PART-A MATHEMATICS

Solutions of SET-D5

Note: Questions with (*) mark are from syllabus of class XL

*1.	The mean of the numbers a , b , b , b , c , 10 is 6 and the variance is $6 \cdot 80$. Then which one of the following gives possible values of a and b^2 .						
	(1) $a=1, b=6$	(2) $a = 3, b = 4$	(3) <i>a</i> = 0, <i>b</i> = 7	(4) $a = 5, b = 2$			
Sol:	Variance is $\frac{\sum x^2}{n} - \left(\frac{\sum x}{n}\right)^2 = 6.$	8 and $\left(\frac{\sum x}{n}\right) = 6$ (given)					
	$\Rightarrow \frac{a^2 + b^2 + 64 + 25 + 100}{5} - 36$	$=6.8 \implies a^2 + b^2 + 9 = 34.0$	$\Rightarrow a^2 + b^2 = 25$				
	Correct c hoice: (2)						
2.	The vector $\vec{a} = \alpha \hat{i} + 2\hat{j} + \beta \hat{k}$ lies \vec{c} . Then which one of the follow	s in the plane of the vectors $\vec{b} =$ ing gives possible values of α and	$\hat{i} + \hat{j}$ and $\hat{c} = \hat{j} + \hat{k}$ and bisect d β ?	s the angle between \dot{b} and			
	(1) $\alpha = 2, \beta = 1$	(2) $\alpha = 1, \beta = 1$	(3) $\alpha = 2, \beta = 2$	(4) $\alpha = 1$, $\beta = 2$			
Sol:	$\because \vec{a}, \vec{b}$ and \vec{c} are coplanar.	$\Rightarrow [\vec{a} \ \vec{b} \ \vec{c}] = 0 \Rightarrow \alpha + \beta$	=2	•.(i)			
	Also \ddot{a} bisects the angle between	$a \ \vec{b} \ \text{and} \ \vec{c} \ , \ \Rightarrow \ \vec{a} = \lambda \left(\hat{b} + \hat{c} \right)$	$\Rightarrow \bar{a} = \lambda \left(\frac{\hat{i} + 2\hat{j} + \hat{k}}{12} \right)$	(ii)			
	Comparing (ii) with $\vec{a} = \alpha \hat{i} + 2\hat{j}$	$+\beta \hat{k}$, we get $\lambda = \sqrt{2}$, $\therefore \alpha = 1$	and $\beta = 1$, which also satisfies (i).			
	Correct choice: (2)		SO .				
3.	The non-zero vectors \tilde{a} , \tilde{b} and \tilde{c}	are related by $\vec{a} = 8\vec{b}$ and $\vec{c} = -$	-7 b . Then the angle between a	and č is			
	(1) $\frac{\pi}{2}$	(2) π	(3) 0	(4) $\frac{\pi}{4}$			
Sol:	Clearly \dot{a} and \dot{c} are anti paralle	1.					
	\therefore Angle between \dot{a} and \dot{c} is π						
+4	Correct choice: (2)		(o 17	-13)			
~4.	The line passing through the poir	is $(0, 1, a)$ and $(0, b, 1)$ crosses	the juz-plane at the point $\left(0, \frac{1}{2}\right)$	$\left(\frac{1}{2}\right)$. Then			
	(1) $a = 6, b = 4$	(2) $a = 3, b = 2$	(3) $a = 2, b = 8$	(4) $a = 4, b = 6$			
Sol:	Equation of given line in symmet	ric form is $\frac{x-3}{-2} = \frac{y-1}{b-1} = \frac{z-a}{1-a}$	= λ(i)				
	$\therefore \text{ Any point on (i) can be } (5-2\lambda, 1+(b-1)\lambda, a+\lambda(1-a)) \qquad \dots (ii)$						
	$\because \left(0, \frac{17}{2}, -\frac{13}{2}\right)$ lies on (i) \Rightarrow	$\lambda = \frac{5}{2}$	(iii)				
	Using (iii) in (ii) and comparing with given point we get $a = 6$, $b = 4$						
	Correct choice: (1)						
5.	If the straight lines $\frac{x-1}{k} = \frac{y-2}{2}$	$=\frac{z-3}{3}$ and $\frac{x-2}{3}=\frac{y-3}{k}=\frac{z-3}{2}$	$\frac{1}{2}$ intersect at a point, then the in	teger k is equal to			
6.1.	(1) 2 	(2) -2	(3) –5	(4) 5			
50L:	iwo given lines are intersection in the section of the section	ng.					
	$\therefore \begin{vmatrix} 1 & 1 & -2 \\ k & 2 & 3 \\ 3 & k & 2 \end{vmatrix} = 0 \implies k = -1$	5 is the required integral value .					

Correct choice: (3)

ó. The differential equation of the family of circles with fixed radius 5 units and centre on the line y = 2 is (1) $(y-2)^2 y'^2 = 25 - (y-2)^2$ (2) $(x-2)^2 y'^2 = 25 - (y-2)^2$ (3) $(x-2)y'^2 = 25 - (y-2)^2$ (4) $(y-2)y'^2 = 25 - (y-2)^2$ **Sol:** Equation of circle can be $(x-a)^2 + (y-2)^2 = 25$(i) $\Rightarrow a = x + (y - 2)y'$...(ii) Using (ii) in (i), we get $(v-2)^2 v'^2 = 25 - (v-2)^2$ Correct choice: (1) 7. Let a, b, c be any real numbers. Suppose that there are real numbers x, y, z not all zero such that x = cy + bz, y = cz + bz, and z = bx + ay. Then $a^2 + b^2 + c^2 + 2abc$ is equal to (1) 0 **Sol:** According to given condition $\begin{vmatrix} 1 & -c & -b \\ c & -1 & a \\ b & a & -1 \end{vmatrix} = 0 \implies a^2 + b^2 + c^2 + 2abc = 1$ Correct choice: (2) Let A be a square matrix all of whose entries are integers. Then which one of the following is true? 8. (1) If det $A = \pm 1$, then A^{-1} exists and all its entries are integers (2) If det $A = \pm 1$, then A^{-1} need not exist (3) If det $A = \pm 1$, then A^{-1} exists but all its entries are not necessarily integer (4) If det $A \neq \pm 1$, then A^{-1} exists and all its entries are non-integers Sol: Obviously(1) is the correct answer. Correct choice: (1) The quadratic equations $x^2 - 6x + a = 0$ and $x^2 - cx + 6 = 0$ have one root in common. The other roots of the first and *9. second equations are integers in the ratio 4 : 3. Then the common root is (1)3(2)2(4) 4(3)1**Sol:** Let the roots of $x^2 - 6x + a = 0$ be $\alpha_1 4\beta$ and the roots of $x^2 - cx + 6 = 0$ be $\alpha_1 3\beta$ $\therefore \alpha + 4\beta = 6$ $4\alpha\beta = a$ $\alpha + 3\beta = c$ and $3\alpha\beta = 6$ (ii) and (iv) 🔿 \therefore 1st equation reduces to $x^2 - 6x + 8 = 0$ Clearly $\alpha = 2$ and $\beta = 1$ Common root is 2. Correct choice: (2) How many different words can be formed by jumbling the letters in the word MISSISSIPPI in which no two S are adjacent? (1) 6.8.⁷C₄ (2) $7.{}^{6}C_{4}.{}^{8}C_{4}$ (3) 8. ${}^{6}C_{4}$. ${}^{7}C_{4}$ (4) 6.7.⁸C₄ Sol: 1M, 4I's and 2P's can be arranged by $\frac{7!}{4!2!}$ and in the 8 gaps 4 S can arranged with ${}^{8}C_{4}$ ways, so total ways are $7.6C_{4}.8C_{4}$ Correct choice: (2)

