
- (d) Neither 1 nor 2

33. Consider the following statements :

- 1. If α , β are acute angles and tan $(\alpha + \beta) = 1$ and $\sqrt{3} \sec (\alpha - \beta) = 2$, then tan $2\alpha = \cot 15^{\circ}$.
- 2. If α , β are the angles in the second quadrant and $\csc (\alpha - \beta) = -\sec (\alpha + \beta) = 2$, then $\sin \beta = \cos 15^{\circ}$.

Which of the above statements is/are correct?

- (a) 1 only
- (b) 2 only
- (c) Both 1 and 2
- (d) Neither 1 nor 2

B-UETC-O-PDV

34.	What is the maximum value of	38.	If the function $f(x) = \sin x + \cos (xa)$ is periodic, then 'a' is
	$5\cos\theta + 3\cos\left(\theta + \frac{\pi}{3}\right) + 3$?		(a) always a natural number
	$3\cos(0+3\cos(0+\frac{3}{3})+3)$		(b) always an integer
	(a) 11		(c) an irrational number
•	(b) 10		(d) a rational number
•	(c) 5		1.6
	(d) 1	39.	At how many points do $y = x$ and $y = \tan x$ intersect?
35.	Consider the following statements :		(a) Zero
			(b) Only one
	1. If $\theta = -\frac{17\pi}{4}$, then $\sin^8 \theta = \frac{1}{8}$.		(c) Two
	4 O	· ·	(d) Infinite
	2. If $\theta = \frac{231\pi}{6}$, then $\sin^6 3\theta = 1$.	40.	ABCDEFG is a 7-sided polygon which is not regular. If its angles are in AP, then which
,	Which of the above statements is/are correct ?	·	one of the following is correct?
	(a) 1 only		(a) Exactly three of its angles are greater
	(b) 2 only	1.	than 125°.
	(c) Both 1 and 2	- 1	(b) Exactly four of its angles are greater
	(d) Neither 1 nor 2	• 11	than or equal to the angle of a regular polygon of 7-sides.
36.	For how many distinct values of A between 0°		(c) Exactly three of its angles are less than
•	and 360° is the expression	-	or equal to $\frac{5\pi}{7}$ radian.
	$\frac{\sin A + \sin 2A + \sin 3A}{\cos 2A}$ undefined ?		or equal to $\frac{1}{7}$ fatial.
	$\frac{1}{\cos A + \cos 2A + \cos 3A}$ undefined ?		(d) The sum of the greatest angle and the
	-	·	least angle is greater than $\frac{10\pi}{7}$ radian.
	(a) 2		7
	(b) 4		If $y = y(t)$, $y = y(t)$, then what is $\frac{d^2y}{dt}$ equal
,	(c) 6	41.	If $x = \varphi(t)$, $y = \psi(t)$, then what is $\frac{d^2 y}{dx^2}$ equal to?
	(d) 8		····
			(a) $\frac{\phi'\psi''-\psi'\phi''}{(\cdot)^2}$
37.	In a triangle ABC if $\cot \frac{A}{2}$, $\tan \frac{B}{2}$, $\cot \frac{C}{2}$ are		(φ') ²
	in HP, then what is the value of		$\phi'\psi''-\psi'\phi''$
			(b) $\frac{\psi \psi}{(\phi')^3}$
	$\tan \frac{A}{2} \tan \frac{C}{2}$?	•	
	2 2		(c) $\frac{\phi''}{\mu}$
•	(a) -1	[`]	Ψ
	(b) $\frac{1}{2}$		(d) $\frac{\varphi'\psi''+\psi'\varphi''}{(\varphi')^2}$
	(c) 1	·	(*)
		·]·	where dashes denote the derivative with
	(d) 2	·	respect to t.
	· · · ·		
B-U	IETC-O-PDV (7	– A)	

