WB-JEE - 2013

Answer Keys by

Aakash Institute, Kolkata Centre PHYSICS

MATHEMATICS				
Q.No.	δ	β	γ	μ
01	В	B	B	р А
01	C	C	D	D
03	*	D	B	C
04	В	B	C	A
05	D	A	A	C
06	C	*	A	B
07	A	В	C	*
08	А	В	С	С
09	В	С	A	В
10	D	D	В	Α
11	В	D	Α	D
12	A	D	D	Α
13	С	Α	С	С
14	В	*	В	A
15	В	С	В	D
16	D	А	D	С
17	С	С	A	В
18	В	В	С	В
19	A	A	D	*
20	D	D	B *	C
21	C C	AB	* A	D
22	-			C
23 24	A	A C	A	B
24 25	A B	A	A C	C A
25	D	A D	A	A D
26	C	A	A B	D
27	C	B	B	C
28	C C	C	B	C C
30	B	*	C	D
30	D	A	В	A
32	A	B	*	B
33	c	C	В	A
34	B	D	D	D
35	D	B	B	A
36	A	C	C	В
37	C	A	B	C
38	D	D	D	A
39	*	С	С	В
40	A	С	Α	D
41	A	D	С	С
42	A	D	В	В
43	A	В	С	В
44	С	С	С	В
45	С	Α	С	В
46	D	С	A	С
47	В	D	В	A
48	*	A	D	В
49	A	В	D	С
50	C	A	*	В
51	D	C	A	D
52	D C	B	D	CB
53			A C	
54	D	B A	D	A
55 56	B C	C	C	C
57	В	В	D	*
58	A	C	A	A
59	В	D	c	D
60	B	C	D	D
61	B	D	D	*
62	D	A	A	С
63	A	С	A	A
64	D	*	D	D
65	A	В	D	С
66	С	D	A	Α
67	А	D	*	A
68	D	А	D	D
69	D	А	С	D
70	D	С	D	В
71	A	Α	Α	D
72	D	D	С	A
73	С	D	В	D
74	A	Α	D	D
75	*	D	A	A
76	A,D	B,C	A,B	C,E
77	B,C	A,D	B,C	В,С
78	B,C	A,B	C,D	A,E
79	C,D	B,C	B,C	A,E

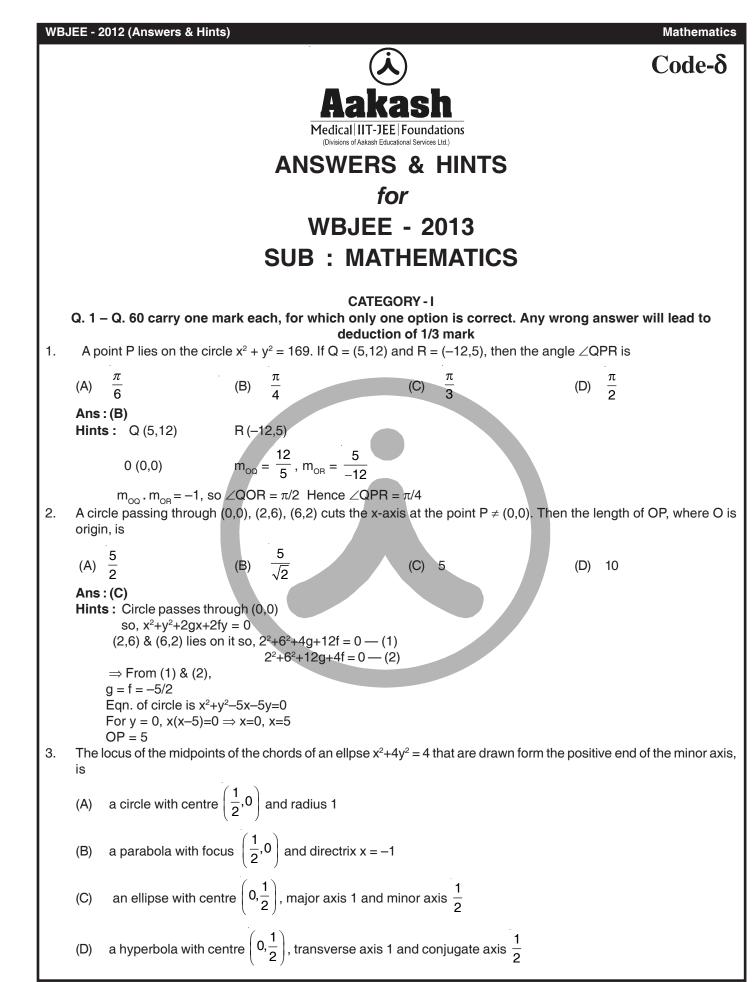
* No Correct Option

PHYSICS				
Q.No.	¢	*	X	*
01	А	D	D	С
02	D	A	С	В
03	D	В	С	D
04	С	D	A	A
05	В	D	В	A*
06	С	В	D	A
07	D	D	A	В
08	Α	В	D	D
09	D	С	С	В
10	В	В	A	A
11	В	Α	D	С
12	D	В	A	С
13	D	D	С	A
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15	В	D	A	D
16	D	D	В	A
17	С	A	С	D
18	С	С	A	С
19	В	В	D	A
20	Α	В	A	C
21	Α	A*	Α	D
22	D	D	В	A
23	В	С	A	В
24	Α	D	D	D
25	D	С	В	A
26	С	С	D	A
27	Α	Α	D	В
28	С	В	В	C
29	D	D	D	C
30	Α	Α	В	D
31	D	D	С	B
32	В	С	В	A
33	Α	Α	Α	D
34	С	D	В	D
35	С	Α	D	В
36	А	С	Α	В
37	В	С	D	D
38	D	A	D	A
39	B	В	A	D
40	A	C	C	C
41	A*	A	B	B
42	A	D	B	C
43	D	A	A*	D
44	B	A	C	D
45	C	В	D	A
46	A	A	A	B
47	A	D	A	B
48	A	A	С	B
49	D	В	D	D
50	C	B	B*	A
51	A	A	A	c
52	D	A	D	C
53	B	c	A	A
54	B*	D	B	A
55	B	B*	B	A
56	A,C,D	B, D	B, C	A,C
57	B,D	В, D А, В, D	A,C,D	A,C A,B
57	B,D B,C	A, D, D A, C, D	A,C,D A,C,D	А, Б
59	A,B,D	A, C, D A, C, D	B, D	в, В,
59 60	А, Б, Б	A, U, D	В, D А, В, D	ь,

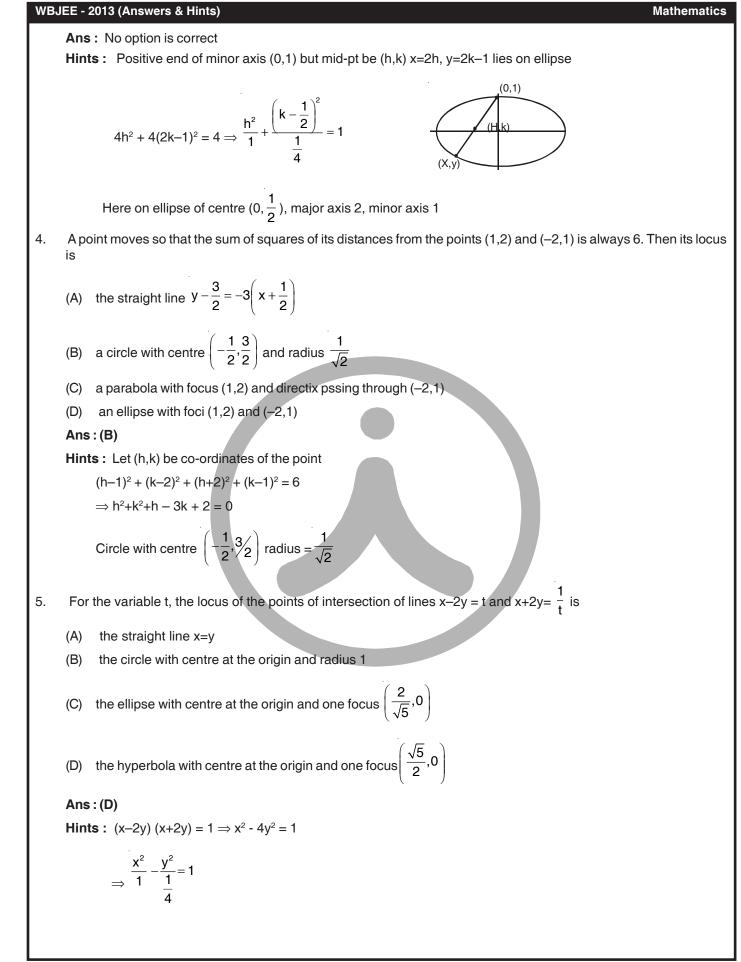
	CHEMISTRY					
Q.No.		•		•		
01	D	С	A	В		
02	С	D	С	С		
03	С	В	С	D		
04	D	С	Α	D		
05	С	D	D	В		
06	С	С	В	D		
07	D	D	D	A		
08	D	D	A	В		
09	С	В	С	A		
10	A	С	D	С		
11	С	D	С	A		
12	B	C	B	C D		
13 14	D	A D	D	D		
14	B	B	C	C		
16	D	D	D	c		
17	A	A	C	D		
18	B	c	В	C		
19	A	c	D	c		
20	C	A	C	D		
21	C	В	C	A		
22	D	С	С	В		
23	A	Α	D	В		
24	В	D	D	С		
25	С	В	Α	A		
26	A	A	С	A		
27	В	С	В	В		
28	В	В	*	A		
29	*	A	D	D		
30	С	С	В	В		
31	D	A	AB	A		
32 33	C B	B	B	D C		
34	A	B	A	c		
35	В	A	A	D		
36	C	В	C	A		
37	A	D	Ă	В		
38	A	*	В	С		
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40	A	С	Α	В		
41	D	A	В	В		
42	В	D	D	*		
43	A	D	Α	С		
44	С	С	С	D		
45	D	С	В	C		
46	В	D	C	A		
47	D A	A	D	B		
48 49	A D	B	A D	B A		
49 50	D	A	B	C		
51	A	B	A	D		
52	B	D	B	B		
53	B	A	B	A		
54	C	D	A	D		
55	A	C	D	D		
56	A, D	A,B,D	A,C,D	A,B,C		
57	A,B,D	A,B,C	B,C	B,C		
58	A,C,D	A,D	A,D	A,B,D		
59	A,B,C	B,C	A,B,C	A,C,D		
60	B,C	A,C,D	A,B,D	A,D		

* No Correct Option





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a = 1, b =
$$\frac{1}{2}$$
 e = $\frac{\sqrt{5}}{2}$ focus $\left(\frac{\sqrt{5}}{2}, 0\right)$

6. Let
$$P = \begin{pmatrix} \cos\frac{\pi}{4} & -\sin\frac{\pi}{4} \\ \sin\frac{\pi}{4} & \cos\frac{\pi}{4} \end{pmatrix}$$
 and $X = \begin{pmatrix} \frac{1}{\sqrt{2}} \\ \frac{1}{\sqrt{2}} \\ \frac{1}{\sqrt{2}} \end{pmatrix}$. Then P³X is equal to

(A)
$$\begin{pmatrix} 0\\1 \end{pmatrix}$$
 (B) $\begin{pmatrix} -1\\\sqrt{2}\\1\\\sqrt{2} \end{pmatrix}$ (C) $\begin{pmatrix} -1\\0 \end{pmatrix}$ (D) $\begin{pmatrix} -\frac{1}{\sqrt{2}}\\-\frac{1}{\sqrt{2}}\end{pmatrix}$

Mathematics

Ans : (C)
Hints :
$$P^{2*}\begin{bmatrix} 0 & -1\\ 1 & 0 \end{bmatrix}$$

 $P^{3} = \begin{bmatrix} -\frac{1}{\sqrt{2}} & -\frac{1}{\sqrt{2}}\\ \frac{1}{\sqrt{2}} & -\frac{1}{\sqrt{2}} \end{bmatrix}$
 $P^{3} \times = \begin{bmatrix} -1\\ 0 \end{bmatrix}$
7. The number of solutions of the equation x+y+z = 10 in positive integers x,y,z is equal to
(A) 36 (B) 55 (C) 72 (D) 45
Ans : (A)
Hints : $^{10-1}C_{3-1} = 9C_{2} = 36$
8. For $0 \le P, Q \le \frac{\pi}{2}$, if sin P + cos Q=2, then the value of tan $\left(\frac{P+Q}{2}\right)$ is equal to
(A) 1 (B) $\frac{1}{\sqrt{2}}$ (C) $\frac{1}{2}$ (D) $\frac{\sqrt{3}}{2}$
Ans : (A)
Hints : $P = \frac{\pi}{2}$, $Q = 0$

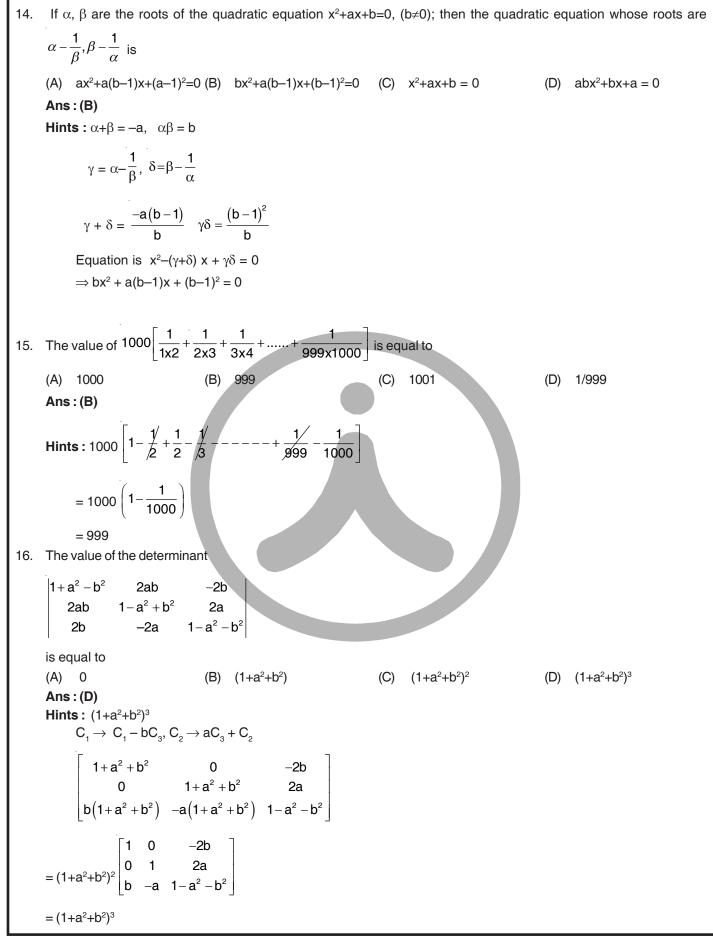
9. If α and β are the roots of $x^2 - x + 1 = 0$, then the value of $\alpha^{2013} + \beta^{2013}$ is equal to

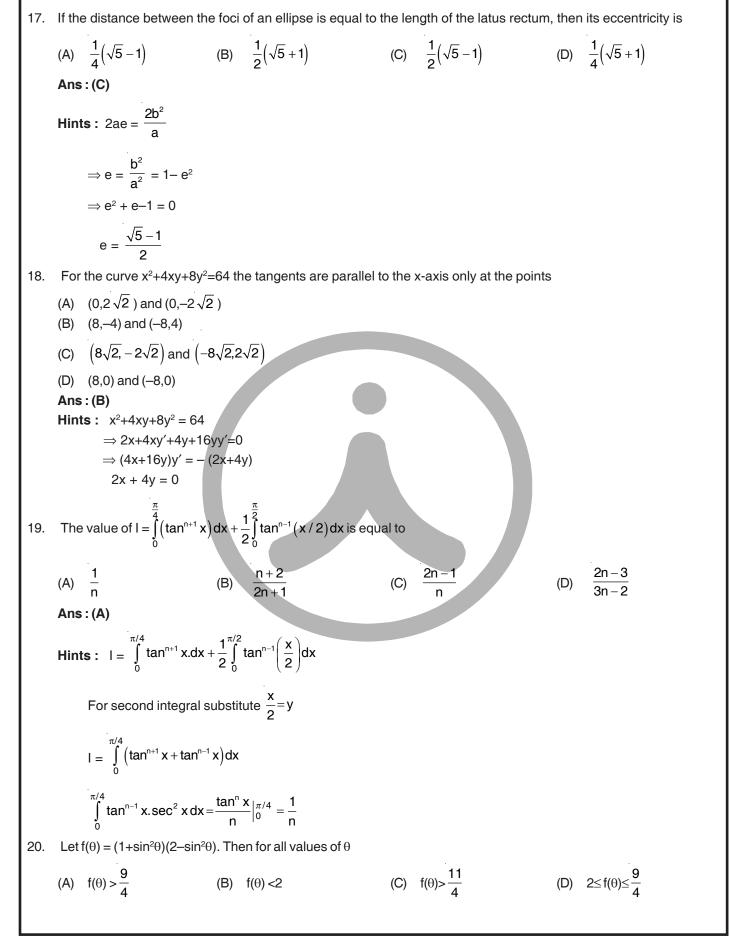
(A) 2 (B) -2 (C) -1 (D) 1
Ans : (B)
Hints :
$$\alpha = -\omega, -\omega^2$$