11. Let
$$I = \int_{0}^{\sin x} dx$$
 and $J = \int_{0}^{\cos x} dx$. Then which one of the following is true?
(1) $I < \frac{2}{3}$ and $J > 2$ (2) $I > \frac{2}{3}$ and $J < 2$ (3) $I > \frac{2}{3}$ and $J > 2$ (4) $I < \frac{2}{3}$ and $J < 2$
Sol: We know that $\frac{\sin x}{x} < 1$, when $x \in (0, 1) = \frac{1}{9} \frac{\cos x}{\sqrt{x}} < x$ $= \int_{0}^{1} \frac{\sin x}{\sqrt{x}} < \frac{2}{3}$
Again $\frac{\cos x}{\sqrt{x}} < \frac{1}{\sqrt{x}}$ when $x \in (0, 1) = \int_{0}^{1} \frac{\cos x}{\sqrt{x}} < 2$
Correct choice: (0)
12. The area of the plane region bounded by the curves $x + 2y^2 = 0$ and $x + 3y^2 = 1$ is equal to
(1) $\frac{2}{3}$ (2) $\frac{4}{3}$ (3) $\frac{5}{3}$
Sol: $x + 2y^2 = 0 \Rightarrow y^2 = -\frac{x}{2}$ parabola
 $x + 3y^2 = 1 \Rightarrow y^2 = -\frac{1}{3}(x-1)$ panabola
Solving equation of two parabolas simultaneously, we get $x = -2$, $y = 21$
Area of the region ABCA
 $= \int_{0}^{1} \left[(-2y^2 - 1 + 3y^2) dy \right] = \left| \int_{0}^{1} \left[y^2 - 1 \right] dy \right| = \left| \left| \frac{x^3}{3} - y \right|_{0}^{1} \right| = \left| \frac{1}{3} + \frac{9}{3} + \frac{9}{3}$

*14. The statement $p \rightarrow (q \rightarrow p)$ is equivalent to

$$(1) \ p \to (p \land q) \qquad (2) \ p \to (p \leftrightarrow q) \qquad (3) \ p \to (p \to q) \qquad (4) \ p \to (p \lor q)$$

Sol:

р	q	p∨q	$q \rightarrow p$	$p \rightarrow (q \rightarrow p)$	$p \rightarrow (p \lor q)$	
Т	Т	Т	Т	Т	Т	
Т	F	Т	Т	Т	Т	
F	Т	Т	F	Т	Т	
F	F	F	Т	Т	Т	

(3)

Correct choice: (4)

15. The value of $\cot\left(\csc^{-1}\frac{5}{3}+\tan^{-1}\frac{2}{3}\right)$ is

(1)
$$\frac{4}{17}$$
 (2) $\frac{5}{17}$

Sol:
$$\cot\left(\csc^{-1}\left(\frac{5}{3}\right) + \tan^{-1}\left(\frac{2}{3}\right)\right) = \cot\left(\tan^{-1}\frac{3}{4} + \tan^{-1}\frac{2}{3}\right) = \cot\left(\tan^{-1}\left(\frac{9}{12} + \frac{8}{12}\right)\right)$$

 $\cot\left(\tan^{-1}\left(\frac{9}{12} + \frac{8}{12}\right)\right) = \cot\left(\cot^{-1}\left(\frac{6}{17}\right)\right) = \frac{6}{17}$

Correct choice: (3)

Directions: Questions number 16 to 20 are Assertion Reason, type questions. Each of these questions contains two statements: Statement-I (Assertion) and Statement-2 (Reason). Each of these questions also has four alternative choices, only one of which is the correct answer. You have to select the correct choice.

16. Let A be a 2 × 2 matrix with real entries. Let I be the 2 × 2 identity matrix. Denote by tr(A), the sum of diagonal entries of A. Assume that A² = I.

Statement-1: If $A \neq I$ and $A \neq -I$, then det A = -1.

Statement-2: If $A \neq I$ and $A \neq -I$, then $tr(A) \neq 0$.

- (1) Statement-1 is true, Statement-2 is rue; Statement -2 is not a correct explanation for Statement-1.
- (2) Statement-1 is true, Statement-2 is false.
- (3) Statement-1 is false, Statement-2 is true.
- (4) Statement-Lis true, Statement-2 is true; Statement-2 is a correct explanation for Statement-1.

Sol: Let A =

$$a^{2} + bc = 1$$
, $bc + d^{2} = 1$, $(a + d)b = 0$, $(a + d)c = 0$

Out of all possible matrices if we consider
$$A = \begin{bmatrix} 1 & 0 \\ 0 & -1 \end{bmatrix}$$
, then tr $A = 0$.

⇒ Statement-2 is wrong.

Again if $A \neq \pm I$, then |A| = -1

 \Rightarrow Statement-1 is correct.

Correct choice: (2)

Let p be the statement "r is an irrational number", q be the statement "p is a transcendental number", and r be the statement *17. "x is a rational number iff y is a transcendental number".

Statement-1: r is equivalent to either q or p.

Statement-2: r is equivalent to $\sim (p \leftrightarrow \sim q)$.

- (1) Statement-1 is true, Statement-2 is true; Statement -2 is not a correct explanation for Statement-1.
- (2) Statement-1 is true, Statement-2 is false.
- (3) Statement-1 is false, Statement-2 is true.
- (4) Statement-1 is true, Statement-2 is true; Statement-2 is a correct explanation for Statement-1.