- 42. Let $f(x) = \sin x$, $g(x) = x^2$ and h(x) = ln x be functions of real variable x > 0. Suppose fog(x) means f[g(x)]. If F(x) = [(hog)of](x), what is F''(x) equal to ?
 - (a) $2 \operatorname{cosec}^2 x$
 - (b) $2 \sec^2 x$
 - (c) $-2 \operatorname{cosec}^2 x$
 - (d) None of the above

43. If $f(x) = a \ln |x| + bx^2 + x$ has its extreme values at x = -1 and x = 2, then what is the value of 'a'?

- (a) 1
- (b) 2
- (c) 1
- $(d) \quad -2$

44. If $g(x) = x^3$ and $3f(x) = 4x^3 - 12x$ where $0 \le x \le 2$, then g[f(x)] will attain its greatest value at

- (a) x = 2
- (b) x = 0
- (c) x = 1
- (d) $x = \frac{1}{3}$

B-UETC-O-PDV

45. If $5y = -3[x] + 4[\tan x] + 3|y|$ where [.] is the greatest integer function, then y as a function of x is

(a) not continuous at x = 0

(b) continuous at x = 0

- (c) differentiable at x = 0
- (d) continuous at x = 0 but not differentiable at x = 0

If $f(x) = \frac{x^3 \sqrt{1+x^2}}{2-x}$, $0 \le x \le 1$ and $f(x) = \frac{x^3 \sqrt{1+x^2}}{2+x}$, $-1 \le x \le 0$, then what is $\frac{1}{2} \int_{0}^{1} f(x) dx$ equal to ?

 $-\frac{1}{2}$ (a) 4

46.

(b)

(c)

(d)

1

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47. Let F(x) be a twice differentiable function with F''(x) = -F(x) and F'(x) = G(x). If $H(x) = {F(x)}^2 + {G(x)}^2$ and H(5) = 5, then what is H(0) equal to ?

(a) 0
(b) 5
(c) 9
(d) 10

(a)

(b)

(c)

(d)

-5

 $\frac{1}{5}$

48. If f(a) = 2, f'(a) = 1, g(a) = -1, g'(a) = 2, then what is $\lim_{x \to a} \left[\frac{g(x)f(a) - g(a)f(x)}{x - a} \right]$ equal to ?

(8-A)

	•		
. 49	The function $f(x) = e^x (1 - x^2)$ is	52. If f(x) is a second order polynomial (or quadratic expression in x) and	! ! .'
	(a) increasing for $x > \sqrt{2}$	b	•
	(b) decreasing for $x < \sqrt{2}$	$\int_{a}^{b} f(x) dx = (a - b) (a^{2} + b^{2} + ab + 2),$	
s .	(c) increasing for $ x-1 < \sqrt{2}$	then f(x) will be of the form	
	(d) increasing for $ x + 1 < \sqrt{2}$	(a) $3x^2 + x + 2$	
		(b) $2x^2 - x$	
		(c) $-3x^2-2$	
.50		(d) $3x^2 + 2$	
	defined by $f(x) = sin\left(\frac{x}{3}\right)$. The function f is	36 66	
		Nº 1 1	
	(a) one-one	$\pi/2$ $\pi/2$	· ··
	(b) onto	53. If $I_1 = \int_{0}^{1} \cos(\sin x) dx$, $I_2 = \int_{0}^{1} \sin(\cos x) dx$.	۱ ب
:	(c) both one-one and onto	$\pi/2$	
	(d) neither one-one nor onto	and $I_3 = \int \cos x dx$, then which one of the	
		0 following is correct ?	
		(a) $I_1 > I_2 > I_3$	
•• .	$\sqrt{\pi}$		
51	What is $\int x e^{x^2} \sin(x^2) dx$ equal to?	(b) $I_3 > I_2 > I_1$	
÷ .	0	(c) $I_3 > I_1 > I_2$	
	(a) $\frac{e^{\pi}+1}{2}$	(d) $I_1 > I_3 > I_2$	
· ·· .	2		
· · ·	(b) $\frac{e^{\pi}-1}{2}$	54. If $a > 1$, $b > 1$ then the minimum value of	
·	4	$\log_a b + \log_b a$ is	
	(c) $\frac{e^{\pi}+1}{2}$	(a) 0 ,	
	4	(b) 2	
	(d) $e^{\pi} + 1$	(c) 1 (d) Noise of the observe $\frac{1}{2}$	
		(d) None of the above	
B	UETC-O-PDV (9	9 – A)	