 $-\omega^{2013} - \omega^{2x2013} = -(\omega^3)^{671} - (\omega^3)^{2x671} = -2$

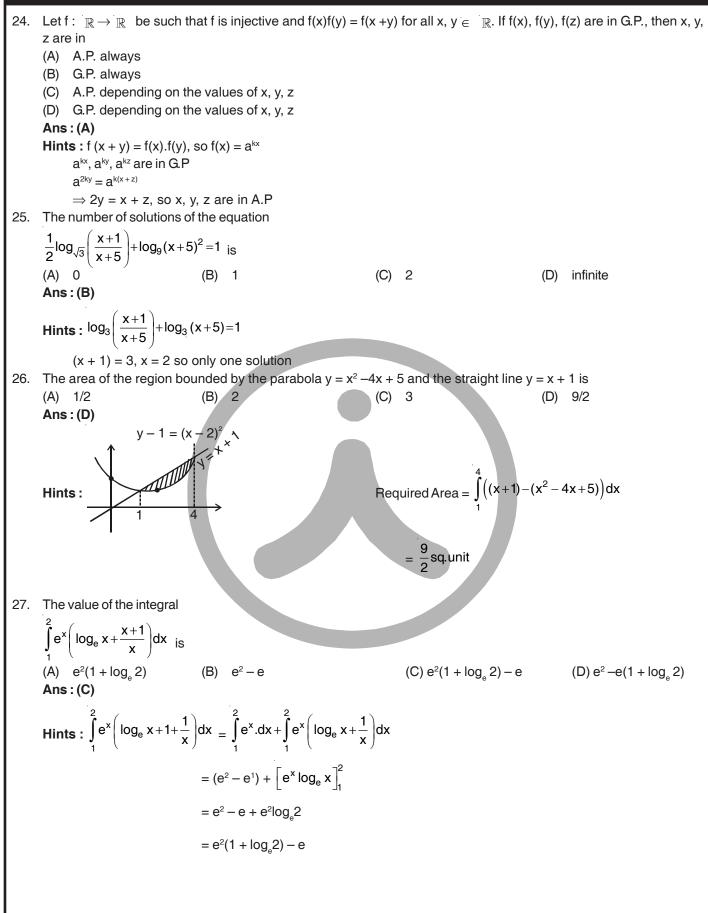
(3)

WB,	JEE - 2013 (Answers & Hints)			Mathematics	
10.	The value of the integral					
	$\int_{-1}^{+1} \left\{ \frac{x^{2013}}{e^{ x } \left(x^2 + \cos x\right)} + \frac{1}{e^{ x }} \right\} c$	дх				
	is equal to					
	(A) 0	(B) 1-e ⁻¹	(C) 2 e ⁻¹	(D) $2(1-e^{-1})$		
	Ans : (D)					
	Hints: $\frac{x^{2013}}{e^{ x }(x^2 + \cos x)}$ is c	odd				
	$I = \int_{-1}^{1} \frac{1}{e^{ x }} dx = 2 \int_{0}^{1} e^{-x}$	x dx=2(1-e ⁻¹)				
11.	Let					
	$f(x) = 2^{100} x + 1,$					
	$g(x) = 3^{100} x + 1.$					
		ers x such that $f(g(x)) = x$ is				
	(A) empty	(B) a singleton	(C) a finite set with more	than one element		
	(D) infinite					
	Ans:(B) Hints: f(x) = 2 ¹⁰⁰ x+1;g($(x) - 3^{100} x + 1$				
12.	$f\left(g(x)\right)=x \Longrightarrow x=$ The limit of $x \sin(e^{1/x})$ as x	$ -\frac{\left(1+2^{100}\right)}{6^{100}-1} $ $ \rightarrow 0 $				
	(A) is equal to 0	(B) is equal to 1	(C) is equal to e/2	(D) does not e	exist	
	Ans : (A) Hints : $-1 \le sine^{1/x} \le 1, -x \le x$	$x\sin(e^{1/x}) < x$				
	$\lim_{x \to 0} x \sin(e^{1/x}) = \lim_{x \to 0} x = 0,$					
13.	Let I = $\begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix}$ and P =	$\begin{bmatrix} 1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & -2 \end{bmatrix}$. Then the mat	rix P ³ +2P ² is equal to			
	(A) P	(B) I–P	(C) 2I+P	(D) 2I–P		
	Ans:(C)					
	Hints : $ \mathbf{P} - \lambda \mathbf{I} = 0$, characteristics equation of P is P ³ +2P ² -P-2I = 0					
	P ³ +2P ² =P+2I					

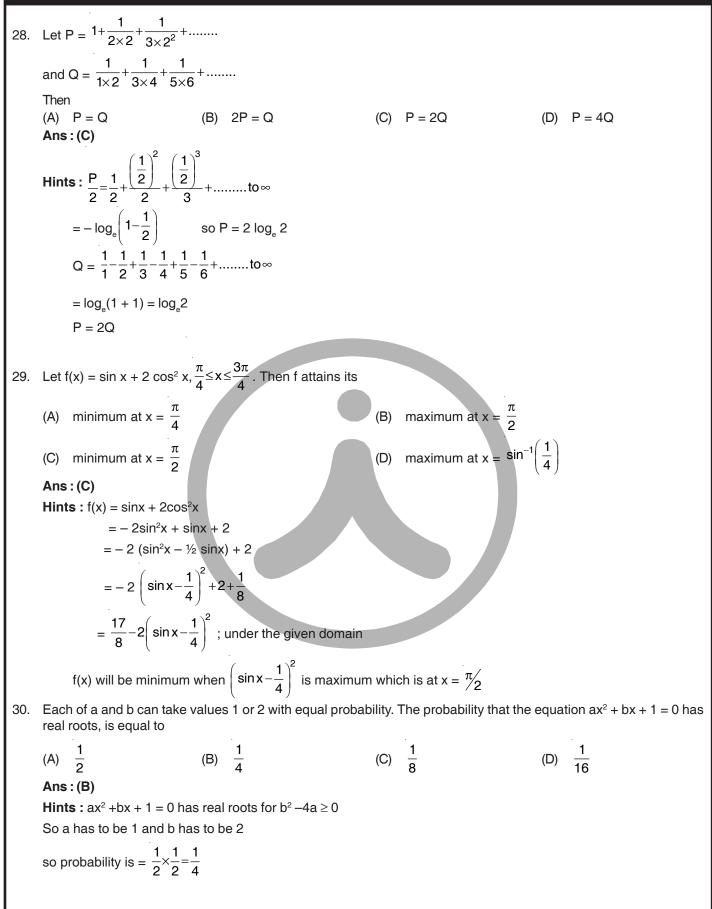


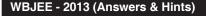


WBJEE - 2013 (Answers & Hints) Mathematics Ans:(D) **Hints**: $f(\theta) = (1 + \sin^2\theta) (2 - \sin^2\theta)$ $f(\theta) = (1 + \sin^2\theta)(1 + \cos^2\theta)$ $=2+\sin^2\theta\cos^2\theta$ $=2+\frac{1}{4}\sin^2\theta$ $2 \le f(\theta) \le \frac{9}{4}$ 21. Let $f(x) = \begin{cases} x^3 - 3x + 2, & x < 2 \\ x^3 - 6x^2 + 9x + 2, & x \ge 2 \end{cases}$ Then (A) $\lim_{x\to 2} f(x)$ does not exist (B) f is not continuous at x = 2(C) f is continuous but not differentiable at x = 2(D) f is continuous and differentiable at x = 2Ans : (C) Hints : $\lim_{x \to 2^+} f(x) = 4$ $\lim_{x\to 2^-} f(x) = 4$ $f'(x) = \begin{cases} 3x^2 - 3, & x < 2\\ 3x^2 - 12x + 9, & x \ge 2 \end{cases}$ so L.H.D at x = 2 is 9, R.H.D at x = 2 is -3so f(x) is continuous but not differentiable at x = 222. The limit of $\sum_{n=1}^{1000} (-1)^n x^n$ as $x \to \infty$ (B) exists and equals to 0 (C) exists and approaches $+\infty$ (D) exists and ap-(A) does not exist Ans : (C) Hints: $\lim_{x\to\infty} (-x + x^2 - x^3 + x^4 \dots + x^{1000})$ $= \lim_{x \to \infty} (-x) \cdot \frac{((-x)^{1000} - 1)}{-x - 1} = \lim_{x \to \infty} \frac{x^{1001} - x}{x + 1} = +\infty$ 23. If $f(x) = e^x (x-2)^2$ then (A) f is increasing in $(-\infty, 0)$ and $(2, \infty)$ and decreasing in (0, 2)(B) f is increasing in $(-\infty, 0)$ and decreasing in $(0, \infty)$ (C) f is increasing in $(2,\infty)$ and decreasing in $(-\infty,0)$ (D) f is increasing in (0, 2) and decreasing in $(-\infty, 0)$ and $(2, \infty)$ Ans:(A) **Hints**: $f'(x) = e^{x} [(x-2)^{2} + 2(x-2)]$ $= e^{x} [x^{2} - 2x] = e^{x} . x(x - 2)$ sign scheme of f'(x) will be $\frac{+}{0}$ - $\frac{/+}{2}$ so f is increasing in $(-\infty, 0)$ and $(2, \infty)$ and decreasing in (0, 2)

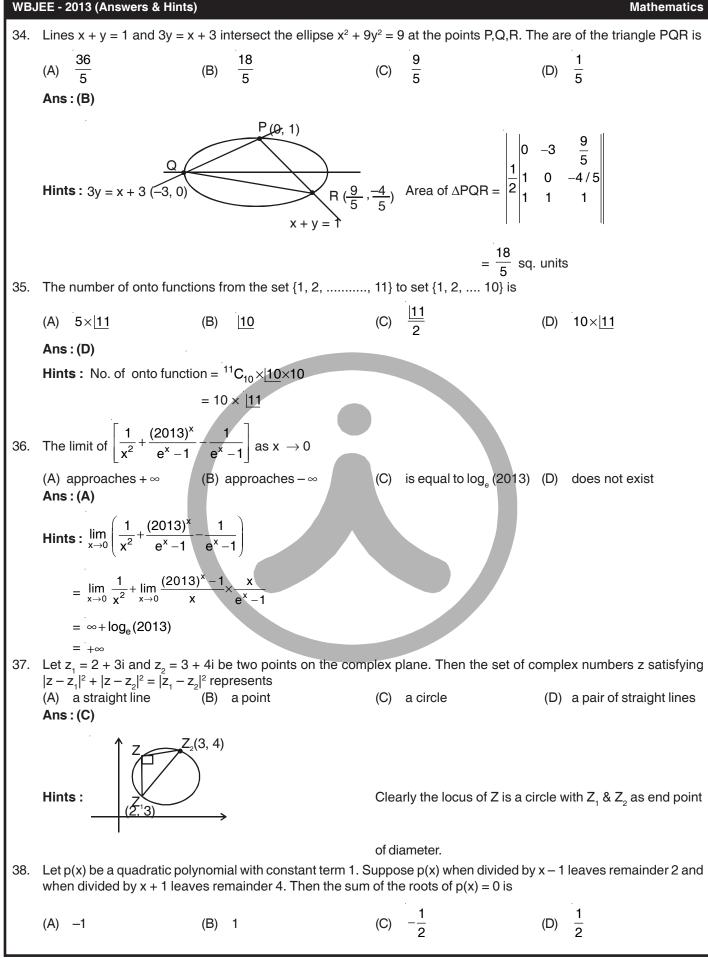


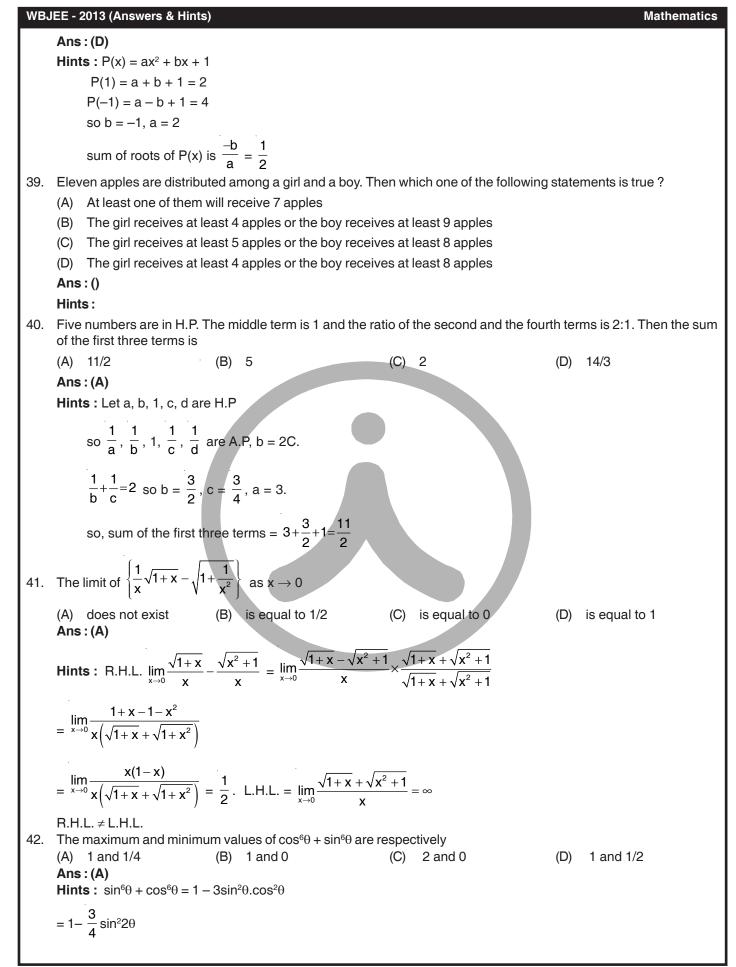






З 31. There are two coins, one unbiased with probability $\frac{1}{2}$ of getting heads and the other one is biased with probability of getting heads. A coin is selected at random and tossed. It shows heads up. Then the probability that the unbiased coin was selected is 2 5 2 (C) $\frac{1}{2}$ (A) (D) (B) 3 Ans:(D) **Hints** : $H \rightarrow$ Event of head showing up $B \rightarrow$ Event of biased coin chosen $UB \rightarrow Event of unbiased coin chosen$ $P\left(\frac{UB}{H}\right) = \frac{P(UB).P\left(\frac{H}{UB}\right)}{P(UB).P\left(\frac{H}{UB}\right) + P(B).P\left(\frac{H}{B}\right)}$ $\frac{\frac{1}{2} \times \frac{1}{2}}{\frac{1}{2} \times \frac{1}{2} + \frac{1}{2} \times \frac{3}{4}} = \frac{2}{5}$ For the variable t, the locus of the point of intersection of the lines 3tx - 2y + 6t = 0 and 3x + 2ty - 6 = 0 is 32. (A) the ellipse $\frac{x^2}{4} + \frac{y^2}{9} = 1$ (B) the ellipse $\frac{x^2}{9} + \frac{y^2}{4} = 1$ (D) the hyperbola $\frac{x^2}{9} - \frac{y^2}{4} = 1$ (C) the hyperbola $\frac{x^2}{4} - \frac{y^2}{9} = 1$ Ans:(A) Hints : The point of intersection of 3tx - 2y + 6t = 0 and 3x + 2ty - 6 = 0 is $x = \frac{2(1-t^2)}{(1+t^2)}, y = \frac{6t}{(1+t^2)}$ Considering t = tan θ , x = 2cos 2 θ , y = 3.sin 2 θ so locus of point of intersection is the ellipse $\frac{x^2}{4} + \frac{y^2}{9} = 1$ 33. Cards are drawn one-by-one without replacement from a well shuffled pack of 52 cards. Then the probability that a face card (Jack, Queen or King) will appear for the first time on the third turn is equal to $\frac{36}{85}$ (C) $\frac{12}{85}$ 300 $\frac{4}{51}$ (B) (D) (A) 2197 Ans : (C) Hints: P (face card on third turn) = P (no face card in first turn) × P (no face card in 2nd turn) × P (face card in 3rd turn) $= \frac{40}{52} \times \frac{39}{51} \times \frac{12}{50} = \frac{12}{85}$