Sol: *p* : *x* is an irrational number

- q: y is a transcendental number
- r: x is a rational number iff y is a transcendental number
- $\Rightarrow r \sim p \leftrightarrow q$
 - $s_1:q$ or p
 - $s_2 :\sim (p \leftrightarrow q)$

ų .y is au			liber					
r∶xisana	ational n	umber iff	y is a trans	cendental num	ber			
$\Rightarrow r \sim p$	$\phi \leftrightarrow q$							
51:q	or p							
s ₂ :~	$(p \leftrightarrow a)$	g)						
р	q	~ p	~ q	$r \sim p \leftrightarrow q$	s ₁ q or p	$p \leftrightarrow q$	$(p \leftrightarrow q)$	
Т	Т	F	F	F	Т	F	Т	
Т	F	F	Т	Т	Т	Т	F	
F	Т	Т	F	Т	Т	Т	F	
F	F	Т	Т	F	F	F	Т	

Clearly s_1 and r are not equivalent \Rightarrow Statement-1 is false.

Also s_2 and r are not equivalent \Rightarrow Statement-2 is also false. Hence none of the option is correct.

*18. In a shop there are five types of ice-creams available. A child buys six ice-creams.

Statement-1: The number of different ways the child can buy the six ice-creams is $^{10}C_5$.

Statement-2: The number of different ways the child can buy the six ice-creams is equal to the number of different ways of arranging 6 A's and 4 B's in a row,

(1) Statement-1 is true, Statement-2 is true, Statement -2 is not a correct explanation for Statement-1.

- (2) Statement-1 is true, Statement-2 is false.
- (3) Statement-1 is false, Statement-2 is true.
- (4) Statement-1 is true, Statement-2 is true; Statement-2 is a correct explanation for Statement-1.
- Statement-1: Number of ways = number of non negative integral solutions of the equation $T_1 + T_2 + T_3 + T_4 + T_5 = 6$ Sol:

= 10 C4 = 6+5-1 C

∴ Statement-1 is wrong.

Statement 2: Number of different ways of arranging 6A's and 4B's in a row = $\frac{10!}{6!4!} = {}^{10}C_4$

... Statement-2 is correct.

Correct choice: (3)

*19. Statement 1:
$$\sum_{r=0}^{n} (r+1)^{n} C_{r} = (n+2)2^{n-1}.$$
Statement 2:
$$\sum_{r=0}^{n} (r+1)^{n} C_{r} x^{r} = (1+x)^{n} + nx(1+x)^{n-1}.$$
(1) Statement 1: is true, Statement 2: is not a correct explanation for Statement 1.
(2) Statement 1: is true, Statement 2: is true: a correct explanation for Statement 1.
(3) Statement 1: is true, Statement 2: is true: a correct explanation for Statement 1.
(4) Statement 1: is true, Statement 2: is true: a correct explanation for Statement 1.
(5) Statement 1: is true, Statement 2: is true: a correct explanation for Statement 1.
(5) Statement 1: is true, Statement 2: is true: a correct explanation for Statement 1.
(6) Statement 1: is also true.
Correct choice: (6)
*20. Statement 1: For every natural number $n \ge 2$, $\frac{1}{2^{n}} + \frac{1}{2^{n}} + \dots + \frac{1}{\sqrt{n}} > \sqrt{n}$
Statement 1: is also true.
Correct choice: (6)
*20. Statement 1: For every natural number $n \ge 2$, $\frac{1}{2^{n}} + \frac{1}{2^{n}} + \dots + \frac{1}{\sqrt{n}} > \sqrt{n}$
Statement 1: is false. Statement 2: is true.
(3) Statement 1: is true, Statement 2: is true.
(4) Statement 1: is false. Statement 2: is true.
(5) Statement 1: is false. Statement 2: is true.
(5) Statement 1: is false. Statement 2: is true.
(6) Statement 1: is false. Statement 2: is true.
(7) Statement 1: is false. Statement 2: is true.
(8) Statement 1: is false. Statement 2: is true.
(9) Statement 1: is false. Statement 2: is true.
(1) Statement 1: $\sqrt{n} < \sqrt{n+1} = \sqrt{2} < \sqrt{3} < \sqrt{n} = \frac{1}{\sqrt{n}}$
 $\sqrt{n} \le \sqrt{n} < \frac{1}{\sqrt{n}} = \frac{1}{\sqrt{n}} = \frac{1}{\sqrt{n}}$
 $\sqrt{n} \le \sqrt{n} < \frac{1}{\sqrt{n}} = \frac{1}{\sqrt{n}} = \frac{1}{\sqrt{n}}$
 $\sqrt{n} \le \sqrt{n} < \frac{1}{\sqrt{n}} = \frac{1}{\sqrt{n}} = \frac{1}{\sqrt{n}}$
Statement 1: $\sqrt{n} < \sqrt{n+1} = \sqrt{2} < \sqrt{3} < \sqrt{n} = \frac{1}{\sqrt{n}}$
 $\sqrt{n} \le \sqrt{n} < \frac{1}{\sqrt{n}} = \frac{1}{\sqrt{n}} =$

 $S = \{(x, y) : y = x+1 \text{ and } 0 < x < 2\}$ $T = \{(x, y) : x - y \text{ is an integel}\}.$ Which one of the following is true? (1) S is an equivalence relation on R but T is not (2) T is an equivalence relation on R but S is not (3) Neither S nor T is an equivalence relation on R(4) Both S and T are equivalence relations on R**Sol:** For $S_{x} = x + 1$ for reflexive $x = x + 1 \implies 0 = 1$ \Rightarrow S is not reflexive. So S can not be equivalence. For $T, x-y \in I$, then $x-x=0 \in I \implies T$ is reflexive. $x-y \in I$, then $y-x \in I \implies T$ is symmetric also. Now $x - y \in I$ and $y - z \in I$ $\Rightarrow x - z \in I \Rightarrow T$ is transitive also. Hence T is an equivalence relation. Correct choice: (2)

23. Let $f: N \to Y$ be a function defined as f(x) = 4x+3, where $Y = \{y \in N : y = 4x+3 \text{ for some } x \in N\}$. Show that f is invertible and its inverse is

 $(3) g(y) = \frac{3y+4}{3}$

(4) $g(y) = 4 + \frac{y+3}{4}$

(1)
$$g(y) = \frac{y+3}{4}$$
 (2) $g(y) = \frac{y-3}{4}$

Sol.: Clearly f is bijective function so it is invertible.

$$y = 4x + 3 \implies \frac{y-3}{4} = x \implies g(y) = \frac{y-3}{4}$$

Correct choice: (2)

*24. AB is a vertical pole with B at the ground level and A at the top A man finds that the angle of elevation of the point A from a certain point C on the ground is 60°. He moves away from the pole along the line BC to a point D such that CD = 7 m. From D the angle of elevation of the point A is 45°. Then the height of the pole is