55. If
$$y = \sin^{-1}\left(\frac{2x}{1+x^2}\right)$$
, then which of the
following is/are correct?
1. $\frac{dy}{dx} = \frac{2}{1+x^2}$ for $-1 < x < 1$
2. $\frac{dy}{dx} = -\frac{2}{1+x^2}$ for $x < -1$

3.
$$\frac{dy}{dx} = -\frac{2}{1+x^2}$$
 for $x > 1$

Select the correct answer using the code given below :

- (a) 1 only
- (b) 1 and 2 only
- (c) 2 and 3 only
- (d) 1, 2 and 3

56. The equation of the curve passing through the point (0, 1) and having x³y⁻³ as the slope of the tangent to the curve at any point (x, y) is

- (a) $x^4 y^4 + 1 = 0$
- (b) $x^4 + y^4 1 = 0$
- (c) $x^3 + y^3 1 = 0$
- (d) $x^3 y^3 + 1 = 0$

57. If I_1 is the integrating factor of the differential equation $x \frac{dy}{dx} - y = x^2$ and I_2 is the integrating factor of the differential equation $x \frac{dy}{dx} + y = x^{-2}$, then which one of the following is **not** correct?

- (a) $I_1 I_2 = 1$ (b) $I_2 = x^2 I_1$
- (c) $I_1 = x^2 I_2$
- (d) $I_2 > I_1 \text{ for } x > 1$

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(10 - A)

58. Consider the following differential equations :

1.
$$(x - y) \frac{dy}{dx} = 2x + y$$

2. $x \cos\left(\frac{y}{x}\right) \frac{dy}{dx} = y \cos\left(\frac{y}{x}\right) + 4x$
3. $2x^2 y^2 \frac{dy}{dx} = x^2 + y^2$
4. $\sin x \frac{dy}{dx} = \cos x$

How many of the above are homogeneous?

(a) One(b) Two(c) Three

Four

(d)

59.

- If $f(x) = \frac{1-x}{1+x}$ where x > 0 and $x \neq 1$, then
- $\mathbf{f}[\mathbf{f}(\mathbf{x})] + \mathbf{f}\left[\mathbf{f}\left(\frac{1}{\mathbf{x}}\right)\right]$ is
- (a) less than 2
- (b) greater than 2
- (c) greater than or equal to 2
- (d) equal to 2

60. What is $\int_{1}^{3} \frac{[x^{2}] dx}{[x^{2} - 8x + 16] + [x^{2}]}$, where [.] denotes the greatest integer function, equal to? (a) 4 (b) 3

(c) 2

1

(d)

61. If $\int \frac{g''(x) g(x) dx}{\{g'(x)\}^2} = x + \text{constant}$, then the function $g(x)$ will be of the form	65. Consider the following statements : 1. The function attains local minimum 7
(a) $ax^2 + b$ (b) $a e^{bx^2}$ (c) $a e^{-bx}$ (d) $a e^{bx}$ where a and b are non-zero constants. 62. What is the area bounded by the curves $y = ln x$ and $y = (ln x)^2$? (a) $e - 1$	value at $x = \frac{7}{5}$. 2. $x = 2$ is the point of inflexion. Which of the above statements is/are correct? (a) 1 only (b) 2 only (c) Both 1 and 2 (d) Neither 1 nor 2
(a) e^{-1} (b) e^{-2} (c) $3-e$ (d) e	For the next two (02) items that follow: Consider $f(x) = -1 + x - 1 , -1 \le x \le 3$ and $g(x) = 2 - x + 1 , -2 \le x \le 2.$
For the next three (03) items that follow: Consider the function $f(x) = \int_{1}^{x} \{2(t-1)(t-2)^3 + 3(t-1)^2(t-2)^2\} dt.$	66. For $x \in (0, 1)$, fog(x) is equal to (a) $x - 1$ (b) $1 - x$ (c) $x + 1$ (d) $-x - 1$
 63. The function attains local maximum at (a) x = 0 (b) x = 1 (c) x = 2 (d) x = 4 64. What is the local maximum value of the function ? (a) 0 	 67. Consider the following statements : 1. For x ∈ (-1, 1), fof(x) = x. 2. For x ∈ (-1, 2), gog(x) = x. Which of the above statements is/are correct ?
(b) 1 (c) 4 (d) 16 B-UETC-O-PDV (11	(c) Both 1 and 2 (d) Neither 1 nor 2

