

## Today's Plan

- Introduction
- Special Graphs
- Various Representations
- Depth First Search
  - Solve a problem from GCJ
- Breadth First Search
  - Solve a problem from SPOJ
- Dijkstra's Algorithm
  - Solve a problem from SPOJ

# **Special Graphs**

- Undirected Graphs
- Edge Weighted Graphs
- Directed Graphs
- Trees
- Directed Acyclic Graphs
- Bi-Partite Graphs

#### **Representation - I**

- Adjacency matrix
  - 2 D Array **M** of size |V| x |V|
  - **M[i][j]** 1 if Vi and Vj are connected by and edge and 0 otherwise.
- Adjacency List
  - Each vertex maintains a list of vertices that are adjacent to it.
  - We can use: vector< vector<int>>

#### **Representation - II**

- Edge List
- Checking if edge (Vi,Vj) is present in G.
  - Adjacency Matrix O(1)
  - Adjacency List O(min(deg(Vi),deg(Vj)))
- Iterating through the list of neighbours of Vi
  - Adjacency Matrix O(|V|)
  - Adjacency List O(deg(Vi))

### Representation - III

- Implicit graphs
  - Two squares on an 8x8 chessboard. Determine the shortest sequence of knight moves from one square to the other.
- Tricks:
  - Use Dx[] , Dy[] for generating the neighbors of a position in grid problems.

## **Depth First Search**

- Finding Connected Components
- Implemented using
  - Stack
  - Recursion (Most Frequently used)
- Complexity
  - Time: O(|V| + |E|)
  - Space: O(|V|) [to maintain the vertices visited till now]
- Google Code Jam Problem
  - <u>http://code.google.com/codejam/contest/dashboard?c=9010</u> <u>1#s=p1</u>

### **Breadth First Search**

- Finding a Path with Minimum # of edges from starting vertex to any other vertex.
- Used to Solve Shortest Path problem in un weighted graphs
- Implemented using queue
- Same Time and Space Complexity as DFS.
- SPOJ Problem
  - <u>http://www.spoj.pl/problems/PPATH/</u>

## Dijkstra's Algorithm

- Used to solve Shortest Path problem in Weighted Graphs
- Only for Graphs with positive edge weights
- Greedy strategy
- Use priority\_queue<node> for implementing Dijkstra's
- SPOJ Problem
  - <u>http://www.spoj.pl/problems/CHICAGO</u>

### Practice problems

- <u>http://www.spoj.pl/problems/PARADOX/</u>
- <u>http://www.spoj.pl/problems/HERDING/</u>
- <u>http://www.spoj.pl/problems/COMCB/</u>
- http://www.spoj.pl/problems/PT07Y/
- <u>http://www.spoj.pl/problems/PT07Z/</u>

#### **More Practice Problems**

- SRM 453.5 Division 2 500 Pt
- <a href="http://www.codechef.com/problems/N4">http://www.codechef.com/problems/N4</a>
- <a href="http://www.spoj.pl/problems/ONEZERO">http://www.spoj.pl/problems/ONEZERO</a>
- <u>http://www.spoj.pl/problems/CERC07K/</u>