(1)
$$\frac{7\sqrt{3}}{2} \left(\sqrt{3} - 1\right) \mathrm{m}$$

(2) $\frac{7\sqrt{3}}{2} \frac{1}{\sqrt{3} + 1} \mathrm{m}$
(3) $\frac{7\sqrt{3}}{2} \frac{1}{\sqrt{3} - 1} \mathrm{m}$
(4) $\frac{7\sqrt{3}}{2} \left(\sqrt{3} + 1\right) \mathrm{m}$
Sol: $\tan 60^\circ = \frac{h}{BC}$
 $\therefore (i)$ and $\tan 45^\circ = \frac{h}{7 + BC}$
 $\Rightarrow 7 + BC = h \Rightarrow BC = h - 7$
From (i) $\Rightarrow \sqrt{3} = \frac{h}{h - 7} \Rightarrow \sqrt{3}h - 7\sqrt{3} = h \Rightarrow \sqrt{3}h - h = 7\sqrt{3}$
 $h = \frac{7\sqrt{3}}{\sqrt{3} - 1} \Rightarrow \frac{7\sqrt{3} \left(\sqrt{3} + 1\right)}{2} \mathrm{m}$
Correct choice: (4)

*25. A die is thrown. Let A be the event that the number obtained is greater than 3. Let B be the event that the number obtained is less than 5. Then $P(A \cup B)$ is

(1)
(2)
$$\frac{2}{5}$$
(3) $\frac{3}{5}$
(4) 0
Sol: $n(A \cup B) = \{1, 2, 3, 4, 5, 6\} \Rightarrow P(A \cup B) = 1$
Correct choice: (1)

26. It is given that the events A and B are such that $P(A) = \frac{1}{4}$, $P(A|B) = \frac{1}{2}$ and $P(B|A) = \frac{2}{3}$. Then P(B) is

(1)
$$\frac{2}{3}$$
 (2) $\frac{1}{2}$ (3) $\frac{1}{6}$ (4) $\frac{1}{3}$

Sol:
$$F(4) = \frac{1}{4}$$

 $f(\frac{d}{B}) = \frac{F(4 \cap B)}{F(B)} = \frac{1}{2} = \frac{F(4 \cap B)}{F(B)}$...(i)
 $f(\frac{d}{B}) = \frac{F(4 \cap B)}{F(A)} = \frac{2}{3} = \frac{F(4 \cap B)}{1/4} = F(4 \cap B) = \frac{1}{6}$. Putting the value of $F(4 \cap B)$ in (i) $\Rightarrow F(B) = 2 \times \frac{1}{6} = \frac{1}{3}$
Correct choice: (d)
***27.** A focus of an ellipse is at the origin. The directivix is the line $x = 4$ and the eccentricity is $\frac{1}{2}$. Then the length of the environ
major axis is
(i) $\frac{4}{3}$...(i) $\frac{5}{3}$...(i) $\frac{8}{3}$...(i) $\frac{8}{3}$...(i) $\frac{2}{3}$
Sol: Perpendicular distance from focus on directive $\frac{|0-4|}{\sqrt{1}} = \frac{a}{e} - ae = 4 = 2a - \frac{a}{2} \Rightarrow 4 = \frac{3a}{2} = -\frac{a}{2}$
Sol: Perpendicular distance from focus on directive $\frac{10-4}{\sqrt{1}} = \frac{a}{e} - ae = 4 = 2a - \frac{a}{2} \Rightarrow 4 = \frac{3a}{2} = -\frac{a}{2}$
Sol: Perpendicular distance from focus on directive $\frac{10-4}{\sqrt{1}} = \frac{a}{e} - ae = 2a - \frac{a}{2} \Rightarrow 4 = \frac{3a}{2} = -\frac{a}{2}$
Sol: Perpendicular distance from focus on directive $\frac{10-4}{\sqrt{1}} = \frac{a}{e} - ae = 2a - \frac{a}{2} \Rightarrow 4 = \frac{3a}{2} = -\frac{a}{2}$
Sol: Vertex will be maid point of F and M.
So, (1, 0)
Correct choice: (d)
***30.** User two will be maid point of F and M.
So, (1, 0)
Correct choice: (d)
***31.** The point dime trically opposite to the point $F(1, 0)$ on there in $e^{2} + y^{2} + 2z + 4y - 3 = 0$ is
(1) $(-3, -4)$(i) $(2) (2, 0)$(i) $(3 (3 - 4)$(i) $(-3, 4)$
Sol: Given $x^{3} + y^{2} + 2z + 4y - 3 = 0$. (2) $(2, 0)$(i) $(3 (3 - 4)$(4) $(-3, 4)$
Sol: Correct choice: (1)
***30.** The propendicular balancher will be in the segment joning $F(1, 4)$ and $Q(k, 3)$ has *y*-intercept -4. Then a possible value of *k* is
(1) -2(2) (-4) ...(3) 1 ...(4) (2)
Sol: Equation of perpendicular basector of FQ is $y - \frac{7}{2} = (k-1)\left(x - \frac{k+1}{2}\right)$
Similarity is, $\frac{B-k^{2}}{2} = -4 \Rightarrow k = 44$
Correct choice:(2)
***31.** The first two terms of a geometric progression add up to 12. The sum of the that and he foru therms is 48. If the terms of the progression are alternative protive and negative



PART-B CHEMISTRY



Correct choice: (1)

*43. Among the following substituted silanes the one which will give rise to cross linked silicone polymer on hydrolysis is