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報告において

e.

For the next three (03) items that follow	
Let $f: \mathbb{R} \to \mathbb{R}$ be defined by	the graph of $ \mathbf{x} + \mathbf{y} < 3$?
$f(x) = \frac{3x^2}{2} + x^2 \sin\left(\frac{1}{x}\right) \text{ for } x \neq 0 \text{ and } f(0)$	= 0. (a) 13 (b) 15 (c) 21 (d) 24
68. The function $f(x)$ is	
(a) continuous and differentiable at	June June (1, 1)
(b) nowhere continuous over \mathbf{R}	and $(-2, 3)$ measured parallel to the line $x + y + 1 = 0$ is
(c) continuous at $x = 0$, but not differentiable at $x = 0$	(a) 4 units
(d) nowhere differentiable over R	(b) $4\sqrt{2}$ units
	(c) 6 units
60 (1)	(d) $6\sqrt{2}$ units .
69. The function f(x) has(a) local maximum at x = 0	73. A double ordinate of the parabola $y^2 = 4ax$ is of length 8a. What is the angle between the
(b) local minimum at $x = 0$ but it absolute minimum	has no lines from the vertex to its ends? (a) 30°
(c) absolute minimum at $x = 0$	(b) 45°
(d) absolute maximum at $x = 0$	(c) 60° (d) 90°
70. Let $x_1 = \frac{1}{2n\pi}$ and $x_2 = \frac{2}{(4n+1)\pi}$ where	74.For how many values of k, the line $3x - 4y = k$ may touch the circle $x^2 + y^2 - 4x - 8y - 5 = 0$?(a) 1(b) 2
The derivative of the function f(x) attai	ne
(a) positive value at x_1 and negative	e value (c) 3 (d) None of the values of k
at x ₂	(d) None of the values of K
(b) positive value at x_1 and positive	e value 75. What is one of the angles between the straight lines
at x ₂	$(\mathbf{x}\cos\alpha - \mathbf{y}\sin\alpha)^2 = (\mathbf{x}^2 + \mathbf{y}^2)\sin^2\alpha?$
(c) negative value at x_1 and positiv	e value (a) α
$\operatorname{at} \mathbf{x}_2$	(b) 2α
(d) negative value at x_1 and negative value at x_2 and negative value at x_2	e value (c) 4α
at x ₂	(d) $\alpha/2$
B-UETC-O-PDV	(12 – A)

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- 76. A straight line passes through a fixed point 80.(h, g). The locus of the foot of the perpendicular on it drawn from the origin is
 - (a) a straight line
 - (b) an ellipse
 - (c) a parabola
 - (d) a circle
- 77. If the three distinct points $(t_i, 2at_i + at_i^3)$ for i = 1, 2, 3 are collinear, then the sum of the abscissa of the points is
 - (a) –1
 - (b) 0
 - (c) 1
 - (d) 3
- 78. Let (a, b) and (c, d) be two points in a plane. Any point on the line joining these points has coordinates
 - (a) $(a + kc, b + kd)^{-1}$
 - (b) (ka + c, kb + d)
 - (c) ((1-k)a + kc, (1-k)b + kd)
 - (d) (a + (1 k) c, b + (1 k) d)

where k is any real number.