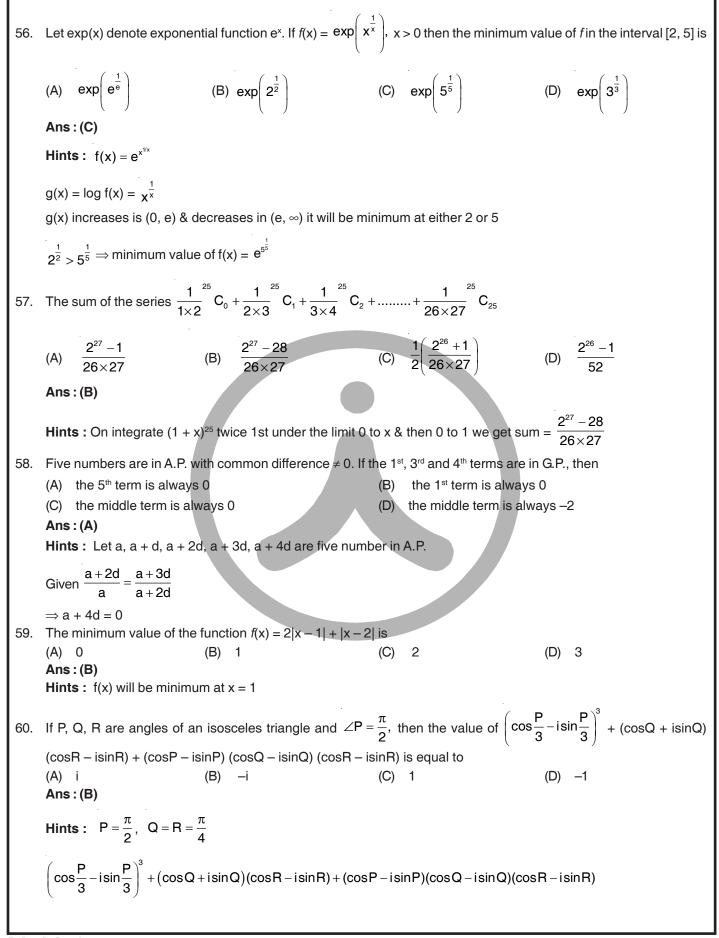
Mathematics

43. If a, b, c are in A.P., then the straight line ax + 2by + c = 0 will always pass through a fixed point whose co-ordinates are (A) (1,−1) (B) (-1, 1) (C) (1,−2) (D) (-2, 1) Ans:(A) **Hints** : a(x + y) + c(y + 1) = 0x = 1, y = -144. If one end of a diameter of the circle $3x^2 + 3y^2 - 9x + 6y + 5 = 0$ is (1, 2) then the other end is (C) (2, -4) (D) (-4, 2) (A) (2, 1) (B) (2,4) Ans : (C) **Hints** : Center $\left(\frac{3}{2}, -1\right)$ Let the other point be (h, k) $\frac{h+1}{2} = \frac{3}{2} \Longrightarrow h = 2$ $\frac{k+2}{2} = -1 \Longrightarrow k = -4$ 45. The value of $\cos^2 75^\circ + \cos^2 45^\circ + \cos^2 15^\circ - \cos^2 30^\circ - \cos^2 60^\circ$ is (A) 0 · (B) 1 1/2 1/4 (C) (D) Ans:(C) Hints : $cos15^{\circ} = sin75^{\circ}$ $\cos^2 75^\circ + \cos^2 45^\circ + \cos^2 15^\circ - \cos^2 30^\circ - \cos^2 60^\circ$ $=\cos^2 75^\circ + \sin^2 75^\circ + \cos^2 45^\circ - \cos^2 30^\circ - \cos^2 60^\circ$ $= 1 + \frac{1}{2} - \frac{3}{4} - \frac{1}{4}$ $=\frac{1}{2}$ 46. Suppose z = x + iy where x and y are real numbers and $i = \sqrt{-1}$. The points (x, y) for which $\frac{z-1}{z-i}$ is real, lie on (A) an ellipse (B) a circle (C) a parabola (D) a straight line Ans:(D) Hints: $\frac{(x-1) + iy}{x + i(y-1)} = k$ $\Rightarrow \frac{(x-1)+iy}{x+i(y-1)} \times \frac{x-i(y-1)}{x-i(y-1)} = k$ \Rightarrow Imaginary part = 0 \Rightarrow x + y = 1 47. The equation $2x^2 + 5xy - 12y^2 = 0$ represents a (A) circle (B) pair of non-perpendicular intersecting straight lines (C) pair of perpendicular straight lines (D) hyperbola Ans:(B) **Hints**: $2x^2 + 5xy - 12y^2 = 0$ (x + 4y) (2x - 3y) = 0

48.	The line y = x intersects the hyperbola $\frac{x^2}{9} - \frac{y^2}{25} = 1$ at the points P and Q. The eccentricity of ellipse with PQ as major					
	axis and minor axis of length $\frac{5}{\sqrt{2}}$ is					
	(A) $\frac{\sqrt{5}}{3}$ (B) $\frac{5}{\sqrt{3}}$ (C) $\frac{5}{9}$ (D) $\frac{25}{9}$					
	Ans : ()					
	Hints : For $y = x$, $x^2 \left(\frac{1}{9} - \frac{1}{25}\right) = 1 \implies x^2 = \left(\frac{5 \times 3}{4}\right)^2 = \left(\frac{15}{4}\right)^2$					
	$\Rightarrow a = \frac{15\sqrt{2}}{4} = \frac{15}{2\sqrt{2}}, b = \frac{5}{2\sqrt{2}}$					
	$e^2 = 1 - \frac{1}{9} = \frac{8}{9}$					
	$e = \frac{2\sqrt{2}}{3}$					
49.	The equation of the circle passing through the point (1, 1) and the points of intersection of $x^2 + y^2 - 6x - 8 = 0$ and $x^2 + y^2 - 6 = 0$ is					
	(A) $x^2 + y^2 + 3x - 5 = 0$ (B) $x^2 + y^2 - 4x + 2 = 0$ (C) $x^2 + y^2 + 6x - 4 = 0$ (D) $x^2 + y^2 - 4y - 2 = 0$					
	Ans : (A) Hints : Circle passing through point of intersection of circles is $x^2 + y^2 - 6x - 8 + \lambda (x^2 + y^2 - 6) = 0$					
	It passes through (1, 1) so, $\lambda = -3$					
	Circle is $x^2 + y^2 + 3x - 5 = 0$					
50.	Six positive numbers are in G.P., such that their product is 1000. If the fourth term is 1, then the last term is (A) 1000 (B) 100 (C) 1/100 (D) 1/1000					
	Ans: (C)					
	Hints: $\frac{a}{r^5}, \frac{a}{r^3}, \frac{a}{r}, ar, ar^3, ar^5$					
	$a^6 = 1000 \Rightarrow a^2 = 10$					
	given ar = 1, $\Rightarrow a^2 r^2 = 1$, $r^2 = \frac{1}{10}$					
	$ar^5 = \frac{1}{100}$					
51.	In the set of all 3×3 real matrices a relation is defined as follows. A matrix A is related to a matrix B if and only if there is a non-singular 3×3 matrix P such that $B = P^{-1}AP$. This relation is (A) Reflexive, Symmetric but not Transitive (B) Reflexive, Transitive but not Symmetric (C) Symmetric, Transitive but not Reflexive (D) an Equivalence relation Ans : (D) Hints : $R = \{(A, B) B = P^{-1}AP\}$ $A = I^{-1}AI \Rightarrow (A, A) \in R \Rightarrow R$ is reflexive Let $(A, B) \in R$, $B = P^{-1}AP$ $PB = AP \Rightarrow PBP^{-1} = A \Rightarrow A = (P^{-1})^{-1} B(P^{-1})$					
1						

WBJEE - 2013 (Answers & Hints) Mathematics \Rightarrow (B, A) \in R, \Rightarrow R is symmetric Let $(A, B) \in R$, $(B, C) \in R$ $A = P^{-1}BP$ and $B = Q^{-1}CQ$ $A = P^{-1}Q^{-1}C QP = (QP)^{-1} C(QP) \Longrightarrow (A, C) \in R$ 52. The number of lines which pass through the point (2, -3) and are at the distance 8 from the point (-1, 2) is (A) infinite (B) 4 (C) 2 (D) 0 Ans:(D) **Hints**: The maximum distance of the line passing through (2, -3) from (-1, 2) is $\sqrt{34}$. So there is no possible line 53. If α , β are the roots of the quadratic equation $ax^2 + bx + c = 0$ and $3b^2 = 16ac$ then (A) $\alpha = 4\beta$ or $\beta = 4\alpha$ (B) $\alpha = -4\beta$ or $\beta = -4\alpha$ (D) $\alpha = -3\beta$ or $\beta = -3\alpha$ (C) $\alpha = 3\beta \text{ or } \beta = 3\alpha$ Ans:(C) Hints: 3b2 = 16ac $\Rightarrow 3\left(\frac{b}{a}\right)^2 = 16\frac{c}{a}$ $3(\alpha + \beta)^2 = 16\alpha\beta$, $3\alpha^2 + 3\beta^2 = 10\alpha\beta$ $3\frac{\alpha}{\beta} + 3\frac{\beta}{\alpha} = 10$, Let $\frac{\alpha}{\beta} = y$ $3y^2 - 10y + 3 = 0$, $\Rightarrow (3y - 1) (y - 3) = 0$ $y = \frac{1}{3}$ or y = 3 \Rightarrow 3 α = β or α = 3 β 54. For any two real numbers a and b, we define a R b if and only if $\sin^2 a + \cos^2 b = 1$. The relation R is (A) Reflexive but not Symmetric (B) Symmetric but not transitive (C) Transitive but not Reflexive (D) an Equivalence relation Ans:(D) Hints : $sin^2a + cos^2b = 1$ Reflexive : $\sin^2 a + \cos^2 a = 1$ ⇒aRa $\sin^2 a + \cos^2 b = 1$, $1 - \cos^2 a + 1 - \sin^2 b = 1$ $sin^{2}b + cos^{2}a = 1$ ⇒bRa Hence symmetric Let aRb, bRc $sin^2a + cos^2b = 1$ (1) $sin^{2}b + cos^{2}c = 1$ (2) (1) + (2) $sin^2a + cos^2c = 1$ Hence transitive therefore equivalence relation. 55. Let n be a positive even integer. The ratio of the largest coefficient and the 2nd largest coefficient in the expansion of $(1 + x)^n$ is 11:10. The the number of terms in the expansion of $(1 + x)^n$ is (A) 20 (B) 21 (C) 10 (D) 11 Ans:(B) Hints: Let n = 2m $\Rightarrow \frac{{}^{2m}C_m}{{}^{2m}C_{m-1}} = \frac{11}{10}$ \Rightarrow m = 10, n = 20 Total No. of term = 21

Mathematics



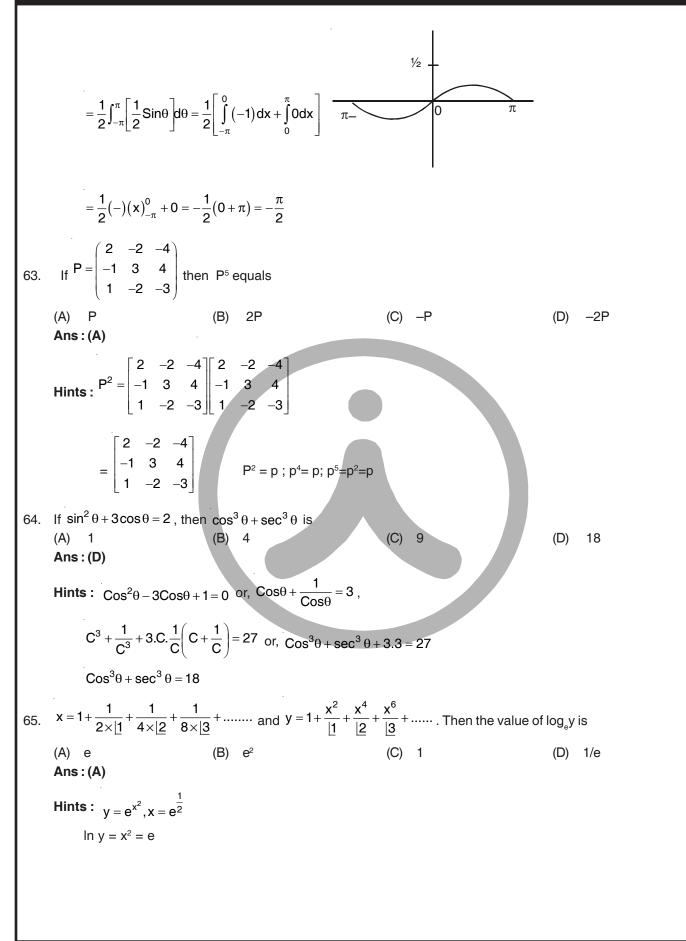
$$= e^{-\psi} + e^{0} e^{-\pi} + e^{-\pi} \times e^{-\pi} \times e^{-\pi} \times e^{-\pi} \times e^{-\pi} = e^{-\pi/2} + e^{(1)(2-\pi)} + e^{-(1)(2-\pi)} + e^{-(1)(2-\pi)} + e^{-(1)(2-\pi)} = e^{-\pi/2} + e^{0} + e^{-\pi} = \left[\left(\cos \frac{\pi}{2} - 1\sin \frac{\pi}{2} \right) + 1 + \left(\cos \pi - 1\sin \pi \right) = -1 + 1 - 1 - 0 = -1 \right]$$

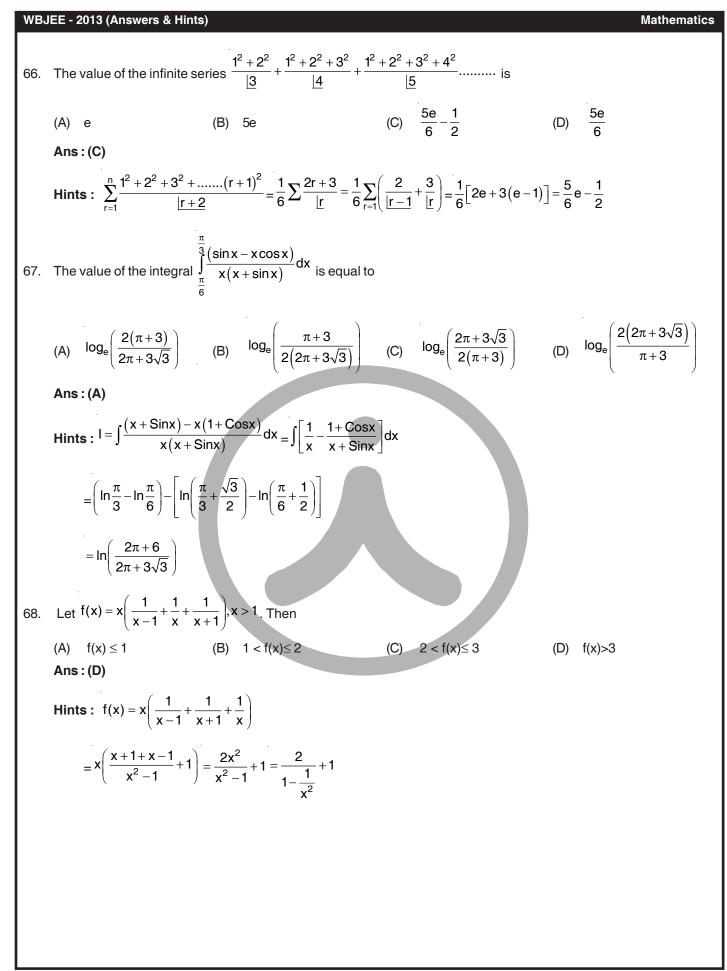
CATEGORY - II
0. 61 - 0. 75 carry two marks each, for which only option is correct. Any wrong answer will lead to deduction of 2/3 mark.
61. A line passing through the point of intersection of x + y = 4 and x - y = 2 makes an angle tan ''(3/4) with the x-axis. It intersects the parabola y² = 4(x-3) at points (x, y, y) and (x, y, y) and (x, y, y) are lower will lead '' = 0.
61. A line passing through the point of intersection of x + y = 4 and x - y = 2 makes an angle tan ''(3/4) with the x-axis. It intersects the parabola y² = 4(x-3) at points (x, y, y) and (x, y, y) and (x, y, y) are lower will lead '' = 0.
61. A line passing through the point of intersection of x + y = 4 and x - y = 2 makes an angle tan ''(3/4) with the x-axis. It intersects the parabola y² = 4(x-3) at points (x, y, y) and (x, y, y) and (x, y, y) are lower will lead '' = 0.
61. A line passing through the point of intersection of x + y = 4 and x - y = 2 makes an angle tan ''(3/4) with the x-axis. It intersects the parabola y² = 4(x-3) or, 'y = \frac{3}{9} = \frac{3}{9} = \frac{2}{9} = \frac{3}{9} = \frac{2}{9} = \frac{3}{9} = \frac{2}{9} = \frac{2}{9}

Hints:
$$I = \int_{-\frac{\pi}{2}}^{\frac{\pi}{2}} \left[\frac{1}{2}\sin 2x\right] dx$$
 Put $2x = \theta$ or, $2dx = d\theta$

(17)