- 54. At 80°C, the vapour pressure of pure liquid 'A' is 520 mm Hg and that of pure liquid 'B' is 1000 mm Hg. If a mixture solution of 'A' and 'B' boils at 80°C and 1 atm pressure, the amount of 'A' in the mixture is (1 atm = 760 mm Hg) (1) 48 mol percent (2) 50 mol percent (3) 52 mol percent (4) 34 mol percent **Sol:** $P_{I} = 760 = P_{A}^{o} X_{A} + P_{B}^{o} X_{B} = 520 X_{A} + 1000 (1 - X_{A})$ $X_A = \frac{1}{2}$ or 50 mol percent. Correct choice: (2) For a reaction $\frac{1}{2} A \longrightarrow 2B$, rate of disappearance of 'A' is related to the rate of appearance of 'B' by the expression 55. (2) $-\frac{d[A]}{dt} = 4\frac{d[B]}{dt}$ (3) $-\frac{d[A]}{dt} = \frac{1}{2}\frac{d[B]}{dt}$ (4) $-\frac{d[A]}{dt} = \frac{1}{4}\frac{d[B]}{dt}$ $(1) - \frac{d[A]}{dt} = \frac{d[B]}{dt}$ **Sol:** $\frac{-2d[A]}{4t}$ = Rate of reaction with respect to A. $\frac{1}{2} \frac{d[B]}{dt}$ = Rate of reaction with respect to B. $\frac{-2\mathrm{d}[\mathsf{A}]}{\mathrm{d}t} = \frac{1}{2}\frac{\mathrm{d}[\mathsf{B}]}{\mathrm{d}t}, \quad -\frac{\mathrm{d}[\mathsf{A}]}{\mathrm{d}t} = \frac{1}{4}\frac{\mathrm{d}[\mathsf{B}]}{\mathrm{d}t}$ Correct choice: (4) The equilibrium constants K_{p_1} and K_{p_2} for the reactions $X \rightleftharpoons 2Y$ and $Z \rightleftharpoons P + Q$ respectively are in the ratio of *56. 1:9. If the degree of dissociation of X and Z be equal then the ratio of total pressures at these equilibria is (1)1:3(2)1:9 (3)1:36(4) 1 : 1 Sol: Let initial moles of X and Z taken are 'a' and 'b' respectively. $\begin{array}{ccc} X & \overleftarrow{} & 2y \\ Moles at equilibrium & a(1-\alpha) & 2a\alpha \end{array}$ Moles at equilibrium b(1 ba ba $K_{\mathbf{p}_{1}} = \frac{(2\alpha\alpha)^{2} P_{\mathbf{T}_{1}}}{\alpha(1-\alpha) \alpha(1+\alpha)}$ K_{P2}· $\frac{K_{P_1}}{K_{P_2}} = \frac{4P_{T_1}}{P_{T_2}} = \frac{1}{9} \quad ; \quad \frac{P_{T_1}}{P_{T_2}} = \frac{1}{36} \, .$ Correct choice: (3) In context with the industrial preparation of hydrogen from water gas $(CO + H_2)$, which of the following is the correct *57. state ment?
 - (1) H_2 is removed through occlusion with Pd.
 - (2) CO is oxidised to CO₂ with steam in the presence of a catalyst followed by absorption of CO₂ in alkali.
 - (3) CO and H₂ are fractionally separated using differences in their densities.
 - (4) CO is removed by absorption in aqueous Cu₂Cl₂ solution.

Sol:
$$\underbrace{CO + H_2}_{Water gas} + H_2 \xrightarrow{Catabas} O_2 + 2H_2 \xrightarrow{2NaOH} Na_2CO_3 + H_2O$$

Correct choice: (2)

- **58.** In which of the following octahedral complexes of Co (atomic number 27), will the magnitude of Δ_0 be the highest? (1) $[Co(H_2O)]^{3+}$ (2) $[Co(NH_3)]^{3+}$ (3) $[Co(CN)]^{3-}$ (4) $[Co(C_2O_4)]^{3-}$
- Sol: Magnitude of Δ_s will be highest with the strongest ligand. Since, CN^- is the strongest ligand of all, thus would lead to a greater separation between t_{2g} and e_g orbitals.

Correct choice: (3)

- 59. The coordination number and the oxidation state of the element 'E' in the complex [E(en)₂(C₂O₄)]NO₂ (where (en) is ethylene diamine) are, respectively,
 - (1) 4 and 3 (2) 6 and 3 (3) 6 and 2 (4) 4 and 2
- Sol: (en) and oxalate ion are both bidentate ligands. Co-ordination number of E in the complex = (2 × 2) + (1 × 2) = 6. Oxidation state of E in the complex = [x + (-2) = +1] = +3.

Correct choice: (2)

*60. Identify the wrong statement in the following:

- Ozone layer does not permit infrared radiation from the sun to reach the earth.
- (2) Acid rain is mostly because of oxides of nitrogen and sulphur.
- (3) Chlorofluorocarbons are responsible for ozone layer depletion.
- (4) Greenhouse effect is responsible for global warming.

Sol: Ozone layer prevents the ultra violet radiations and not the infrared radiations from the sun to reach the earth.

Correct choice: (1)

- б1. Larger number of oxidation states are exhibited by the actinoids than those by lanthanoids, the main reason being
 - more energy difference between 5f and 6d than between 4f and 5d orbitals.
 - (2) more reactive nature of the actinoids than the lanthanoids.
 - (3) 4f orbitals more diffused than the 5f orbitals.
 - (4) lesser energy difference between 5f and 6d than between 4f and 5d orbitals.
- Sol: The energy difference between 5f and 6d is lesser than that between 4f and 5d orbitals. Thus, in actinoids, the electrons can be removed from 5f as well as 6d, so more number of oxidation states are exhibited by them.

Correct choice: (4)

- б2. In a compound, atoms of element Y form ccp lattice and those of element X occupy 2/3st of tetrahedral voids. The formula of the compound will be (A) X₂Y₃ (2) X₃Y₄ $(3) X_4 Y_3$
 - (1) X₂Y
- Sol: Number of effective Y in a unit cell = 4.

Number of effective X in a unit cell = $8 \times \frac{2}{2} = \frac{16}{2}$.

So, formula of the compound = $X_{16/3}Y_4 = X_{1/3}Y_{1/4} = X_4Y_3$

Correct choice: (3)

- Gold numbers of protective colloids (A), (B), (C) and (D) are 050, 001, 0,10 and 0.005, respectively. The correct order of бЗ. their protective powers is (2)(B) < (D) < (A) < (C)(3) (D) < (A) < (C) < (B) $(4)(C) \le (B) \le (D) \le (A)$
- (1)(A) < (C) < (B) < (D)Sol: Lesser the value of gold number of a protective colloid better is the protective power. \therefore (A) < (C) < (B) < (D)

Correct choice: (1)

The vapour pressure of water at 20°C is 17.5 mm Hg. If 18 g of glucose (C (H12O)) is added to 178.2 g of water at 20°C, the б4. vapour pressure of the resulting solution will be (1) 16.500 mm Hg (2) 17.325 mm Hg (3) 17.675 mm Hg (4) 15.750 mm Hg

(4) CH₃CHO

Sol: Moles of glucose =
$$\frac{18}{180}$$
 = 0.1, moles of H₂O = $\frac{178.2}{18}$ = 9.9

$$\frac{P^{\circ} - P_{S}}{P_{S}} = \frac{\text{moles of gluose}}{\text{moles of water}}, 17.5 - P_{g} = \frac{0.1 \times P_{S}}{9.9}$$
$$P_{g} = 17.325 \text{ mm Hg}.$$

Correct choice: (2)

- б5. Bake lite is obtained from phenol by reacting with (1) CH₃COCH₃ (2) HCHO $(3)(CH_2OH)_2$
- $\xrightarrow{\text{acid}} \circ$ and p-hydroxybenzylalcohol $\xrightarrow{\Delta}$ Bakelite Sol: Phenol + HCHO-Correct choice: (2)

őő. The absolute configuration of

HO₂C
$$CO_2H$$

HO H H OH
(1) R S (2) S, R (3) S, S (4) R, R



Correct choice: (4)