79. The equation

$$|\vec{r}|^2 + \vec{r} \cdot (2\hat{i} + 4\hat{j} - 2\hat{k}) - 10 = 0$$

represents a sphere of radius

- (a) 2 units
- (b) 3 units
- (c) 4 units
- (d) 5 units

What is $\int \frac{(ax+b) dx}{|ax+b|}$, where $a \neq 0$, $x \neq -\frac{b}{a}$, equal to?

- (a) $\frac{(ax+b)}{a} + c$ (b) (ax+b) + c(c) |x| + c
- (d) None of the above

where c is the constant of integration.

For the next three (03) items that follow :

Consider a point A(-2, 3, 0) above the line PQ. The line PQ passes through P(-3, 5, 2) and makes equal angles with the coordinate axes.

- 81. What are the coordinates of the foot of the perpendicular from A on the line PQ?
 - (a) (-4, 4, 1)
 - (b) (4, 4, 1)
 - (c) (-2, 2, 1)
 - (d) (2, 2, 1)
- 82. What are the direction ratios of the line perpendicular to the line PQ?
 - (a) < 2, 1, −1 >
 - (b) <-2, 1, 1 >
 - (c) < 4, 1, 1 >
 - (d) < 1, 1, 1 >

B-UETC-O-PDV

(13 – A)

			:
83. V d	Vhat is the square of the perpendicular stance of the point A from the line PQ?	86.	If ABCDEF is
(4	a) 4		$\overrightarrow{AB} = \overrightarrow{a}$ and \overrightarrow{BC}
0	p) 5		equal to ?
(0	c) 6		(a) $\overrightarrow{b} - \overrightarrow{a}$
(0	i) 9		(a) D - a
			(b) $\vec{b} - 2\vec{a}$
For the	e next two (02) items that follow :		
A vari	able plane $\frac{x}{3a} + \frac{y}{3b} + \frac{z}{3c} = 1$ at unit		(c) $2\overrightarrow{b} - \overrightarrow{a}$
distanc	e from the origin cuts the coordinate axes at	1	4 CI
A, B an	d C respectively. The centroid of the triangle	6	(d) $\vec{b} + \vec{a}$
ABC sa	tisfies the equation $\frac{1}{x^2} + \frac{1}{y^2} + \frac{1}{z^2} = k^2$.		V
84. T	he centroid of the triangle is at 8	7.	If (0, 1) and (1, 0) a
	4.1		of a right-angled t
(a	$) \left(\frac{a}{3}, \frac{b}{3}, \frac{c}{3}\right)$		following statement
(b) (a, b, c)		
(c)) (3a, 3b, 3c)		1. (0, 0) can be
	24.2		triangle.
(a	$\left(\frac{a}{2}, \frac{b}{2}, \frac{c}{2}\right)$		2. (1, 1) can be
26			triangle.
6	1		
85. Th	e value of k is		Which of the above s
: (a)	$\frac{1}{9}$. (a) 1 only
		(h) 9 and -
. (b)	$\frac{1}{3}$		b) 2 only
(-)		. (c) Either 1 or 2
(c)	3	(d) Neither 1 nor 2
(d)	9		· · · · · · · · · · · · · · · · · · ·
B-UETC-	O-PDV (14 – A)	

If ABCDEF is a regular hexagon with 86. $\overrightarrow{C} = \overrightarrow{b}$, then what is \overrightarrow{CE}

- are mid-points of the sides triangle, then consider the ts:
 - be the orthocentre of the
 - be the orthocentre of the

statements is/are correct?