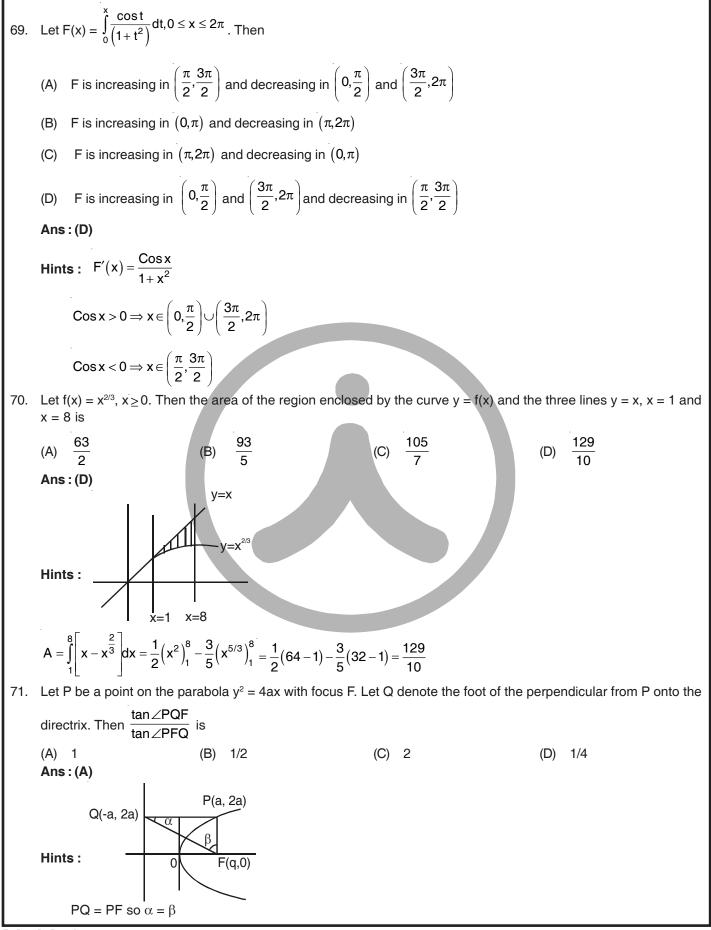
Mathematics



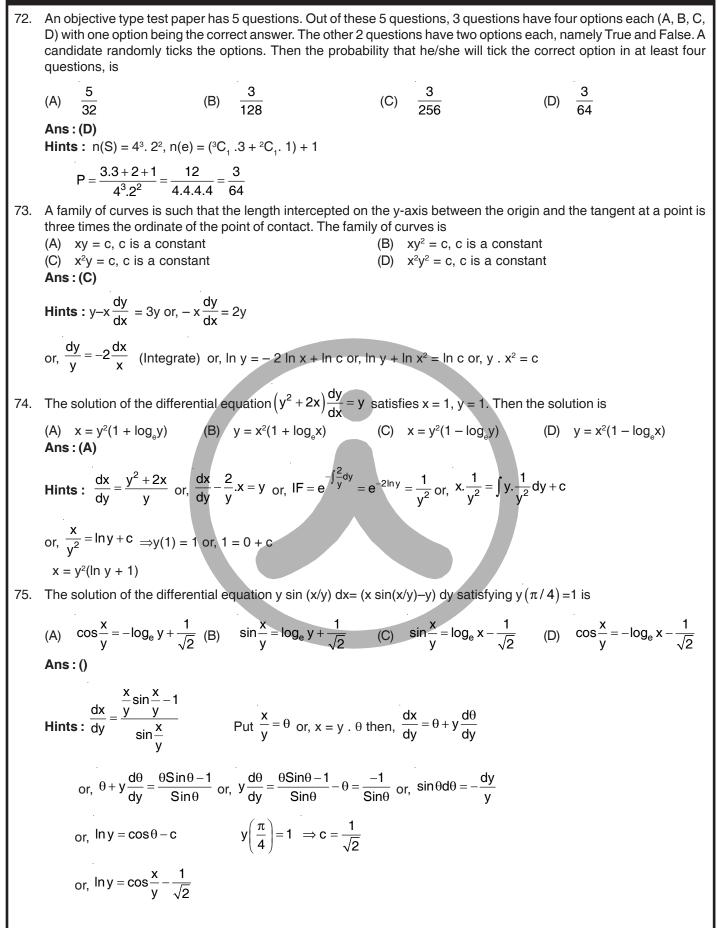


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Mathematics

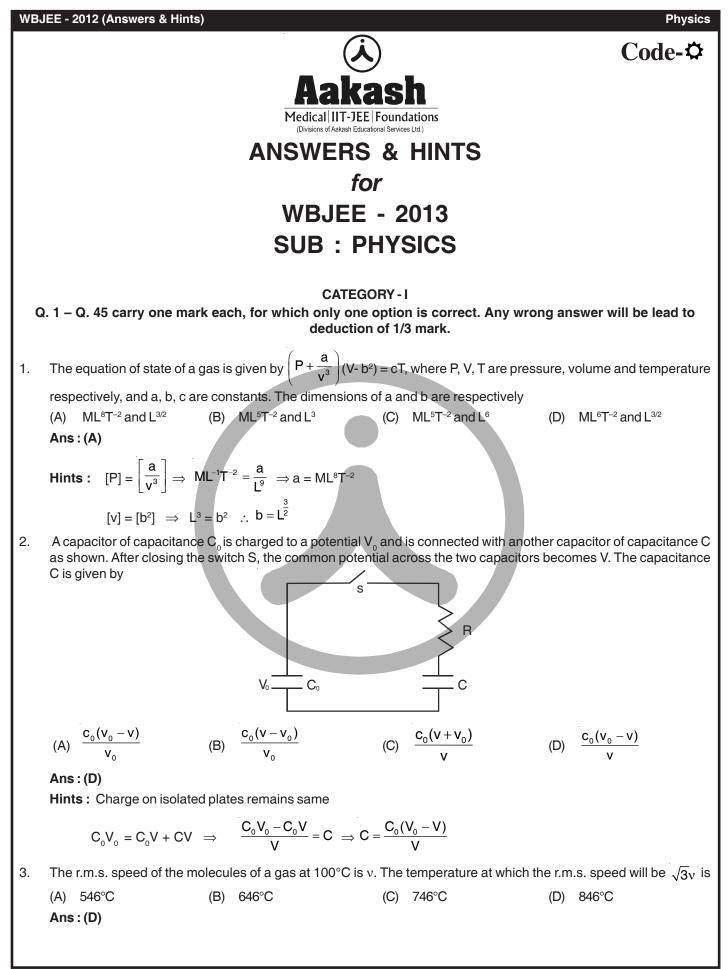


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CATEGORY-3

Q. 76 – Q. 80 carry two marks each, for which one or more than one options may be correct. Marking of correct options will lead to a maximum mark of two on pro rata basis. There will be no negative marking for these questions. However, any marking of wrong option will lead to award of zero mark against the respective question –irrespective of the number of correct options marked 76. The area of the region enclosed between parabola $y^2 = x$ and the line y = mx is $\frac{1}{48}$. Then the value of m is (A) -2 (B) -1 (C) 1 (D) 2 Ans : (A, D) Hints: . $A = \int_{-\infty}^{\frac{1}{m}} \left(\frac{y}{m} - y^2\right) dy = \left|\frac{1}{2m} \left(y^2\right)_0^{1/m} - \frac{1}{3} \left(y^3\right)_0^{\frac{1}{m}}\right|$ $\frac{1}{48} = \left| \frac{1}{2m^3} - \frac{1}{3m^3} \right|$ or, $\frac{1}{48} = \left| \frac{1}{6m^3} \right|$ (1) $m^3 = \frac{1}{6}.48 = 1.8 = 8 \text{ or}, m = 2$ (2) $m^3 = -\frac{1}{6}.48 = -1.8 \text{ or}, m = -2$ 77. Consider the system of equations: x + y + z= 0 $\alpha \mathbf{x} + \beta \mathbf{y} + \gamma \mathbf{z}$ = 0 $\alpha^2 \mathbf{x} + \beta^2 \mathbf{y} + \gamma^2 \mathbf{z}$ = 0 Then the system of equations has (A) A unique solution for all values α , β , γ (B) Infinite number of solutions if any two of α , β , γ are equal (C) A unique solution if α , β , γ are distinct (D) More than one, but finite number of solutions depending on values of α , β , γ Ans : (B, C) Hints: $\begin{vmatrix} 1 & 1 & 1 \\ \alpha & \beta & \gamma \\ \alpha^2 & \beta^2 & \gamma^2 \end{vmatrix} = (\alpha - \beta)(\beta - \gamma)(\gamma - \alpha)$ 78. The equations of the circles which touch both the axes and the line 4x + 3y = 12 and have centres in the first quadrant, are (A) $x^2 + y^2 - x - y + 1 = 0$ (B) $x^2 + y^2 - 2x - 2y + 1 = 0$ (D) $x^2 + y^2 - 6x - 6y + 36 = 0$ (C) $x^2 + y^2 - 12x - 12y + 36=0$ Ans: (B, C) Hints: $\left|\frac{4h+3h-12}{5}\right| = h$ or, |7h-12| = 5h(i) 7h - 12 = 5h or, 2h = 12 or, h = 6 Centre (6, 6) $x^{2} + y^{2} - 12x - 12y + 36 = 0$ (ii) 7h - 12 = -5h or, h = 1(1, 1) or, r = 179. Which of the following real valued functions is/are not even functions? (A) $f(x) = x^3 \sin x$ (B) $f(x) = x^2 \cos x$ (C) $f(x) = e^x x^3 \sin x$ (D) f(x) = x-[x], where [x] denotes the greatest integer less than or equal to x

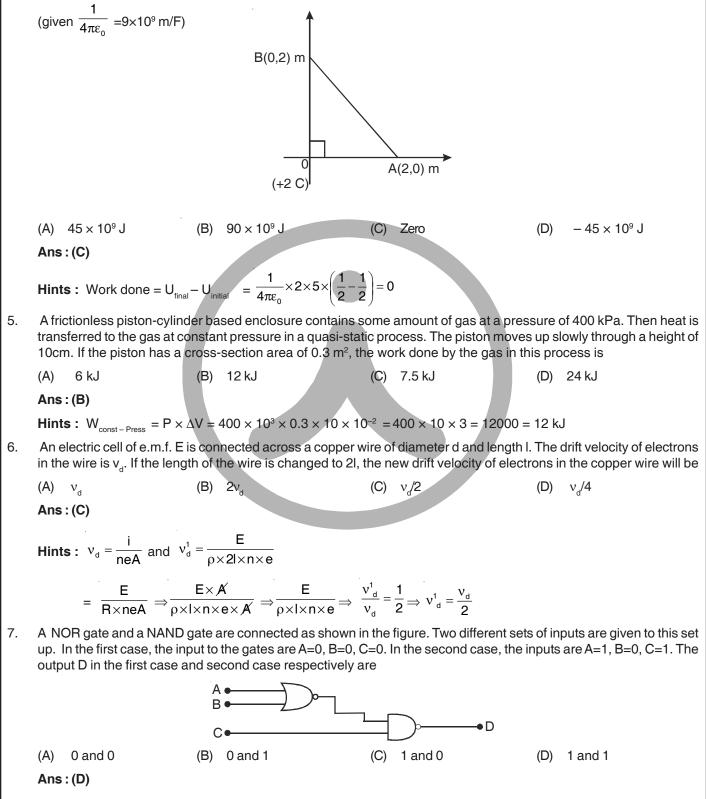
WB	JEE - 2013 (Answers	& Hints)			Mathematics
	Ans : (C, D)				
	Hints : (A) $f(-x) =$	f(x) even	(B) f((-x) = f(x) even	
	(C) $f(-x) \neq f(x)$ r	ot even	(D) f((−x) ≠ f(x) not even	
80.	Let sin α , cos α be	the roots of the equation x^2 -	-bx + c= 0. Then w	which of the following	statements is/are correct?
	$(A) c \leq \frac{1}{2}$	(B) $b \leq \sqrt{2}$	(C) C	$2 > \frac{1}{2}$	(D) $b > \sqrt{2}$
	Ans : (A, B)				
	Hints : Sin α + Cos	$\mathbf{s}\alpha = \mathbf{b}, \mathbf{Sin}\alpha.\mathbf{Cos}\alpha = \mathbf{c}$			
	$b \leq \sqrt{2}$,	$c = \frac{1}{2}sin2\alpha$			
	·	$c \leq \frac{1}{2}$			
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Hints:
$$V_{\text{rms}} = \sqrt{\frac{3\text{RT}}{M}} \Rightarrow V = \sqrt{\frac{3\text{R} \times 373}{M}} \Rightarrow \sqrt{3}V = \sqrt{\frac{3\text{R} \times T}{M}} \Rightarrow \sqrt{3} = \sqrt{\frac{1}{373}} \Rightarrow 3 = \frac{1}{373} \Rightarrow 1 = 3 \times 373 = 1119\text{K}$$

T (°C) = 846°C

4. As shown in the figure below, a charge +2C is situated at the origin O and another charge +5C is on the x-axis at the point A. The later charge from the point A is then brought to a point B on the y-axis. The work done is



	A bar magnet has a magnetic moment of 200 A.m ² . The magnet is suspended in a magnetic field of 0.30 NA ⁻¹ m ⁻¹ . The torque required to rotate the magnet from its equilibrium position through an angle of 30°, will be					
	(A) 30 N m (B) $30 \sqrt{3} \text{ N m}$ (C) 60 N m (D) $60 \sqrt{3} \text{ N m}$					
	Ans:(A)					
	Hints : $\vec{T} = \vec{M} \times \vec{B} \implies \vec{T} = M \times B \times \sin \theta = 200 \times 0.3 \times \frac{1}{2} = 100 \times 0.3 = 30 \text{ Nm}$					
9.	Two soap bubbles of radii r and 2r are connected by a capillary tube-valve arrangement as shown in the diagram. The valve is now opened. Then which one of the following will result:					
	Valve					
	(A) the radii of the bubbles will remain unchanged					
	(B) the bubbles will have equal radii					
	(C) The radius of the smaller bubble will increase and that of the bigger bubble will decrease					
	(D) The radius of the smaller bubble will decrease and that of the bigger bubble will increase					
	Ans : (D)					
	Hints : Pressure – Difference = $\frac{4T}{r}$					
	For smaller soap $P_{atm} - P_{it} = \frac{4T}{r}$					
	For bigger soap $P_{atm} - P_{i2} = \frac{4T}{2r}$					
	As pressure inside smaller bubble is greater than pressure inside bigger bubble . so air flows from smaller to bigger					
10.	An ideal mono-atomic gas of given mass is heated at constant pressure. In this process, the fraction of supplied heat energy used for the increase of the internal energy of the gas is					
	(A) 3/8 (B) 3/5 (C) 3/4 (D) 2/5					
	Ans:(B)					
	Hints : Fraction = $\frac{\Delta U}{\Delta Q} = \frac{C_v}{C_P} = \frac{1}{\Upsilon} = \frac{3}{5}$					
11.	The velocity of a car travelling on a straight road is 36 kmh ⁻¹ at an instant of time. Now travelling with uniform acceleration for 10 s, the velocity becomes exactly double. If the wheel radius of the car is 25 cm, then which of the following numbers is the closest to the number of revolutions that the wheel makes during this 10 s?					
	(A) 84 (B) 95 (C) 126 (D) 135					
	Ans:(B)					

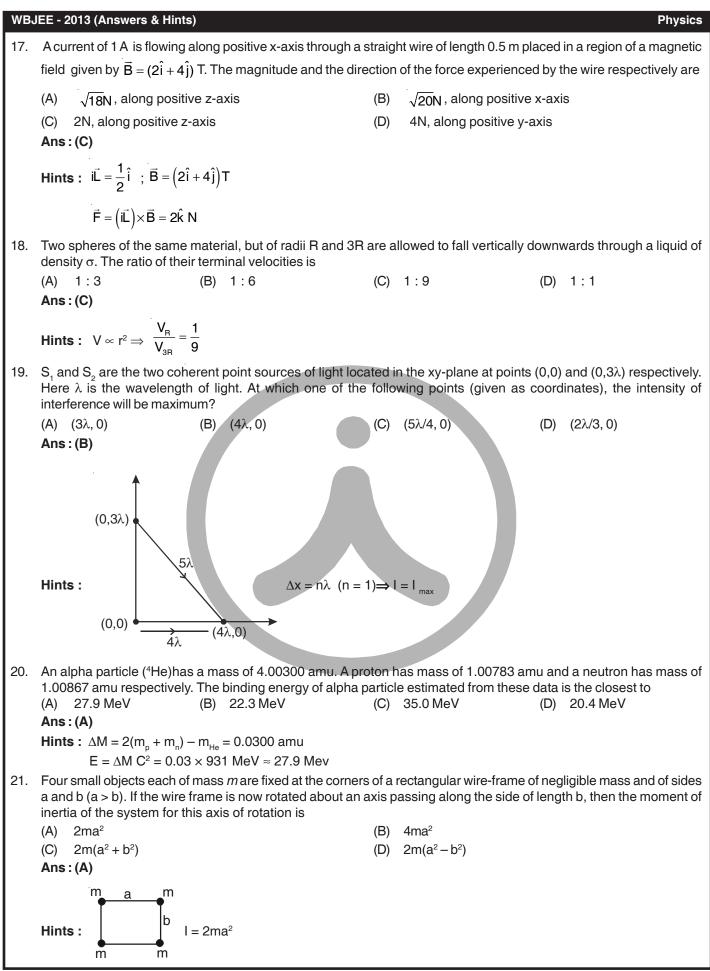
be

Physics Hints: $\theta = 2\pi n = \frac{\left(\frac{v_{f}^{2}}{r^{2}} - \frac{v_{i}^{2}}{r^{2}}\right)}{\left(2\frac{a}{r}\right)} \Rightarrow n = \frac{v_{f}^{2} - v_{i}^{2}}{(2ar)2\pi} \approx 95$ 12. Two glass prisms P_1 and P_2 are to be combined together to produce dispersion without deviation. The angles of the prisms P₁ and P₂ are selected as 4° and 3° respectively. If the refractive index of prism P₁ is 1.54, then that of P₂ will (A) 1.48 (B) 1.58 (C) 1.62 (D) 1.72 Ans:(D) **Hints**: $\delta_1 + \delta_2 = 0 \Rightarrow (\mu - 1)A_1 = (\mu_2 - 1)A_2 \Rightarrow \mu_2 = 1.72$ 13. The ionization energy of the hydrogen atom is 13.6 eV. The potential energy of the electron in n = 2 state of hydrogen atom is (B) - 3.4 eV (C) + 6.8 eV (A) + 3.4 eV (D) - 6.8 eV Ans:(D) Hints: $E_{n=2} = \frac{-13.6z^2}{r^2} \approx -3.4 \text{ ev}, PE = 2E_{n=2} \approx -6.8 \text{ ev}$ 14. Water is flowing in streamline motion through a horizontal tube. The pressure at a point in the tube is p where the velocity of flow is v. At another point, where the pressure is p/2, the velocity of flow is [density of water = ρ] (B) $\sqrt{v^2 - \frac{p}{o}}$ (C) $\sqrt{v^2 + \frac{2p}{q}}$ (A) $\sqrt{v^2 + \frac{p}{q}}$ (D) $\sqrt{v^2 - \frac{2p}{p}}$ Ans:(A) Hints: $p + \frac{1}{2}\rho v^2 = \frac{p}{2} + \frac{1}{2}\rho v_1^2 \implies v_1 = \sqrt{\frac{p}{\rho} + v^2}$ 15. In the electrical circuit shown in figure, the current through the 4Ω resistor is 9V **8**Ω 0.5 A 20 \sim (A) 1A (B) 0.5 A 0.25 A (D) 0.1 A (C) Ans:(B) Hints : $\frac{1}{2}$ A