- *67. For the following three reactions a, b, c, equilibrium constants are given:
- a. $CO(g) + H_2O(g) \implies CO_2(g) + H_2(g)$; K_1 b. $CH_4(g) + H_2O(g) \implies CO(g) + 3H_2(g)$; K_2 c. $CH_4(g) + 2H_2O(g) \rightleftharpoons CO_2(g) + 4H_2(g)$; K_3 Which of the following relations is correct? (3) $K_1 \sqrt{K_2} = K_3$ (2) $K_3 \cdot K_2^3 = K_1^2$ (1) $K_3 = K_1 K_2$ $(4) K_2 K_3 = K_1$ Sol: $CO(g) + H_2O(g) \implies CO_2(g) + H_2(g)$; K_1 $CH_4(g) + H_2O(g) \rightleftharpoons CO(g) + 3H_2(g)$; K_2 $CH_4(g) + 2H_2O(g) \implies CO_2(g) + 4H_2(g); K_3 = K_1 \times K_2$ Correct choice: (1) Standard entropy of X2, Y2 and XY3 are 60, 40 and 50 JK⁻¹ mol⁻¹, respectively. For the reaction, $\rightarrow XY_{3}$, б8. $\Delta H = -30$ kJ, to be at equilibrium, the temperature will be (4) 500 K (3) 1250 K (1) 750 K (2) 1000 K **Sol:** $\frac{1}{2}X_2 + \frac{3}{2}Y_2 \longrightarrow XY_3$; $\Delta S = 50 - \left[\left(60 \times \frac{1}{2}\right) + \left(40 \times \frac{3}{2}\right)\right] = -40 \text{ JK}^{-1}$; $\Delta H = -30 \text{ kJ}$ $\Delta G = \Delta H - T \Delta S$ At equilibrium, $\Delta G = 0$; $\therefore \Delta H = T\Delta S$; $T = \frac{\Delta H}{\Delta S} = \frac{-30000J}{-40 \text{ JK}^{-1}} = 750 \text{ K}.$ Correct choice: (1) The electrophile, E^Φattacks the benzene ring to generate the intermediate σ-complex. Of the following, which σ-complex is *69. of lowest energy? (3) Arenium ion (σ -complex) formed by the attack of electrophile on nitrobenzene at any one of the three positions is less stable Sol: than that formed by the attack of electrophile on benzene. Correct choice: (4) 70. α -D-(+)-glucose and β -D-(+)-glucose are (1) anomers (2) enantiomers (3) conformers (4) epimers cz-D-(+)-glucose and g-D-(+)-glucose are those diastereomers that differ in configuration at C-1 atom. Such isomers are Sol: referred as anomers Correct c hoice: (1)

PART-C PHYSICS

71. This question contains Statement-1 and Statement -2. Of the four choices given after the statements, choose the one that best describes the two statements.

Statement - l: Energy is released when heavy nuclei undergo fission or light nuclei undergo fusion.

and

Statement -2: For heavy nuclei, binding energy per nucleon increases with increasing Z while for light nuclei it decreases with increasing Z.

- (1) Statement -1 is true, Statement-2 is true; Statement -2 is not a correct explanation for Statement-1
- (2) Statement -1 is true, Statement-2 is false
- (3) Statement -1 is false, Statement-2 is true
- (4) Statement -1 is true, Statement-2 is true; Statement -2 is a correct explanation for Statement-1

Sol: Correct choice: (2)

*72. This question contains Statement-1 and Statement -2. Of the four choices given after the statements, choose the one that best describes the two statements.

Statement -1: For a mass M kept at the centre of a cube of side 'a' the flux of gravitational field passing through its sides is 4π GM.

and

Statement -2: If the direction of a field due to a point source is radial and its dependence on the distance 'r' from the source is

given as $\frac{1}{r^2}$, its flux through a closed surface depends only on the strength of the source enclosed by the surface and not on

the size or shape of the surface.

- (1) Statement -1 is true, Statement-2 is true; Statement -2 is not a correct explanation for Statement-1
- (2) Statement -1 is true, Statement-2 is false
- (3) Statement -1 is false, Statement- 2 is true

(4) Statement -1 is true, Statement-2 is true; Statement -2 is a correct explanation for Statement-1

Sol:
$$\oint \vec{E}_{g} d\vec{s} = -4\pi GM_{embred} = -4\pi GM$$

Correct choice: (4)

*73. Two full turns of the circular scale of a screw gauge cover a distance of 1 mm on its main scale. The total number of divisions on circular scale is 50. Further, it is found that screw gauge has a zero error of - 0.03mm. While measuring the diameter of a thin wire, a student notes the main scale reading of 3mm and the number of circular scale divisions in line with the main scale as 35. The diameter of wire is

(1) 3.67 mm

(3) 3.32 mm

(4) 3.73 mm

Sol: Least count = $\frac{0.5 \text{nm}}{50}$ = 0.01mm

Zero error ≈ -0.03 mm

Measured diameter = $3 \text{ mm} + 35 \times 0.01 \text{ mm} = 3.35 \text{ mm}$

Connected diameter = 3.35 mm - (-0.03 mm) = 3.38 mm

Correct choice: (2)

An insulated container of gas has two chambers separated by an insulating partition. One of the chambers has volume V_1 and contains ideal gas at pressure P_1 and temperature T_1 . The other chamber has volume V_2 and contains ideal gas at pressure P_2 and temperature T_2 . If the partition is removed without doing any work on the gas, the final equilibrium temperature of the gas in the container will be

(1) $\frac{P_1 V_1 T_2 + P_2 V_2 T_1}{P_1 V_1 + P_2 V_2}$	(2) $\frac{T_1T_2(P_1V_1 + P_2V_2)}{P_1V_1T_1 + P_2V_2T_2}$
(3) $\frac{T_1T_2(P_1V_1 + P_2V_2)}{P_1V_1T_2 + P_2V_2T_1}$	$(4) \ \frac{P_1 V_1 T_1 + P_2 V_2 T_2}{P_1 V_1 + P_2 V_2}$

Sol: Internal energy of the system will remain conserved.

$$(n_{I} + n_{2})C_{v}T = n_{I}C_{v}T_{I} + n_{2}C_{v}T_{2}$$

$$\left(\frac{P_{I}V_{1}}{RT_{1}} + \frac{P_{2}V_{2}}{RT_{2}}\right)T = \frac{P_{I}V_{1}}{R} + \frac{P_{2}V_{2}}{R} ; \qquad T = \frac{T_{1}T_{2}(P_{I}V_{1} + P_{2}V_{2})}{P_{I}V_{1}T_{2} + P_{2}V_{2}T_{1}}$$
Correct choice: (3)

75. A student measures the focal length of a convex lens by putting an object pin at a distance 'u' from the lens and measuring the distance 'v' of the image pin. The graph between 'u' and 'v' plotted by the student should look like



Directions: Questions No. 76 and 77 are based on the following paragraph

Consider a block of conducting material of resistivity ' ρ ' shown in the figure. Current 'I' enters at 'A' and leaves from 'D'. We apply superposition principal to find voltage ' ΔV ' developed between 'B' and 'C'. The calculation is done in the following steps:

- (i) Take current 'I' entering from 'A' and assume it to spread over a hemispherical surface in the block.
- (ii) Calculate field E(r) at distance 'r' from A by using Ohm's law E = ρj, where 'j' is the current per unit area at 'r'.
- (iii) From the 'r' dependence of E(r), obtain the potential V(r) at 'r'.