For the next three (03) items that follow: The vectors $\vec{b} = (\tan \alpha)\hat{i} - \hat{j} + 2\sqrt{\sin\left(\frac{\alpha}{2}\right)}\hat{k}$ and $\vec{c} = (\tan \alpha)\hat{i} + (\tan \alpha)\hat{j} - 3\sqrt{\csc\left(\frac{\alpha}{2}\right)}\hat{k}$ are orthogonal and a vector $\vec{a} = \hat{i} + 3\hat{j} + (\sin 2\alpha)\hat{k}$	 91. The numbers 1, 2, 3, 4, 5, 6, 7, 8 are arranged in a random order. The probability that the digits 1, 2, 3, 4 appear as neighbours in that order is (a) 1/2 (b) 1/128
makes an obtuse angle with z-axis.	(c) $\frac{1}{256}$ (d) $\frac{1}{336}$
 88. What is/are the permissible value(s) of tan α? (a) -2 only (b) 3 only (c) Both -2 and 3 (d) Neither -2 nor 3 	92. The average marks of 10 students in a class was 60 with a standard deviation 4, while the average marks of other 10 students was 40 with a standard deviation 6. If all the 20 students are taken together, their standard deviation will be
89. In which quadrant does α lie? (a) First quadrant (b) Second quadrant (c) Third quadrant (d) Fourth quadrant 90. What is α equal to? (a) $(4n + 1)\pi \pm \tan^{-1} 2$ (b) $(4n + 2)\pi \pm \tan^{-1} 2$ (c) $(4n + 1)\pi - \tan^{-1} 2$; $(4n + 2)\pi - \tan^{-1} 2$ (d) None of the above	(a) $5 \cdot 0$ (b) $7 \cdot 5$ (c) $9 \cdot 8$ (d) $11 \cdot 2$ 93. The two lines of regression of y on x and x on y are $5y + 4x = 37$ and $y + 5x = 20$ respectively. The correlation between x and y will be (a) $\frac{2}{5}$ (b) $\frac{-2}{5}$ (c) $\frac{1}{5}$ (d) $\frac{-1}{5}$
where n is an integer. B-UETC-O-PDV (1	5 – A ⁻)

- 94. Correlation between two variables X and Y is given to be 0.6. These variables are transformed to new variables u = -2X + 3 and v = 5Y - 2. What will be the correlation between u and v?
 - (a) 0.6
 - (b) -0.6
 - (c) 0.2
 - (d) Information is insufficient

95. If A and B are any two events with P(A) = 0.6, P(B) = 0.3 and $P(A \cap B) = 0.2$, what will be $P(A^c | B^c)$, where A^c is the complementary event of A?

- (a) 3/7
- (b) 4/7
- (c) 1/3
- (d) 2/3

96. A point is chosen at random inside a rectangle measuring 5 inches by 6 inches. What is the probability that the point chosen at random inside the rectangle is at least one inch from the edge ?

- (a) 5/6
- (b) 4/5
- (c) 3/4
- (d) 2/5

97.

A box contains three types of seeds : 50% of type A; 20% of type B and rest of type C. It is known that 20% of A, 30% of B and 30% of C germinate. A seed is drawn randomly from the box. What is its probability to germinate?

- (a) 0·25
- (b) 0.50
- (c) 0.80
- (d) 1

B-UETC-O-PDV

A box contains a fair coin and a two-headed coin B. A coin is selected at random from the box and tossed twice. If head comes both the times, the probability that it is by the two-headed coin is

(a) 1/4

98.

(b) **1/2**

(c) 4/5

(d) 5/8

Some urns contain 4 white and 6 black balls, while one urn contains 5 white and 5 black balls. One urn is chosen at random from these and 2 balls are drawn from it, and both are found to be black. The probability that 5 white and 3 black balls remain in the chosen urn is 1/7. The total number of urns is

- (a) 4
 (b) 5
 (c) 6
 (d) 7
- 100. n observations on a variable X are $X_i = A + iB$ for i = 1, 2, 3, ..., n where A, B are real constants. The mean of the observations is
 - (a) $A + B\left(\frac{n+1}{2}\right)$ (b) $nA + B\left(\frac{n+1}{2}\right)$ (c) $A + Bn\left(\frac{n+1}{2}\right)$ (d) $A + B\left(\frac{n}{2}\right)$
- (16 A)

B-UETC-O-PDV

(17-A)

1

(19⁻-A)

B-UETC-O-PDV

B-UETC-O-PDV

(20 – A)