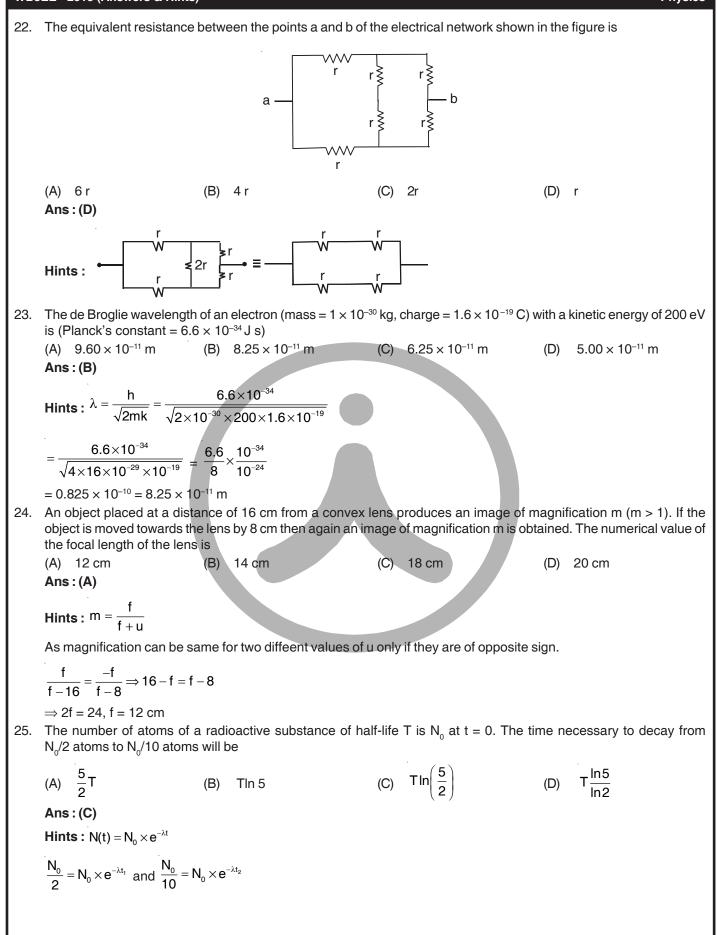
16. A wire of initial length L and radius r is stretched by a length I. Another wire of same material but with initial length 2L and radius 2r is stretched by a length 2l. The ratio of the stored elastic energy per unit volume in the first and second wire is,

(C) 2:1 (A) 1:4 (B) 1:2 (D) 1:1 Ans:(D) **Hints**: $\frac{U_1}{U_2} = \left\{ \frac{(\text{strain})_1}{(\text{strain})_2} \right\}^2 = \frac{l^2}{L^2} \frac{4L^2}{4l^2} = 1 : 1$

(27)







(D) 1 m

$$\ell n 2 = \lambda t_1, \quad t_1 = \frac{\ell n 2}{\lambda} = \frac{\ell n 2 \times T}{\ell n 2}, \quad t_2 = \frac{T \times \ell n 10}{\ell n 2}$$

$$(t_2 - t_1) = T \left[\frac{\ell n 10}{\ell n 2} - 1 \right] = T \times \left[\frac{\ell n 10 - \ell n 2}{\ell n 2} \right]$$

$$= T \times \frac{\ell n 5}{\ell n 2}$$
26. A travelling acoustic wave of frequency 500 Hz is moving along the positive x-direction with a velocity of 300 ms⁻¹. The phase difference between two points x₁ and x₂ is 60°. Then the minimum separation between the two pints is (A) 1 mm (B) 1 cm (C) 10 cm (D) 1 m Ans : (C)
Hints : $\lambda = \frac{300}{700} = \frac{3}{7}$

$$\phi = \frac{2\pi}{\lambda} (\Delta x), \quad \frac{\pi}{3} = \frac{2\pi}{\lambda} (\Delta x)$$

$$\therefore \Delta x = 10 \text{ cm}$$

27. A mass M at rest is broken into two pieces having masses m and (M-m). The two masses are then separated by a distance r. The gravitational force between them will be the maximum when the ratio of the masses [m:(M-m)] of the two parts is

(C) 10 cm

(A) 1:1
(B) 1:2
(C) 1:3
(D) 1:4
Ans:(A)
Hints:
$$F = \frac{Gm_1m_2}{r^2}$$

 $\frac{dF}{dm} = \frac{d}{dm}[m(M-m)] = 0$
 $\boxed{m = \frac{M}{2}}, \quad (\frac{m}{M-m}) = \frac{1}{1}$

- 28. A shell of mass 5M, acted upon by no external force and initially at rest, bursts into three fragments of masses M, 2M and 2M respectively. The first two fragments move in opposite directions with velocities of magnitudes 2V and V respectively. The third fragment will
 - (A) move with a velocity V in a direction perpendicular to the other two
 - (B) move with a velocity 2V in the direction of velocity of the first fragment
 - (C) be at rest
 - (D) move with a velocity V in the direction of velocity of the second fragment

Ans : (C)

Hints : By conservation of momentum

$$0 = M \times 2\vec{V} - 2M\vec{V} + 2M\vec{V}$$

$$\overrightarrow{V} = 0$$

29. A bullet of mass m travelling with a speed v hits a block of mass M initially at rest and gets embedded in it. The combined system is free to move and there is no other force acting on the system. The heat generated in the process will be

(C) $\frac{Mmv^2}{2(M-m)}$ (D) $\frac{mMv^2}{2(M+m)}$ (B) $\frac{mv^2}{2}$ (A) Zero Ans:(D)

Hints : Loss in K.E. =
$$\frac{m_m^2}{2(m_1 + m_n)} (u_1 - u_n)^2 = \frac{Mmu^2}{2(M + m)}$$

30. A particle moves along X-axis and its displacement at any time is given by $x(t) = 2t^5 - 3t^4 + 4t$ in SI units. The velocity of the particle when its acceleration is zero, is
(A) 2.5 ms^{-1} (B) 3.5 ms^{-1} (C) 4.5 ms^{-1} (D) 8.5 ms^{-1}
Ans: (A)
Hints : $x(t) = (2t^2 - 3t^2 + 4t)$
 $v = \frac{dx}{dt} = (6t^2 - 6t + 4), a = (\frac{dv}{dt}) = (12t - 6) = 0$
 $12t = 6, t = \frac{6}{12} - \frac{1}{2} \sec c, v = (6t^2 - 6t + 4) = 2.5 \text{ m/s}$
31. A planet moves around the sun in an elliptical orbit with the sun at one of its foci. The physical quantity associated with the motion of the planet that remains constant with time is
(A) velocity (B) centripetal force (C) linear momentum (D) angular momentum
Ans: (D)
Torque about the sun, $S = 6$
 \Rightarrow Angular momentum is conserved
32. The fundamental frequency of a closed pipe is equal to the frequency of the second harmonic of an open pipe. The ratio of their lengths is
(A) 1:2 (B) 1:4 (C) 1:8 (D) 1:16
Ans: (B)
Hints: $t_u = 2t_u = \frac{v}{4t_{u_u}} = 2\frac{v_u x}{2t_{u_u}}$
 $\Rightarrow \frac{t_{u_u}}{t_{u_u}} = \frac{1}{4}$
33. A particle of mass M and charge q is released from rest in a region of uniform electric field of magnitude E. After a time t, the distance travelled by the charge is S and the kinetic energy attained by the particle is T. Then, the ratio TS
(A) remains constant with time (B) varias linearly with the mass M of the particle
(C) is independent of the charge q
Ans: (A)
Hints: $S = \frac{1}{2} \left(\frac{qE}{m}\right)t^2$
 $T = \frac{1}{2}n \left(\frac{qE}{m}\right)t^2$
 $T = \frac{1}{2}n \left(\frac{qE}{m}\right)t^2$
An alternating current in a circuit is given by I = 20 sin (100 mt + 0.05 m) A. The r.m.s. value and the frequency of current respectively are
(A) 10A & 100 Hz (B) 10A & 50 Hz (C) 10\sqrt{2} A & 50 Hz (D) 10\sqrt{2} A & 100 Hz (E) 10 \sqrt{2} A & 1

Ans:(C)

Hints : $I = 20 \sin (100 \pi t + 0.05 \pi)$

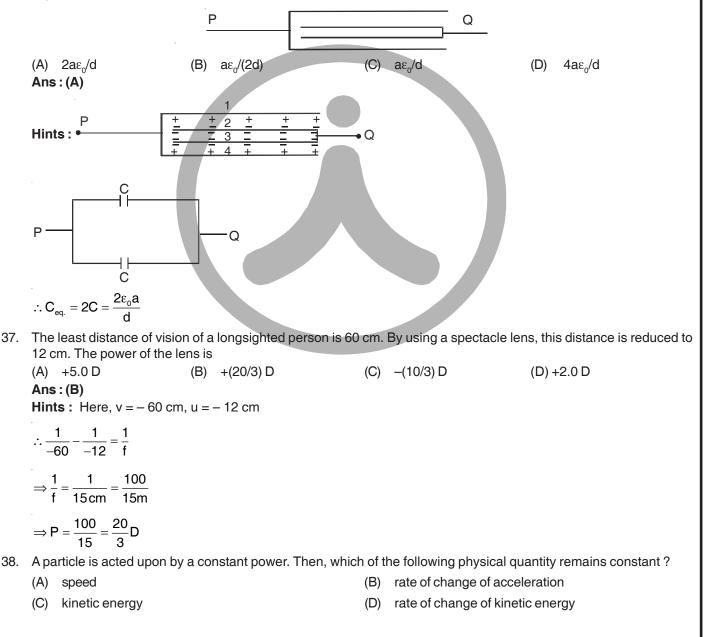
$$\therefore I_{\rm rms} = \frac{20}{\sqrt{2}} = 10\sqrt{2}$$

 $w = 100\pi \Rightarrow f = 50 Hz$

35. The specific heat c of a solid at low temperature shows temperature dependence according to the relation $c = DT^3$ where D is a constant and T is the temperature in kelvin. A piece of this solid of mass m kg is taken and its temperature is raised from 20 K to 30 K. The amount of the heat required in the process in energy units is (A) 5×10^4 Dm (B) $(33/4) \times 10^4$ Dm (C) $(65/4) \times 10^4$ Dm (D) $(5/4) \times 10^4$ Dm Ans : (C)

Hints:
$$Q = \int dQ = \int_{T_1=20}^{T_2=30} mcdT = \int_{20}^{30} mDT^3 dT = \frac{65mD}{4} \times 10^4$$

36. Four identical plates each of area a are separated by a distance d. The connection is shown below. What is the capacitance between P and Q?



Ans:(D)

Hints : By definition, $P = \frac{dw}{dt} = \frac{dk}{dt} = constant$

39. A particle of mass M and charge q, initially at rest, is accelerated by a uniform electric field E through a distance D and is then allowed to approach a fixed static charge Q of the same sign. The distance of the closest approach of the charge q will then be

(A)
$$\frac{qQ}{4\pi\epsilon_0 D}$$
 (B) $\frac{Q}{4\pi\epsilon_0 ED}$ (C) $\frac{qQ}{2\pi\epsilon_0 D^2}$ (D) $\frac{Q}{4\pi\epsilon_0 E}$

Ans:(B)

Hints :

$$\therefore (qED) = \frac{1}{4\pi\epsilon_0} \frac{qQ}{r_0} \implies r_0 = \frac{Q}{4\pi\epsilon_0 ED}$$

40. In an n-p-n transistor

- (A) the emitter has higher degree of doping compared to that of the collector
- (B) the collector has higher degree of doping compared to that of the emitter
- (C) both the emitter and collector have same degree of doping
- (D) the base region is most heavily doped

Ans:(A)

41. At two different places the angles of dip are respectively 30° and 45°. At these two places the ratio of horizontal component of earth's magnetic field is

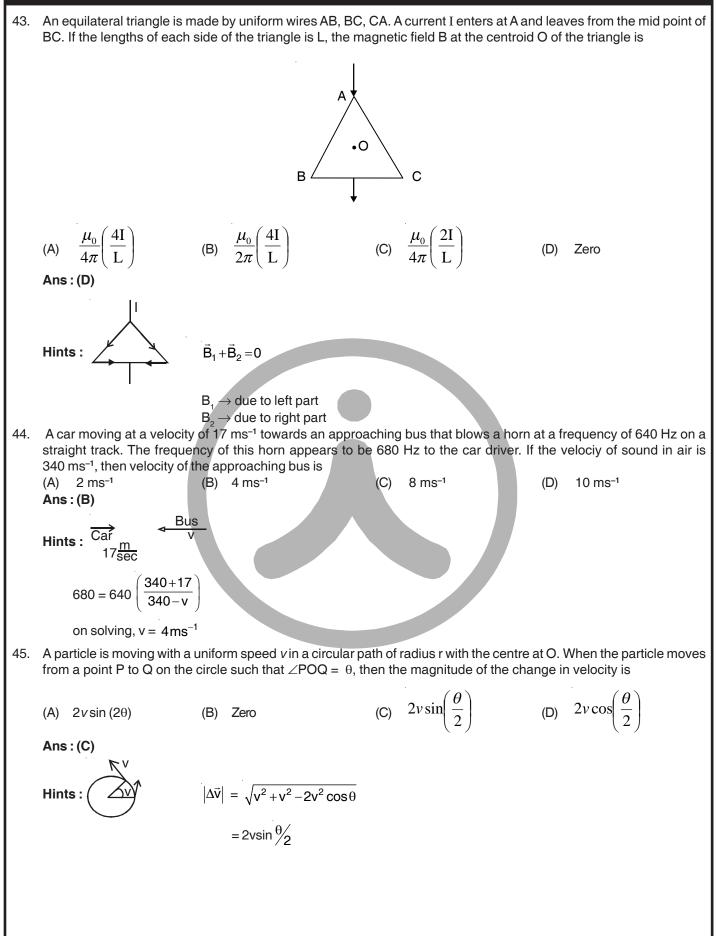
(A) $\sqrt{3}:\sqrt{2}$	(B) $1:\sqrt{2}$	(C) 1:2	(D) $1:\sqrt{3}$
Ans : (A)			

 $Hints: \frac{H_1}{H_2} = \frac{B\cos 30^\circ}{B\cos 45^\circ}$

- Note : Information is not sufficient in the given question. It can be solved only when magnetic field at these two places are equal.
- 42. Two vectors are given by $\vec{A} = \hat{i} + 2\hat{j} + 2\hat{k}$ and $\vec{B} = 3\hat{i} + 6\hat{j} + 2\hat{k}$. Another vector \vec{C} has the same magnitude as \vec{B}

but has the same direction as \vec{A} . Then which of the following vectors represents \vec{C} ?

