

Jaypee Institute of Information Technology University, Sector 128 – Noida
Test -1(B. tech. first year)

COURSE NAME: MATHEMATICS 1
COURSE CODE: 07B11MA101

MAX. TIME: 1 HR.

MAX. MARKS: 20

Note: Attempt all questions.

Q1. Check whether the limit of the function $f(x,y)$ near point $(0,0)$ exists?

$$f(x,y) = \tan^{-1} \left(\frac{|x| + |y|}{x^2 + y^2} \right)$$

If yes then find the value, otherwise justify.

[4]

Q2. Obtain the second order Taylor series approximation to the function

$$f(x,y) = x^2 - xy + \frac{y^2}{2} + 3$$

about the point $(3,2)$. Calculate the value of the function at $(3.01, 2.01)$ using the series and then compare the value by direct substitution in the function $f(x,y)$. [4]

Q3. Find the absolute maxima or minima of the function

$$f(x,y) = x^2 - xy + y^2 + 1$$

on a closed region in the first quadrant bounded by the lines $x=0$, $y=4$ & $y=x$. [4]

Q4. Sketch the region of the integration for the integral

$$\int_0^2 \int_{x^2}^{2x} (4x + y) dy dx$$

and calculate the integral using change of order of integration. [4]

Q5. Find the area of the region cut from the first quadrant by the Cardioid

$$r = 1 + \sin \theta$$

[4]