(iv) Repeat (i), (ii) and (iii) for current 'I' leaving 'D' and superpose results for 'A' and 'D'.



Correct choice: (3)



(2) $\frac{2}{2}$ ma²

Sol: Correct choice: (1)

*78. Consider a uniform square plate of side 'a' and mass 'm'. The moment of inertia of this plate about an axis perpendicular to its plane and passing through one of its corners is

(3) $\frac{5}{6}$ ma²

(1)
$$\frac{7}{12}$$
 ma²

Sol: I = I_{cm} + md² =
$$\frac{ma^2}{6} + m\left(\frac{a}{\sqrt{2}}\right)^2 = \frac{2}{3}ma^2$$

- An experiment is performed to find the refractive index of glass using a travelling microscope. In this experiment distances 79. are measured by
 - (1) a meter scale provided on the microscope
 - (3) a vernier scale provided on the microscope
- Sol: Correct choice: (3)

(2) a screw gauge provided on the microscope (4) a standard laboratory scale.

(4) $\frac{\rho l}{r^2}$

(4) $\frac{1}{12}$ ma²

80. A horizontal overhead powerline is at a height of 4m from the ground and carries a current of 100 A from east to west. The magnetic field directly below it on the ground is $(\mu_0 = 4\pi \times 10^{-7} \text{ T} \text{ m A}^{-1})$ (2) 2.5×10^{-7} T northward

(1)
$$5 \times 10^{-4}$$
 T southward

(3) 2.5×10^{-7} T southward

Sol:
$$B = \frac{\mu_0}{4\pi} \frac{2i}{r} = 5 \times 10^{-6} T$$

Correct choice: (1)

The speed of sound in oxygen (O2) at a certain temperature is 460 ms⁻¹. The speed of sound in helium (He) at the same *81. temperature will be (assume both gases to be ideal) ns⁻¹ (2) 330 ms

 $V = \sqrt{\frac{5RT}{2\times 4}}$... (ii)

⇒

(3) 460 ms⁻¹ $(4) 500 \text{ ms}^{-1}$

(4) 5 × 10⁻⁴ T north ward

Sol: $V = \sqrt{\frac{\gamma RT}{M_0}}$ $460 = \sqrt{\frac{7RT}{5 \times 32}}$

 $V = 3.08 \times 460 = 1419 \text{ ms}^{-1}$

Correct choice: (no ne of the answers is correct)

- 82. A SV battery with internal resistance 2Ω and a 2Vbattery with internal resistance 1 Ω are connected to a 10 Ω resistor as shown in the figure. The current in the 10 Ω resistor is (1) 0.03 A P₂ to P₁ (2) 0.27 A P1 to P2
 - (4) 0.03 A P₁ to P₂ (3) 0.27 A P₂ to P₁
- **Sol:** $i = \frac{\epsilon_1 \epsilon_2 + \epsilon_2 \epsilon_1}{\epsilon_1 \epsilon_2 + \epsilon_1 \epsilon_1 + \epsilon_1 \epsilon_2} = \frac{5 \times 1 + (-2) \times 2}{2 \times 1 + 10 \times 2 + 10 \times 1} = 0.03 \text{ A}$ Correct choice: (1)



A body of mass m = 3.513 kg is moving along the x-axis with a speed of 5.00 ms⁻¹. The magnitude of its momentum is *83. recorded as

(1) 17.56 kg ms⁻¹ (2) 17.57 kg ms⁻¹ (3) 17.6 kg ms⁻¹ **Sol:** $p = mv = 3.513 \times 5.00 = 17.565 \text{ kg ms}^{-1}$ Since result should have only 3 significant digits

 $\therefore p = 17.6 \text{ kg ms}^{-1}$ Correct choice: (3)

84. A working transistor with its three legs marked P, Q and R is tested using a multimeter. No conduction is found between P and Q. By connecting the common (negative) terminal of the multimeter to R and the other (positive) terminal to P 🚛 some resistance is seen on the multimeter. Which of the following is true for the transistor?

(1) It is a pnp transistor with R as emitter

(2) It is an npn transistor with R as collector (4) It is a pnp transistor with R as collector

(3) It is an npn transistor with R as base

Sol.: Correct choice: (3)

A block of mass 0.50 kg is moving with a speed of 2.00 ms⁻¹ on a smooth surface. It strikes another mass of 1.00 kg and *85. then they move together as a single body. The energy loss during the collision is

(1) 0.67 J (2) 0.34 J (3) 0.16 J (4) 1.00 J

(4) 17.565 kg ms⁻¹

Sol: Using momentum conservation, $0.5 \times 2 = 1.5 \times v \implies v = \frac{2}{2} ms^{-1}$

Loss of energy =
$$\left[\left(\frac{1}{2} \times 0.5 \times (2)^2 \right) - \frac{1}{2} \times 1.5 \times \left(\frac{2}{3} \right)^2 \right] = 1 - \frac{1}{3} = 0.67 \text{ J}$$

Correct choice: (1)

A wave travelling along the x-axis is described by the equation $\overline{y}(x, t) = 0.005 \cos(\alpha x - \beta t)$. If the wavelength and the time *86. period of the wave are 0.08 m and 2.0 s, respectively, then α and β in appropriate units are

(1)
$$\alpha = \frac{0.04}{\pi}$$
, $\beta = \frac{1.0}{\pi}$
(2) $\alpha = 1250\pi$, $\beta = \frac{\pi}{2.0}$
(3) $\alpha = 25.00\pi$, $\beta = \pi$
(4) $\alpha = \frac{0.08}{\pi}$, $\beta = \frac{2.0}{\pi}$
Sol: $\alpha = \frac{2\pi}{\lambda} = \frac{2\pi}{0.08} = 25\pi$; $\beta = \frac{2\pi}{1} = \frac{2\pi}{2} = \pi$
Correct choice: (3)

- 87. Two coaxial solaring are made by winding thin insulated wire over a pipe of cross sectional area $A = 10 \text{ cm}^2$ and length = 20 cm. If one of the science is ($\mu_{b} = 4\pi \times 10^{-7}$ T m A⁻¹)
 - (2) 2.4 π× 10⁻⁴ H (3) 2.4 $\pi \times 10^{-5}$ H (4) $4.8 \ \pi \times 10^{-4} \ H$
- Sol: Correct c hoice: (2)

(1) $4.8 \ \pi \times 10$

*88. A capillary tube (A) is dipped in water. Another identical tube (B) is dipped in a soap-water solution. Which of the following shows the relative nature of the liquid columns in the two tubes?