(A)
$$\frac{7}{3}(\hat{i}+2\hat{j}+2\hat{k})$$
 (B) $\frac{3}{7}(\hat{i}-2\hat{j}+2\hat{k})$ (C) $\frac{7}{9}(\hat{i}-2\hat{j}+2\hat{k})$ (D) $\frac{9}{7}(\hat{i}+2\hat{j}+2\hat{k})$
Ans : (A)
Hints : $\vec{C} = \frac{\hat{i}+2\hat{j}+2\hat{k}}{\sqrt{1+4+4}} \times \sqrt{3^2+6^2+2^2}$
 $= \frac{\hat{i}+2\hat{j}+2\hat{k}}{3} \times \sqrt{49}$
 $= \frac{7}{3}(\hat{i}+2\hat{j}+2\hat{k})$



CATEGORY-II

Q. 46 – Q. 55 carry two marks each, for which only one option is correct. Any wrong answer will lead to deduction of 2/3 mark 46. Two simple harmonic motions are given by

 $x_1 = a \sin \omega t + a \cos \omega t$ and n

$$x_2 = a \sin \omega t + \frac{a}{\sqrt{3}} \cos \omega t$$

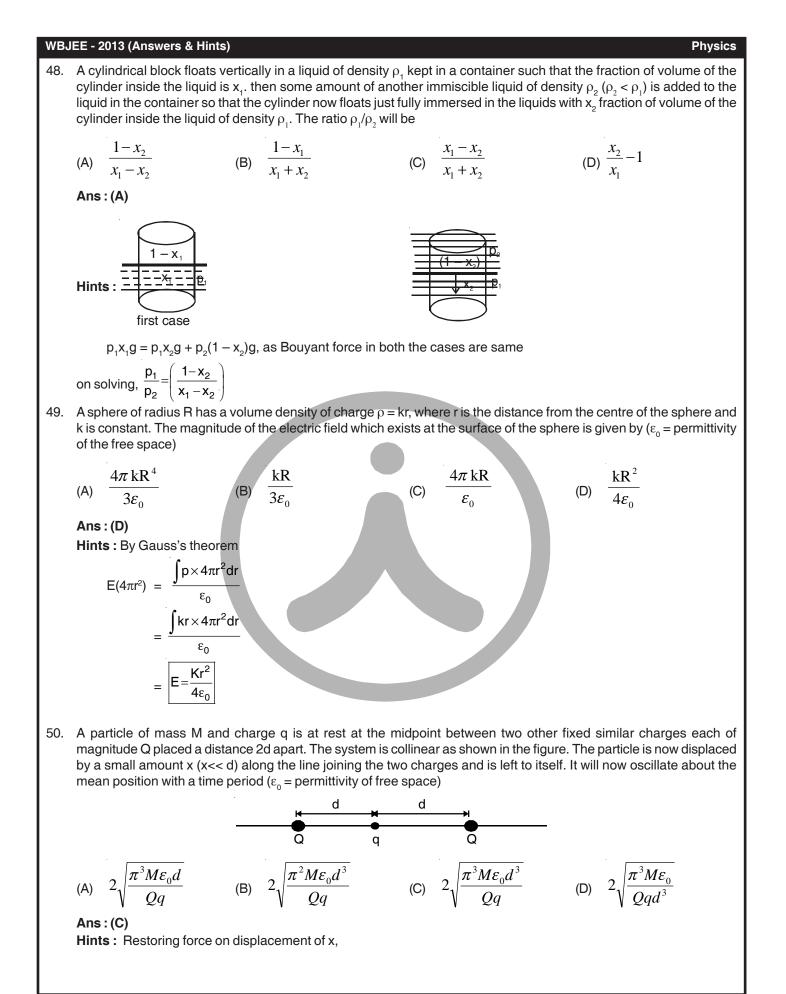
The ratio of the amplitudes of first and second motion and the phase difference between them are respectively

(A) $\sqrt{\frac{3}{2}} \text{ and } \frac{\pi}{12}$ (B) $\frac{\sqrt{3}}{2} \text{ and } \frac{\pi}{12}$ (C) $\frac{2}{\sqrt{3}} \text{ and } \frac{\pi}{12}$ (D) $\sqrt{\frac{3}{2}} \text{ and } \frac{\pi}{6}$ Ans:(A) Hints : for first S.H.M for second S H M phase difference is $\frac{\pi}{4} - \frac{\pi}{6} = \frac{\pi}{12}$

Ratio of amplitude $\frac{a_1}{a_2} = \frac{\sqrt{3}}{\sqrt{2}}$

47. A small mass m attached to one end of a spring with a negligible mass and an unstretched length L, executes vertical oscillations with angular frequency ω_0 . When the mass is rotated with an angular speed ω by holding the other end of the spring at a fixed point, the mass moves uniformly in a circular path in a horizontal plane. Then the increase in length of the spring during this rotation is

(A)
$$\frac{\omega^2 L}{\omega_0^2 - \omega^2}$$
 (B) $\frac{\omega_0^2 L}{\omega^2 - \omega_0^2}$ (C) $\frac{\omega^2 L}{\omega_0^2}$ (D) $\frac{\omega_0^2 L}{\omega^2}$
Ans : (A)
Kxcosθ of Kx
Hints : $\frac{1}{\omega_0^2}$ Kxsinθ
Kxsinθ = m ω^2 (L + x) sinθ
Kx = m ω_0^2
K = m ω_0^2
 $K = m\omega_0^2$
 $m\omega_0^2 x = m\omega^2$ (L + x)
and
 $\sqrt{\frac{K}{m}} = \omega_0$
 $K = m\omega_0^2$



Physics

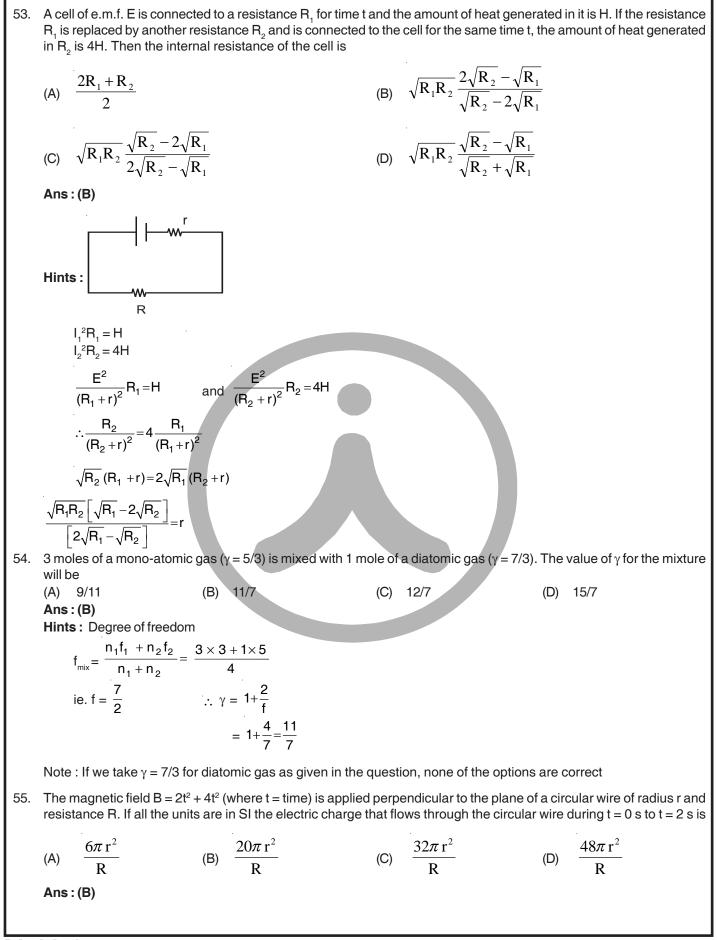
F = K
$$\left[\frac{q}{(d-x)^2} - \frac{Qq}{(d+x)^2} \right]$$

= KQq $\left[\frac{dx}{(d-x)^2} - \frac{Qq}{(d+x)^2} \right]$
= KQq $\left[\frac{dx}{(d^2-x^2)^2} \right]$
= KQq $\left[\frac{dx}{(d^2-x^2)^2} \right]$
= KQq $\left[\frac{dx}{d^2} \right]$ If (d ax)
= KQq $\left[\frac{dx}{d^2} \right]$
acceleration a = $\frac{F}{m} = \frac{4KQq}{md^3}$ X
 $w^2 = \frac{4KQq}{md^3}$
T = $\frac{2\pi}{m} = 2\pi \sqrt{\frac{md}{4KQq}} = 2\sqrt{\frac{\pi^3md^3\epsilon_0}{Qq}}$
51. A body is projected from the ground with a velocity $\vec{y} = (3\hat{t} + 10\hat{j}) \text{ ms}^{-1}$. The maximum height attained and the range
of the body respectively are (given g = 10 \text{ ms}^{-2})
(A) 5 m and 6 m (B) 3 m and 10 m (C) 6 m and 5 m (D) 3 m and 5 m
Ans : (A)
Hints : V = 3i + 10j
V_z = 3 V_y = 10
H = $\frac{V_y^2}{2g} = \frac{10g}{2x 1g} = 5m$
E32. The stopping potential for photoelectrons from a metal surface is V, when monochromatic light of frequency v, is
incident on it. The stopping potential becomes V, when monochromatic light of frequency v, is
incident on it. The stopping potential becomes V, when monochromatic light of frequency v, is
incident on it. The stopping potential becomes V, when monochromatic light of frequency v, is
incident on it. The stopping potential becomes V, when monochromatic light of frequency v, is
incident on it. The stopping potential becomes V when monochromatic light of frequency v, is
incident on it. The stopping potential becomes V when monochromatic light of frequency v, is
incident on it. The stopping potential becomes V when monochromatic light of frequency v is incident on the
same metal surface. If h be the Planck's constant and e be the charge of an electron, then the frequency of light in the
second case is

(A)
$$v_1 - \frac{e}{h}(V_2 + V_1)$$
 (B) $v_1 + \frac{e}{h}(V_2 + V_1)$ (C) $v_1 - \frac{e}{h}(V_2 - V_1)$ (D) $v_1 + \frac{e}{h}(V_2 - V_1)$

Ans:(D)

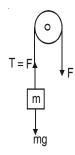
Hints:
$$hv_1 = \phi_0 + ev_1$$
 (1)
 $hv_2 = \phi_0 + ev_2$ (2)
 $h(v_2 - v_1) = e(v_2 - v_1)$
 $v_2 = \frac{e}{h}(v_2 - v_1) + v_1$



(38)

WB	JEE - 2013 (Answers & Hints) Physics
	Hints : $\Delta Q = \frac{\Delta \phi}{R}$
	R
	$= \frac{\pi r^{2}(B_{2} - B_{1})}{R} = \frac{\pi r^{2}[2 \times 2 + 4 \times 4]}{R} = \frac{20\pi r^{2}}{R}$
	R R R CATEGORY - III
	Q. 56 – Q. 60 carry two marks each, for which one or more than one options may be correct. Marking of
	correct options will lead to a maximum mark of twoon pro rata basis. There willbe no negative marking for these questions. However, any marking of wrong option will lead to award of zero mark against the respective question – irrespective of the number of corredt options marked.
56.	If E and B are the magnitudes of electric and magnetic fields respectively in some region of space, then the possibili- ties for which a charged particle may move in that space with a uniform velocity of magnitude v are
	(A) $E = vB$ (B) $E \neq 0, B = 0$ (C) $E = 0, B \neq 0$ (D) $E \neq 0, B \neq 0$
	Ans : (A, C, D)
57.	of the following statements are correct?
	(A) The equivalent current flowing in the circular path is proportional to r^2
	(B) The magnetic moment due to circular current loop is independent of m
	(C) The magnetic moment due to circular current loop is equal to 2e/m time the angular momentum of the electron
	(D) The angular momentum of the particle is proportional to the areal velocity of electron.
	Ans : (B , D) Hints : Magnetic moment μ = IA
	-
	$= \frac{ev \times}{2\pi y'} \pi r^2 = \frac{evr}{2}$ Angular momentum = 2 m $\frac{dA}{dt}$
58.	A biconvex lens of focal length f and radii of curvature of both the surfaces R is made of a material of refractive index n_1 . This lens is placed in a liquid of refractive index n_2 . Now this lens will behave like
	(A) either as a convex or as a concave lens depending solely on R
	(B) a convex lens depending on n_1 and n_2
	(C) a concave lens depending on n_1 and n_2
	(D) a convex lens of same focal length irrespective of R, n_1 and n_2
	Ans : (B , C)
59.	A block of mass m (= 0.1 kg) is hanging over a frictionless light fixed pulley by an inextensible string of negligible mass. The other end of the string is pulled by a constant force F in the vertically downward direction. The linear momentum of the block increase by 2 kg ms ⁻¹ in 1 s after the block starts from rest. Then, (given g = 10 ms ⁻²)
	m F
	(A) The tension in the string is F
1	(B) The tension in the string is 3N
	(C) The work done by the tension on the block is 20 J during this 1 s
	(D) The work done against the force of gravity is 10 J Ans : (A, B, D)

Hints :



F - mg = 2F = 2 + mg = 3 N

$$a = \frac{\text{unbalanced force}}{\text{mass}} = \frac{2}{0.1} = 20 \text{ m/s}^2$$

$$\therefore S = \frac{1}{2}at^2 = \frac{1}{2} \times 20 \times 1 = 10m$$

:. W by tension = $F \times 10 = 3 \times 10 = 30 J$ W against gravity = mg × s = = 1 × 10 = 10 J

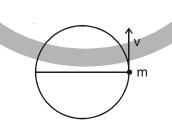
60. A bar of length I carrying a small mass m at one of its ends rotates with a uniform angular speed ω in a vertical plane about the mid-point of the bar. During the rotation, at some instant of time when the bar is horizontal, the mass is detached from the bar but the bar continues to rotate with same ω . The mass moves vertically up, comes back and reches the bar at the same point. At that place, the acceleration due to gravity is g.

(A) This is possible if the quantity
$$\frac{\omega^2 \ell}{2\pi g}$$
 is an integer

(B) The total time of flight of the mass is proportional to ω^2

- (C) The total distance travelled by the mass in air is proportional to ω^2
- (D) The total distance travelled by the mass in air and its total time of flight are both independent on its mass.

Ans : (A, C, D) Hints :



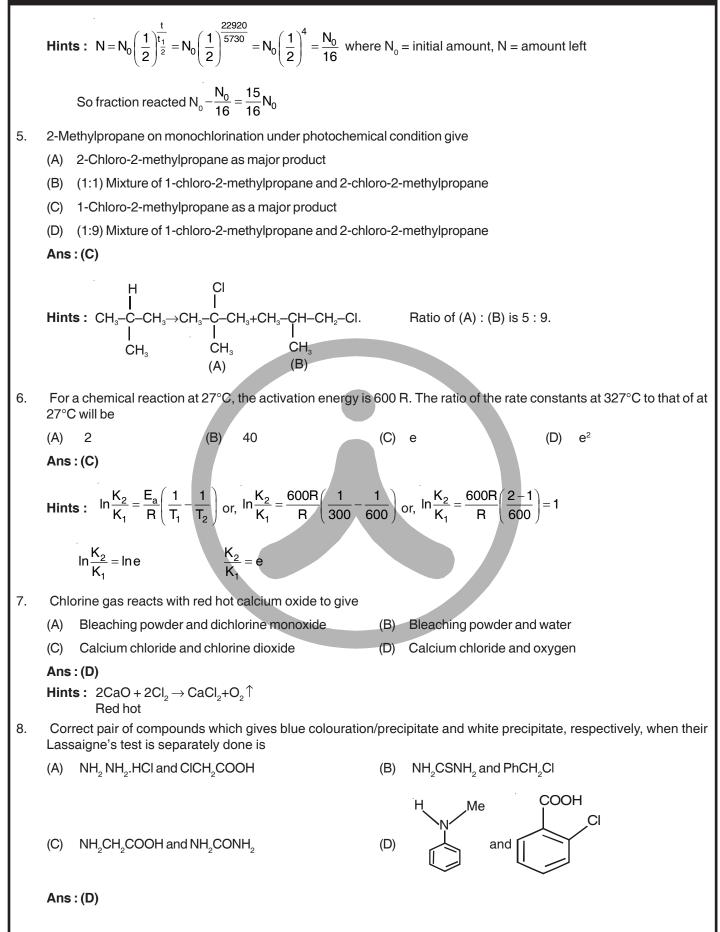
$$v = \frac{\ell}{2}\omega$$
, $T = \frac{2v}{g} = \frac{\ell\omega}{g}$

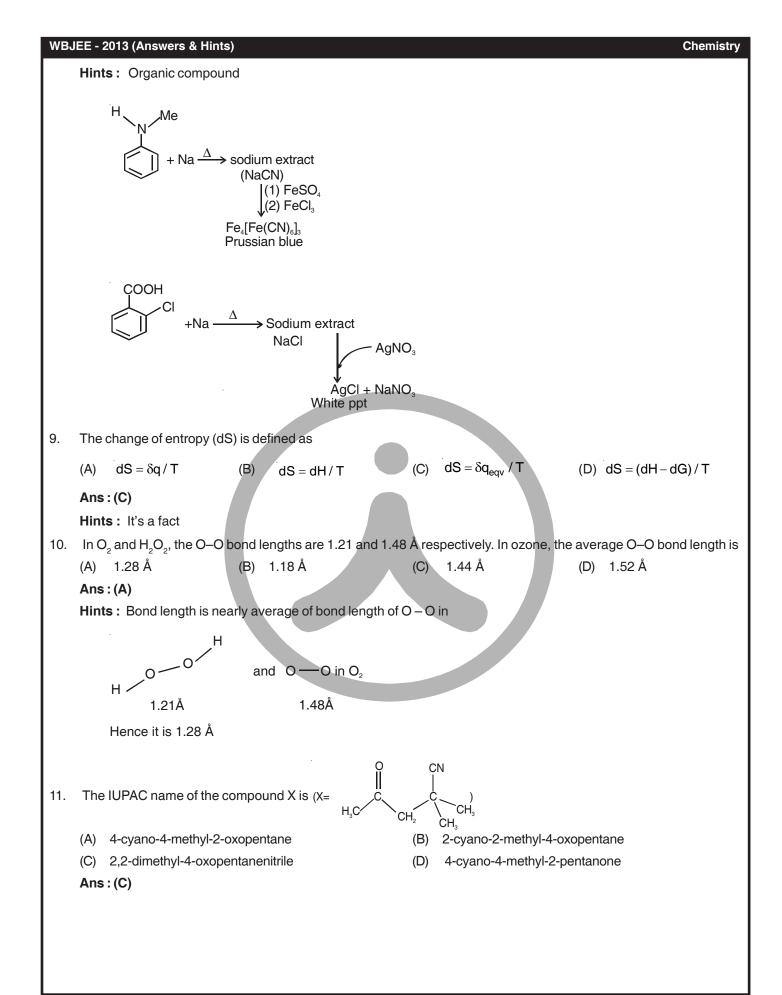
$$n\frac{2\pi}{\omega} = \frac{\ell\omega}{g}$$
 (as completes n rotations within T) $\therefore n = \frac{\ell\omega^2}{2\pi g}$

Distance travelled =
$$2h = 2\frac{v^2}{2g} = \frac{\ell^2 \omega^2}{4g}$$

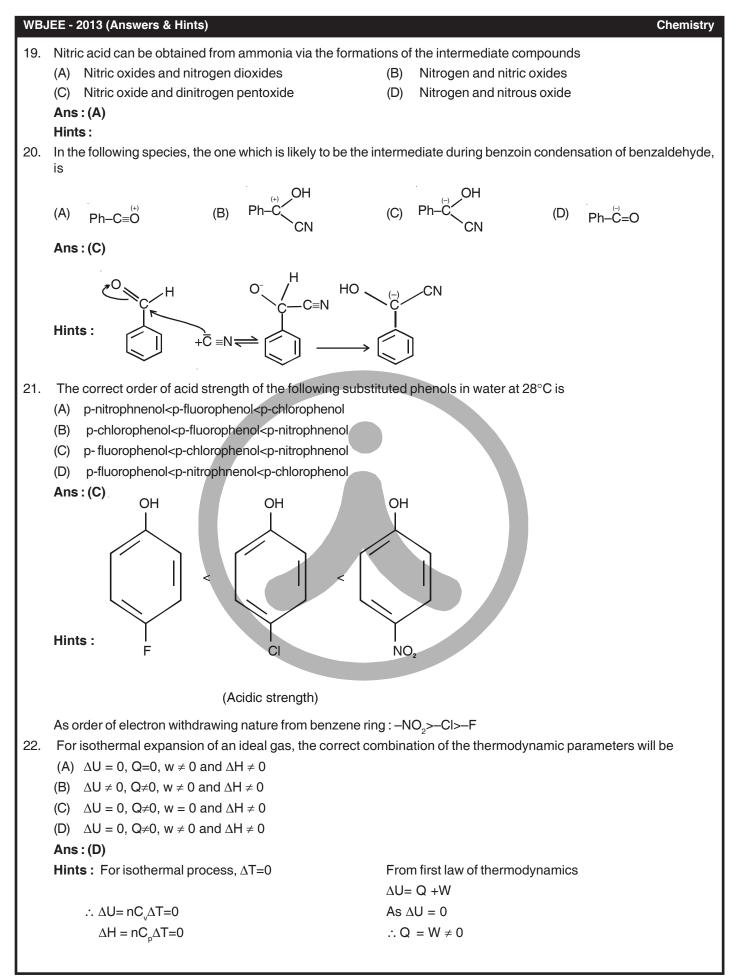
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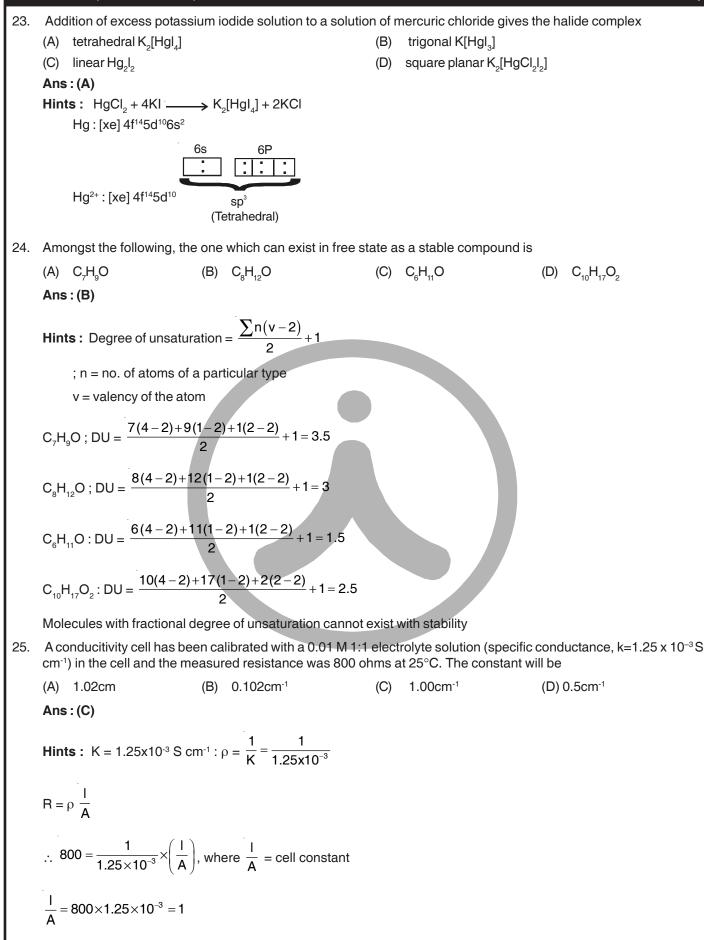
	BJEE - 2012 (Answers & Hints)	Chemistry					
	(Å)	Code- ▲					
	Aakash						
	Medical IIT-JEE Foundations						
	(Divisions of Aakash Educational Services Ltd.)						
	ANSWERS & HINTS						
	for						
	WBJEE - 2013						
	SUB : CHEMISTRY						
	CATEGORY - I Q. 1 – Q. 45 carry one mark each, for which only one option is correct. Any wrong	answer will lead to					
	deduction of 1/3 mark.						
1.	In diborane, the number of electrons that account for bonding in the bridges is (A) Six (B) Two (C) Eight (D) F	Four					
	Ans : (D)	our					
	H. H. H						
	Hints :						
	Each bridging bond is formed by two electrons. Hence four electrons account for bond	dina in the bridaes.					
2.	The optically active molecule is						
	COOMe COOMe COOMe	СООН					
		н — — он					
		н — — Он					
	COOMe COOMe COOH	СООН					
	Ans : (C) Hints : Others are meso compound due to presence of plane of symmetry.						
3.	A van der Waals gas may behave ideally when						
	(A) The volume is very low						
	(B) The temperature is very high						
	(C) The pressure is very low(D) The temperature, pressure and volume all are very high						
	Ans : (C)						
	Hints : A van der waals gas may behave ideally when pressure is very low as compressibility 1. At high temperature $7 > 1$	factor (Z) approaches					
4.	1. At high temperature Z > 1. The half-life for decay of ¹⁴ C by β -emission is 5730 years. The fraction of ¹⁴ C decays, in a samp	le that is 22,920 vears					
	old, would be						
		5/16					
	Ans : (D)						
Ļ	ach Institute - Read Office: Askash Tower Plot No. 4 Sector 11 Dwarks New Delhi 110075 Ph : 011-4760						



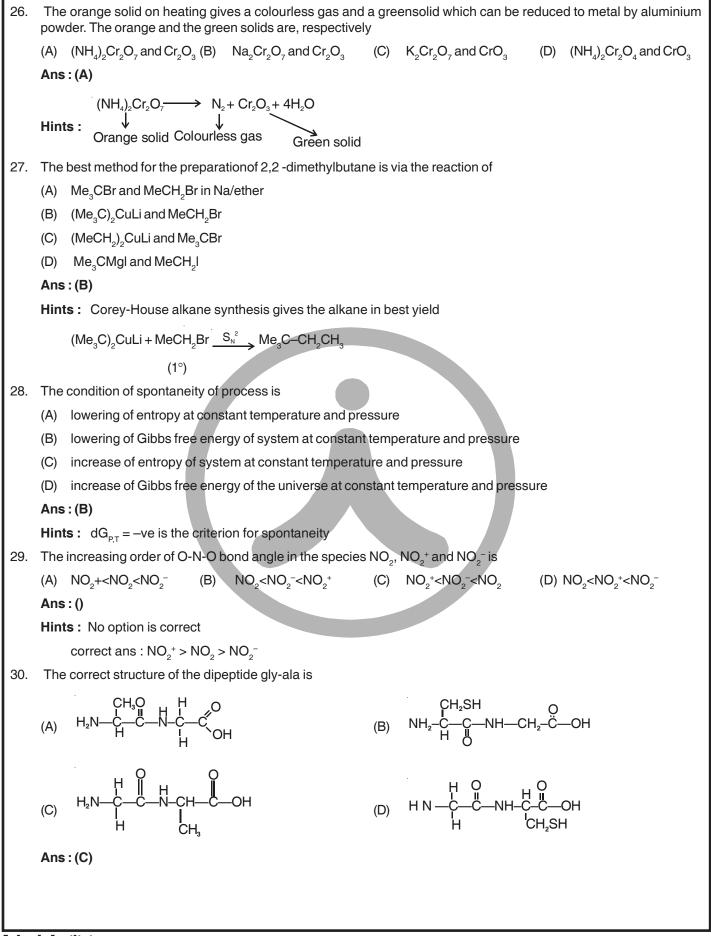


WB.	JEE - 2013 (Answers & Hints)				Chemistry
	Hints: (1) (2) (1)	4-охој	pentanenitrile		
12.	At 25°C, the solubility product of a salt of MX_2 type is 3. at the same temperature will be	2 × 10	⁻³ in water. The solubili	ty (in n	noles/lit) of MX ₂ in water
	(A) 1.2×10^{-3} (B) 2×10^{-3}	(C)	3.2 × 10 ^{−3}	(D)	1.75 × 10⁻³
	Ans : (B)				
	Hints: $K_{sp}(MX_2) = 4s^3 = 3.2 \times 10^{-8} \implies s = \sqrt{\frac{3.2 \times 10^{-8}}{4}}$				
1	$= 2 \times 10^{-3}$				
13.	In SOCI ₂ , the CI–S–CI and CI–S–O bond angles are				
	(A) 130° and 115° (B) 106° and 96°	(C)	107° and 108°	(D)	96° and 106°
	Ans:(D)				
	Hints : Fact				
14.	(+)-2-chloro-2-phenylethane in toluene racemises slowly tion of	y in the		ount of	0
1	(A) Carbanion (B) Carbene	(C)	Free-radical	(D)	Carbocation
1	Ans : (D)				
	Hints : SbCl ₅ removes Cl ⁻ from the substrate to generate by Cl ⁻ from both top and bottom to result in a racemic m	nixture			
15.	Acid catalysed hydrolysis of ethyl acetate follows a pseu carried out with large excess of ester, the order with res			spect	to ester. If the reaction is
1	(A) 1.5 (B) 0	(C)	2	(D)	1
1	Ans: (B)				
16.	Hints : With large excess of ester the rate of reaction is The different colours of litmus in acidic, neutral and basi	•		ntratio	n.
10.	(A) Red, orange and blue		Blue, violet and red		
	(C) Red, colourless and blue	(D)	Red, violet and blue		
	Ans : (D)				
	Hints :				
17.	Baeyer's reagent is (A) Alkaline potassium permanganate	(B)	Acidified potassium pe	arman	nanate
1	(C) Neutral potassium permanganate	(D)	Alkaline potassium m		
1	Ans: (A)		·	U	
1	Hints :				
18.	The correct order of equivalent conductances at infinite d HO^- ions is	ilution	in water at room tempe	rature	for H⁺, K⁺, CH₃COO⁻ and
1	(A) $HO^->H^+>K^+>CH_3COO^-$		H ⁺ >HO ⁻ >K ⁺ >CH ₃ COO		
	(C) $H^+>K^+>HO^->CH_3COO^-$	(D)	H+>K+>CH ₃ COO->HO	-	
	Ans:(B)				