90.

Directions : Questions No. 91, 92 and 93 are based on the following paragraph.

Wave property of electrons implies that they will show diffraction effects. Davisson and Germer demonstrated this by diffracting electrons from crystals. The law governing the diffraction from a crystal is obtained by requiring that electron waves reflected from the planes of atoms in a crystal interfere constructively (see figure).



92. If a strong diffraction peak is observed when electrons are incident at an angle 'i' from the normal to the crystal planes with distance 'd' between them (see figure), de Broglie wavelength $\lambda_{\rm HE}$ of electrons can be calculated by the relationship (n is an integer)

(1) 2 d sini = nλ_{dB}
(2) d cos i = nλ_{dB}
(3) d sini = nλ_{dB}
(4) 2 d cos i = nλ_{dB}
Sol: For strong peak, path difference = nλ_{dB}
∴ 2d cos i = nλ_{dB}
Correct c hoice: (4)
93. In an experiment, electrons are made to pass through a narrow slit of width id comparable to their de Broglie

v = 0

d

wavelength. They are detected on a screen at a distance ²D' from the slit (see figure) Which of the following graphs can be expected to represent the number of electrons 'N' detected as a function of the detector position 'y' (y = 0 corresponds to the middle of the slit)?



Sol.: After diffraction electron beam will spread. Correct choice: (2) 94. In the circuit shown, A and B represent two inputs and C represents the output. The circuit represents

- (1) NAND gate (2) OR gate
- (3) NOR gate (4) AND gate



Sol: Correct choice: (2)

95. A thin spherical shell of radius R has charge Q spread uniformly over its surface. Which of the following graphs most closely represents the electric field E(r) produced by the shell in the range $0 \le r < \infty$, where r is the distance from the centre of the shell?



- Sol: For given situation, electric field inside the shell is zero and is inversely proportional to r² for a point outside the shell. Correct choice: (3)
- *9б. A body is at rest at x = 0. At t = 0, it starts moving in the positive x-direction with a constant acceleration. At the same instant another body passes through x = 0 moving in the positive x direction with a company speed. The position of the first body is given by x1(t) after time t and that of the second body by x2(t) after the same time interval. Which of the following graphs correctly describes $(x_1 - x_2)$ as a function of time t?



97. Relative permittivity and parmeability of a material are z and He respectively. Which of the following values of these quantifies are allowed for a diamagnetic material? (1) $\varepsilon_r = 0.5, \mu_r = 0.5$

(2)
$$\varepsilon_r = 1.5$$
, $\mu_r = 1.5$ (3) $\varepsilon_r = 0.5$, $\mu_r = 1.5$ (4) $\varepsilon_r = 1.5$, $\mu_r = 0.5$

Sol: For diamagnetic material, $0 < \mu_r < 1$ and for any material $\varepsilon_r > 1$ Correct choice: (4)

A planet in a distant solar system is 10 times more massive than the earth and its radius is 10 times smaller. Given that the escape velocity from the earth is 11 km s⁻¹, the escape velocity from the surface of the planet would be $(2) 0.11 \text{ km s}^{-1}$ (1) 110 km s⁻¹ $(3) 1.1 \text{ km s}^{-1}$ (4) 11 km s⁻¹

Sol:
$$\frac{V_1}{V_2} = \sqrt{\frac{M_1}{M_2} \times \frac{R_2}{R_1}}$$

 $V_1 = V_2 \sqrt{\frac{M_1}{M_2} \times \frac{R_2}{R_1}} = 11(\text{km/s}) \times \sqrt{10 \times 10} = 110 \text{km/s}$

Correct choice: (1)

*99. A thin rod of length 'L' is lying along the x-axis with its ends at x = 0 and x = L. Its linear density(mass/length) varies with x as $k \left(\frac{x}{L}\right)^n$, where 'n' can be zero or any positive number. If the position x_{CM} of the centre of mass of the rod is plotted against 'n', which of the following graphs best approximates the dependence of x_{CM} on n?



: estimated kinetic energy
$$K = \frac{1}{2}mv^2$$

Let mass of athlete lies between 40 kg and 100 kg

∴ 2000J < K < 5000J

Correct choice: (2)

- *103. A spherical solid ball of volume V is made of a material of density ρ_1 . It is falling through a liquid of density ρ_2 ($\rho_2 < \rho_1$). Assume that the liquid applies a viscous force on the ball that is proportional to the square of its speed ν , i.e. $F_{\text{viscove}} = -k\nu^2 (k > 0)$. The terminal speed of the ball is
 - (1) $\sqrt{\frac{\forall g \rho_1}{k}}$ (2) $\frac{\forall g (\rho_1 \rho_2)}{k}$ (3) $\sqrt{\frac{\forall g (\rho_1 \rho_2)}{k}}$ (4) $\frac{\forall g \rho_1}{k}$
- Sol: The ball will acquire terminal speed in the state of equilibrium
 - $\therefore \quad \nabla \rho_2 g + k \nu^2 \nabla \rho_1 g = 0$ $\nu = \sqrt{\frac{\nabla g (\rho_1 \rho_2)}{\nu}}$

- 104. Shown in the figure is a meter-bridge set up with null deflection in the galvanometer. The value of the unknown resistor R is
 - (1) 110 Ω
 (2) 55 Ω
 - (3) 13.75 Ω (4) 220 Ω
- Sol: For balanced meter bridge (null deflection)
 - $\frac{55}{R} = \frac{20}{80}$
 - R = 220 Ω

(1) 54 > x > 36

Correct choice: (4)

*105. While measuring the speed of sound by performing a resonance column experiment, a student gets the first resonance condition at a column length of 13 cm during winter. Repeating the same experiment during summer, she measures the column length to be x cm for the second resonance. Then

20cm

77777

Sol: $\frac{\nabla}{4\ell} = \frac{3\nabla'}{4x}$ $x = 3\frac{\nabla}{\nabla} = (54\text{ cm})\frac{\nabla'}{\nabla}$ As velocity of sound increases with temperature, $\nabla' > \nabla$ $\therefore x > 54 \text{ cm}$ Correct choice: (4)