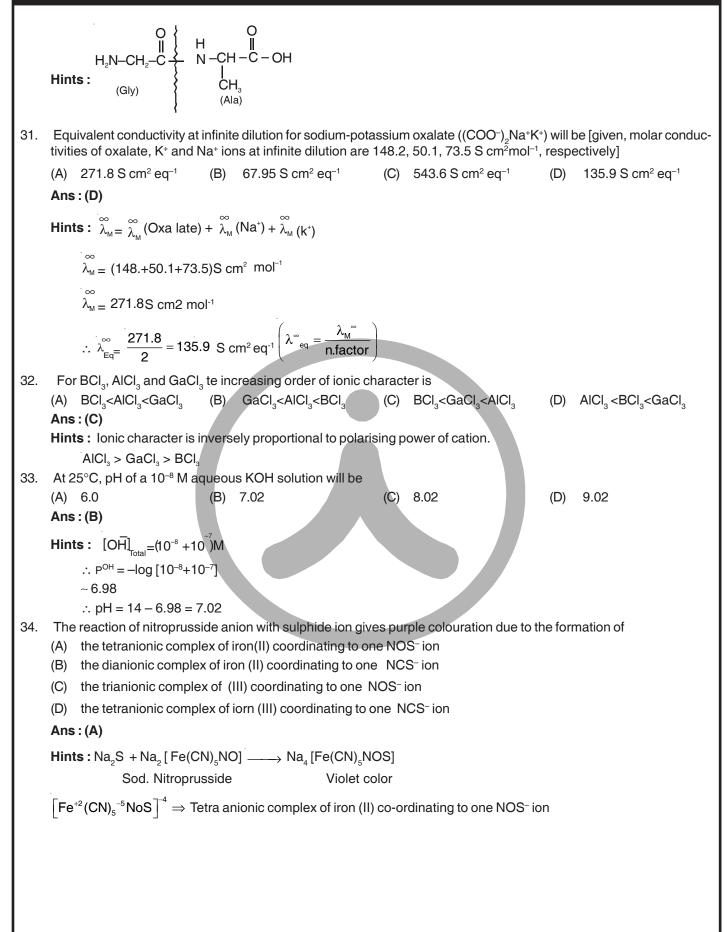




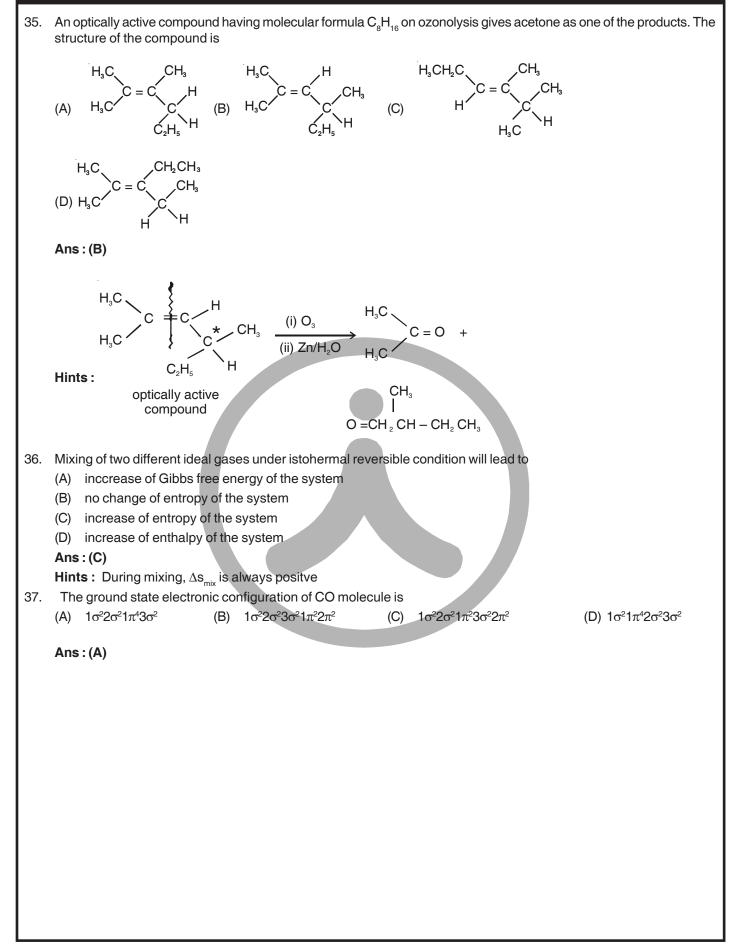
Chemistry



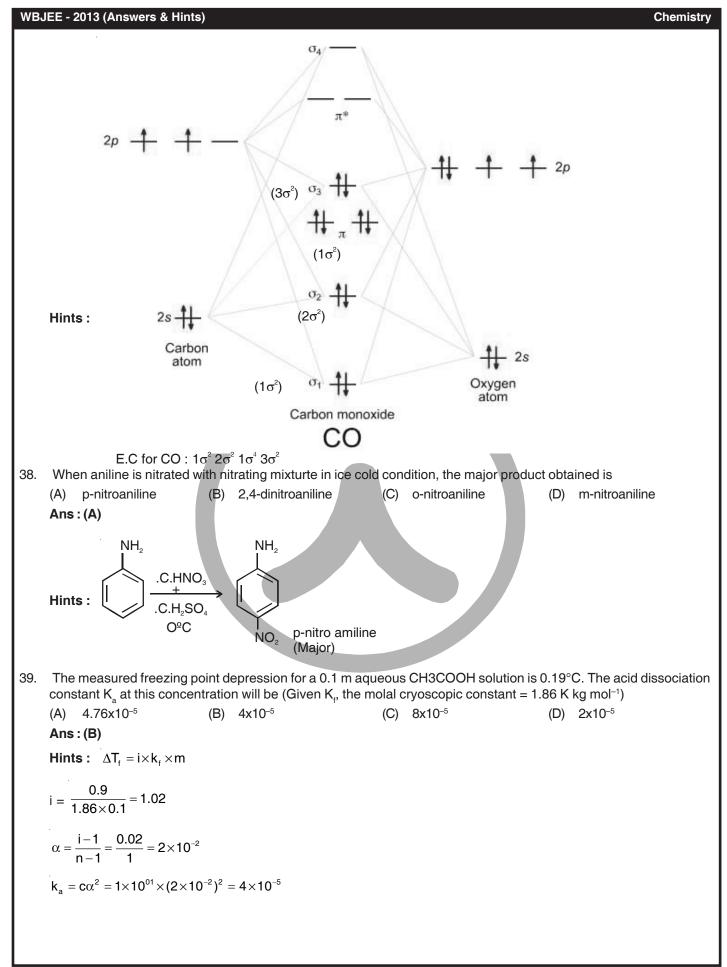
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Chemistry



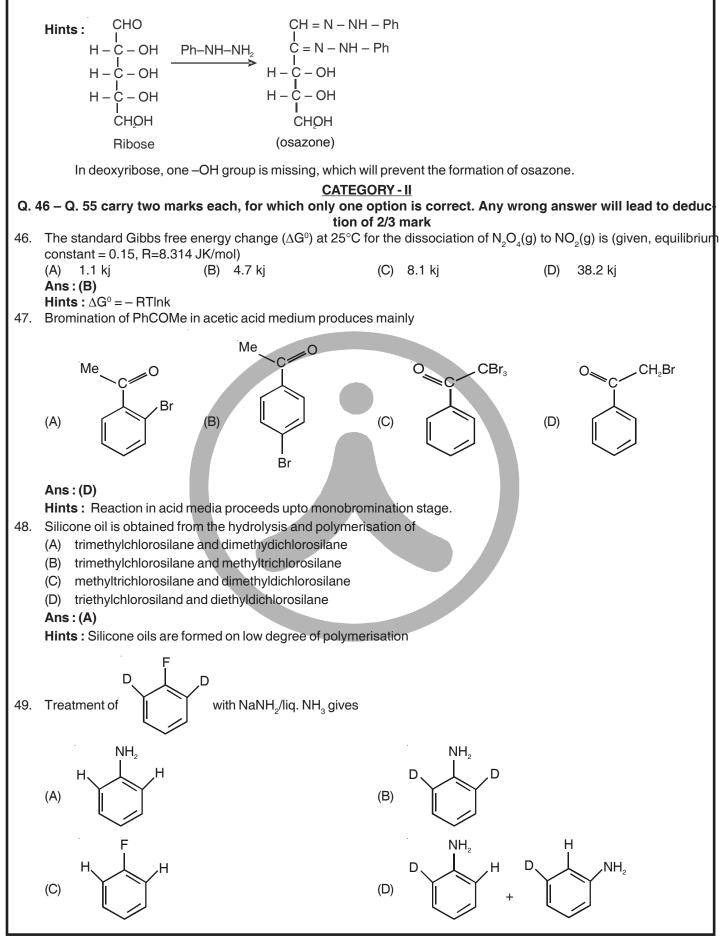
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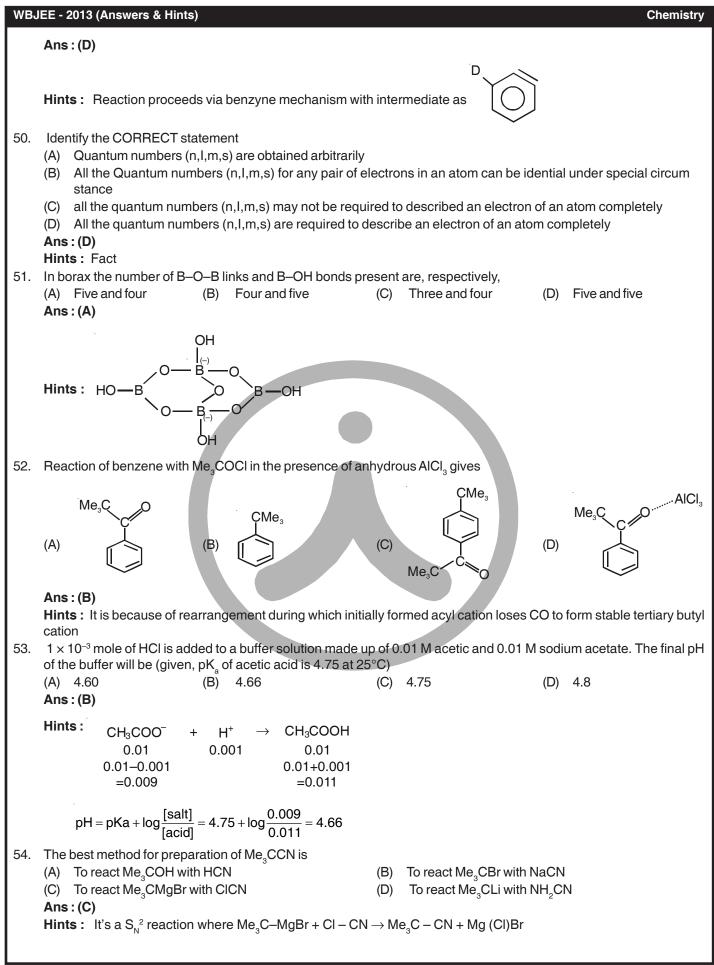


40.	The ore chromite is (A) $FeCr_2O_4$ (B) $CoCr_2O_3$ Ans : (A) Chromite ore is $FeCr_2O_4$ 'Sulphan' is (A) a mixture of SO ₃ and H ₂ SO ₅ (B) 100% conc. H ₂ SO ₄ (C) a mixture of gypsum and conc. H ₂ SO ₄	(C) CrFe ₂ O ₄	(D) FeCr ₂ O3
41.	Ans : (A) Chromite ore is $FeCr_2O_4$ 'Sulphan' is (A) a mixture of SO ₃ and H ₂ SO ₅ (B) 100% conc. H ₂ SO ₄ (C) a mixture of gypsum and conc. H ₂ SO ₄	(C) CrFe ₂ O ₄	(D) FeCr ₂ O ₃
41.	Chromite ore is FeCr_2O_4 'Sulphan' is (A) a mixture of SO ₃ and H ₂ SO ₅ (B) 100% conc. H ₂ SO ₄ (C) a mixture of gypsum and conc. H ₂ SO ₄		2 0
41.	'Sulphan' is (A) a mixture of SO ₃ and H ₂ SO ₅ (B) 100% conc. H ₂ SO ₄ (C) a mixture of gypsum and conc. H ₂ SO ₄		
41.	(A) a mixture of SO ₃ and H ₂ SO ₅ (B) 100% conc. H ₂ SO ₄ (C) a mixture of gypsum and conc. H ₂ SO ₄		
	(B) 100% conc. H_2SO_4 (C) a mixture of gypsum and conc. H_2SO_4		
	(C) a mixture of gypsum and conc. H_2SO_4		
	(D) 100% oleum (a mixture of 100% SO_3 in 100% H_2	SO ₄)	
	Ans : (D)		
10	Hints : Sulphan is pure liquid SO_3 Bracquire volume (P)() work done by an ideal graceous	avetam at constant valuma	is (where E is internal anarow of the
42.	Pressure-volume (PV) work done by an ideal gaseous system)	system at constant volume	is (where E is internal energy of the
1	(A) –ΔP/P (B) Zero	(C) –V∆P	(D) −∆E
1	Ans:(B)		
1	Hints : From 1st law of thermodynamic $AF = G_{1}w_{1}$ Now $w_{2} = BAV$ for $Av = 0$		
1	$\Delta E = q+w$. Now w = P ΔV . for $\Delta v = 0$ w = 0		
43.	Amongst [NiCl ₄] ²⁻ , [Ni(H ₂ O) ₆] ²⁺ ,[Ni(PPh ₃) ₂ Cl ₂], [Ni(CO) ₄] and $[Ni(CN)_4]^{2-}$, the paran	nagnetic species are
1			
1	(A) $[NiCl_4]^{2-}, [Ni(H_2O)_6]^{2+}, [Ni(PPh_3)_2Cl_2]$ (B) $[Ni(CO)_4], [Ni(PPh_3)_2Cl_2], [NiCl_4]^{2-}$		
1	(b) $[Ni(CN)_{4]}^{2-}, [Ni(H_{2}O)_{5}]^{2+}, [NiCl_{4}]^{2-}$		
1	(D) $[Ni(PPh_3)_2Cl_2], [Ni(CO)_4], [Ni(CN)_4]^{2-}$		
1	Ans: (A)		
1	Hints : $Ni^{+2} = 3d^8 4s^0$ (i) [NiCl] ² -Cl ⁻ weak ligand	(spectrochemical series)	so no pairing possible CFSE <
1	Pairing energy)	(spectrochemical series),	
1			possible. CFSE < pairing energy)
1	(iii) [Ni(PPh ₃) ₂ Cl ₂] alou complex tetrahedral.	gn. PPn ₃ nas d-accepta	nce but presence of CI makes
44.	Number of hydrogen ions present in 10 millionth part of	of 1.33 cm ³ of pure water at	t 25°C is
	(A) 6.023 million (B) 60 million	(C) 8.01 million	(D) 80.23 million
	Ans : (C)		
	Ans : (C) Hints :		
	Ans : (C)		
	Ans : (C) Hints : Now $[H^+] = 10^{-7}$ mole / litre Now 1000 ml contains 10^{-7} mole. H^+		
	Ans : (C) Hints : Now $[H^+] = 10^{-7}$ mole / litre Now 1000 ml contains 10^{-7} mole. H^+ 1ml " " $\frac{10^{-7}}{1000}$ mole H^+	$10 \text{ million} = 10^{-7}$	
	Ans : (C) Hints : Now $[H^+] = 10^{-7}$ mole / litre Now 1000 ml contains 10^{-7} mole. H^+	10 million = 10^{-7} so,10 million th part of 1	1.33cm ³
	Ans : (C) Hints : Now $[H^+] = 10^{-7}$ mole / litre Now 1000 ml contains 10^{-7} mole. H^+ 1ml " " $\frac{10^{-7}}{1000}$ mole H^+		1.33cm ³
	Ans : (C) Hints : Now $[H^+] = 10^{-7}$ mole / litre Now 1000 ml contains 10^{-7} mole. H^+ 1ml " " $\frac{10^{-7}}{1000}$ mole H^+ 1.33×10 ⁻⁷ ml — "1.33×10 ⁻¹⁷ so, no of H ⁺ ions = 1.33×10 ⁻¹⁷ × N _A	so,10 million th part of 1	1.33cm ³
45.	Ans : (C) Hints : Now $[H^+] = 10^{-7}$ mole / litre Now 1000ml contains 10^{-7} mole. H^+ $1ml$ " " $\frac{10^{-7}}{1000}$ mole H^+ 1.33×10^{-7} ml — " 1.33×10^{-17} so, no of H^+ ions = $1.33 \times 10^{-17} \times N_A$ Ribose and 2-deoxyribose can be differentiated by	so,10 million th part of 1 = 1.33×10^{-7} ml	
45.	Ans : (C) Hints : Now $[H^+] = 10^{-7}$ mole / litre Now 1000 ml contains 10^{-7} mole. H^+ $1ml$ " $\frac{10^{-7}}{1000}$ mole H^+ 1.33×10^{-7} ml — " 1.33×10^{-17} so, no of H^+ ions = $1.33 \times 10^{-17} \times N_A$ Ribose and 2-deoxyribose can be differentiated by (A) Fehling's reagent (B) Tollens's reagent	so,10 million th part of 1	
45.	Ans : (C) Hints : Now $[H^+] = 10^{-7}$ mole / litre Now 1000ml contains 10^{-7} mole. H^+ $1ml$ " " $\frac{10^{-7}}{1000}$ mole H^+ 1.33×10^{-7} ml — " 1.33×10^{-17} so, no of H^+ ions = $1.33 \times 10^{-17} \times N_A$ Ribose and 2-deoxyribose can be differentiated by	so,10 million th part of 1 = 1.33×10^{-7} ml	
45.	Ans : (C) Hints : Now $[H^+] = 10^{-7}$ mole / litre Now 1000 ml contains 10^{-7} mole. H^+ $1ml$ " $\frac{10^{-7}}{1000}$ mole H^+ 1.33×10^{-7} ml — " 1.33×10^{-17} so, no of H^+ ions = $1.33 \times 10^{-17} \times N_A$ Ribose and 2-deoxyribose can be differentiated by (A) Fehling's reagent (B) Tollens's reagent	so,10 million th part of 1 = 1.33×10^{-7} ml	

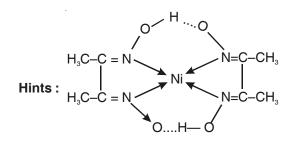








WBJEE - 2013 (Answers & Hints) Chemistry 55. On heating, chloric acid decompose to (A) $HCIO_4$, CI_9 , O_9 and H_9O (B) $HCIO_2$, CI_2 , O_2 and H_2O (D) HCl, HClO, Cl₂O and H₂O (C) HCIO, Cl₂O and H₂O₂ Ans:(A) Hints : Fact **CATEGORY - III** Q. 56 – Q. 60 carry two marks each, for which one or more than one options may be correct. Marking of correct options will lead to a maximum mark of two on pro rata basis. There will be no negative marking for these questions. However, any marking of wrong option will lead to award of zero mark against the respective question-irrespective of the number of correct options marked. 56. Consider the following reaction for $2NO_3(g) + F_3(g) \rightarrow 2NO_3F(g)$. The expression for the rate of reaction interms of the rate of change of partial pressures of reactant and product is/are (A) rate = $-\frac{1}{2}[dp(NO_2)/dt]$ (B) rate = $\frac{1}{2}[dp(NO_2)/dt]$ (C) rate = $-\frac{1}{2}[dp(NO_2F)/dt]$ (D) rate = $\frac{1}{2}[dp(NO_2F)/dt]$ Ans : (A, D) Hints: Fact 57. Tautomerism is exhibited by (Me₂CCO)₂CH (B) Ans : (A, B, D) Hints : (CH₃)CCO (CH_a)CCO (CH₃)CCC Availability of acidic α H-atoms at these positions(shown by arrow marks) enable the compounds to show keto-enol tautomerism 58. The important advantage(s) of Lintz and Donawitz (L.D.) process for the manufacture of steel is (are) (A) The process is very quick (B) Operating costs are low (C) Better quality steel is obtained (D) Scrap iron can be used Ans: (A, C, D) Hints: Fact 59. In basic medium the amount of Ni²⁺ in a solution can be estimated with the dimethylglyoxime reagent. The correct statement(s) about the reaction and the product is(are) (A) In ammoniacal solution Ni²⁺ salts give cherry-red precipitate of nickel (II) dimethylglyoximate (B) Two dimethylglyoximate units are bound to one Ni²⁺ (C) In the complex two dimethylglyoximate units are hydrogen bonded to each other (D) Each dimethylglyoximate unit forms a six-membered chelate ring with Ni²⁺ Ans: (A, B, C)



- 60. Correct statement(s) in cases of n-butanol and t-butanol is (are)
 - (A) Both are having equal solubility in water
- (B) t-butanol is more soluble in water than n-butanol
- (C) Boiling point of t-butanol is lower than n-butanol Ans:(B,C)
- (D) Boiling point of n-butanol is lower than t-butanol

Hints : More branching means less boiling point and high solubility

